



CS491/691: Introduction to Aerial Robotics

Topic: Navigation Sensors

Dr. Kostas Alexis (CSE)

Navigation Sensors

- ▶ Providing the capacity to estimate the **state** of the aerial robot
 - ▶ Self-Localize and estimate its pose in the environment
 - ▶ Often this infers to also derive the map of the environment
 - ▶ In some cases also rely in external systems (e.g. GPS), while a lot of work is undergoing into making aerial robots completely autonomous.



Classification of Sensors

➤ What:

➤ **Proprioceptive sensors**

- Measure values internally to the robot.
 - Angular rate, heading.

➤ **Exteroceptive sensors**

- Information from the robot environment
 - Distances to objects, extraction of features from the environment.

➤ How:

➤ **Passive Sensors**

- Measure energy coming from a signal of the environment – very much influenced from the environment.

➤ **Active Sensors**

- Emit their proper energy and measure reaction.
- Better performance, but some influence on the environment.
- Not always easily applicable concept.



Uncertainty Representation

- ▶ **Sensing is always related to uncertainties**

- ▶ How can uncertainty be represented or quantified?
- ▶ How do they propagate – uncertainty of a function of uncertain values?

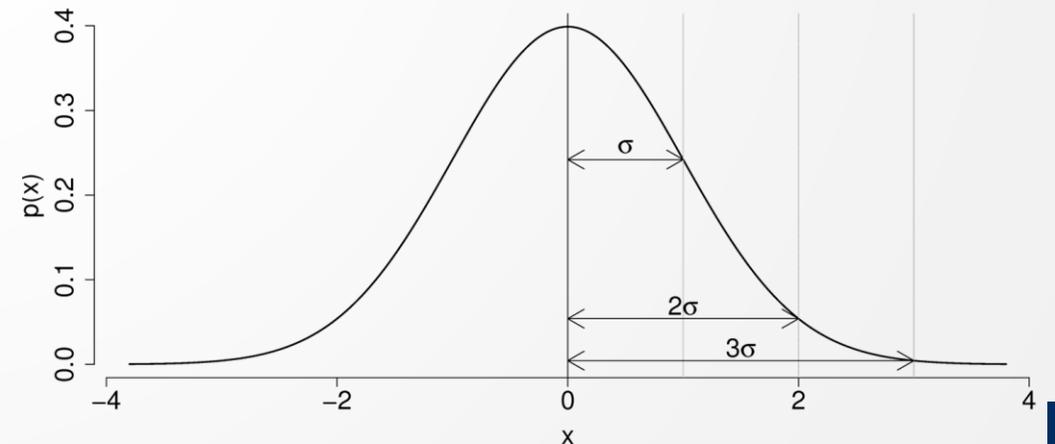
- ▶ **Systematic errors**

- ▶ They are caused by factors or processes that can in theory be modeled and, thus, calibrated, (for example the misalignment of a 3-axes accelerometer)

- ▶ **Random errors**

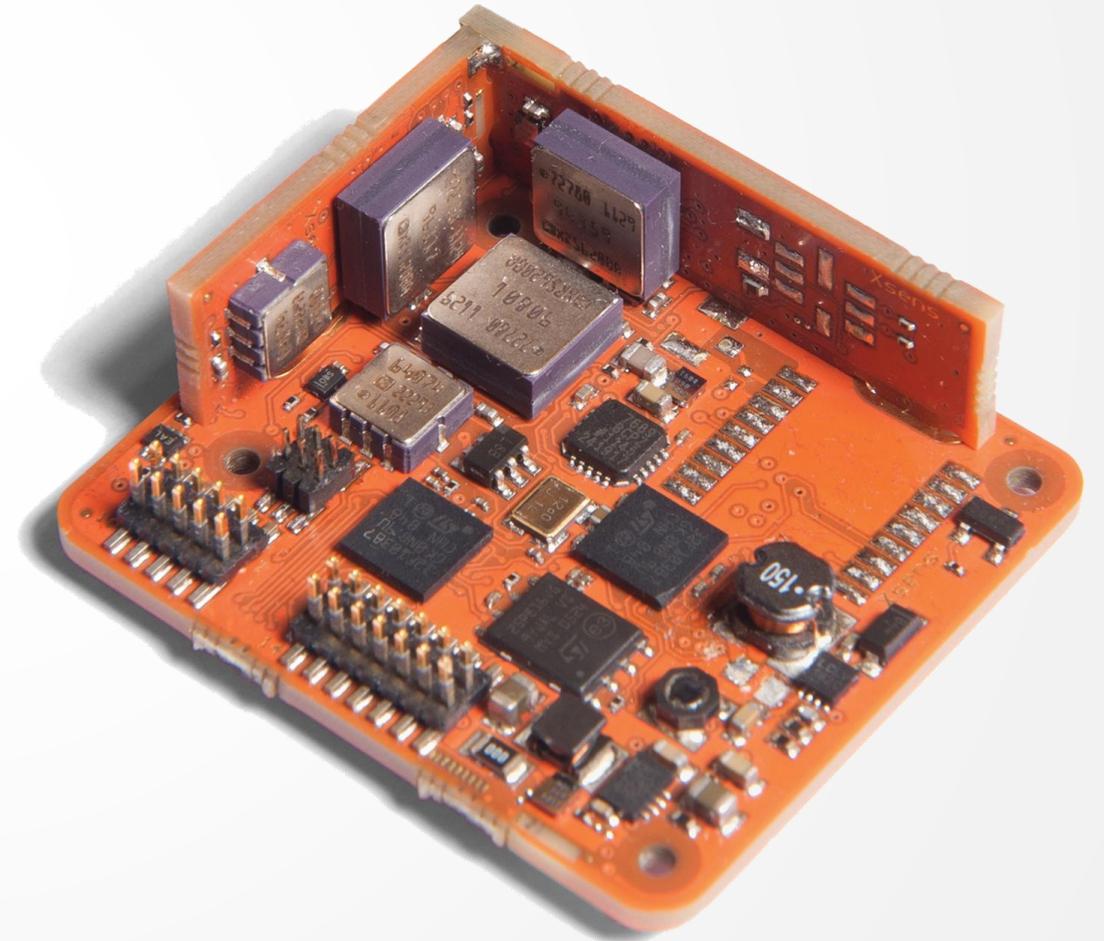
- ▶ They cannot be predicted using a sophisticated model but can only be described in probabilistic terms

Normal distribution when $\mu=0$ and $\sigma=1$



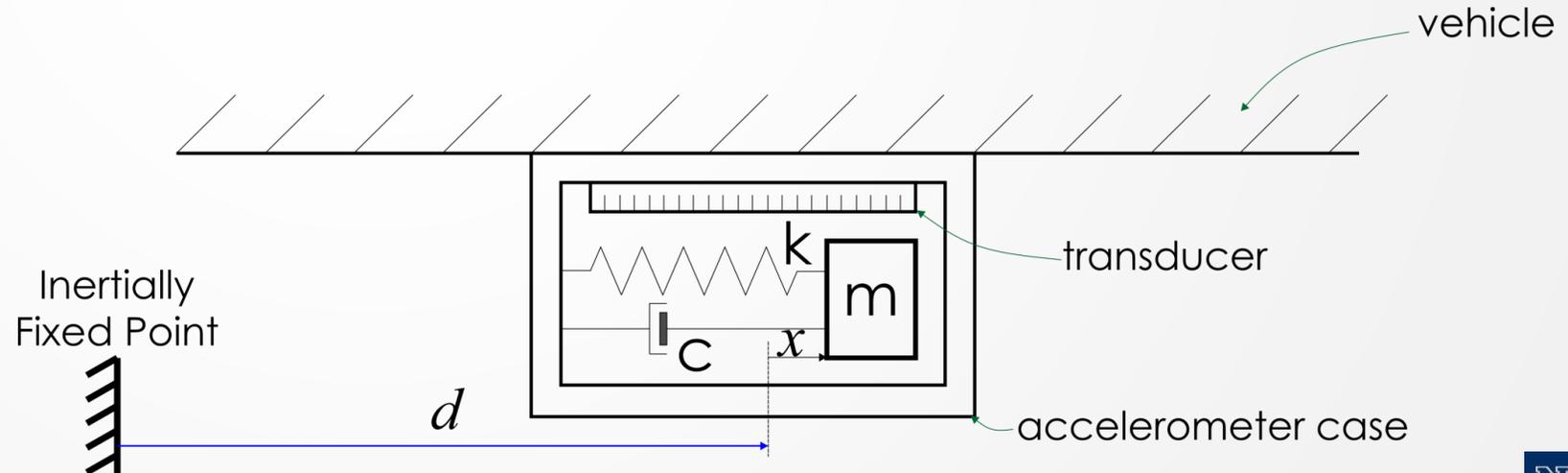
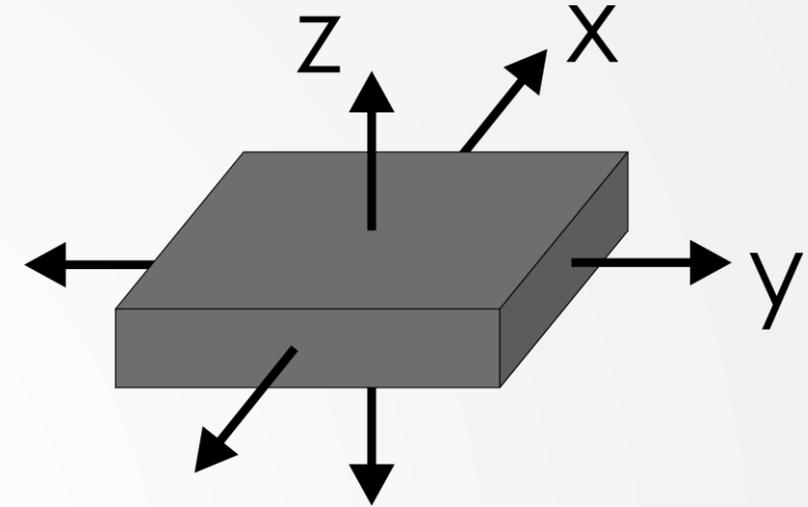
Typical Navigation Sensors

- ▶ The following sensors are commonly used for the navigation of aerial robots:
 - ▶ **Inertial Sensors:**
 - ▶ Accelerometers
 - ▶ Gyroscopes
 - ▶ **Magnetometers (digital compass)**
 - ▶ **Pressure Sensors**
 - ▶ Barometric pressure for altitude sensing
 - ▶ Airspeed measurements
 - ▶ **GPS**
 - ▶ **Camera based systems**
 - ▶ **Time-of-Flight sensors**



Accelerometer

- ▶ Accelerometers are devices that **measure proper acceleration** ("g-force"). Proper acceleration is not the same as coordinate acceleration (rate of change of velocity). For example, an accelerometer at rest on the surface of the Earth will measure an acceleration $g = 9.81 \text{ m/s}^2$ straight upwards.
- ▶ Accelerometers are electromechanical devices that are able of measuring static and/or dynamic forces of acceleration. Static forces include gravity, while dynamic forces can include vibrations and movement. Accelerometers can measure acceleration on 1, 2 or 3 axes.

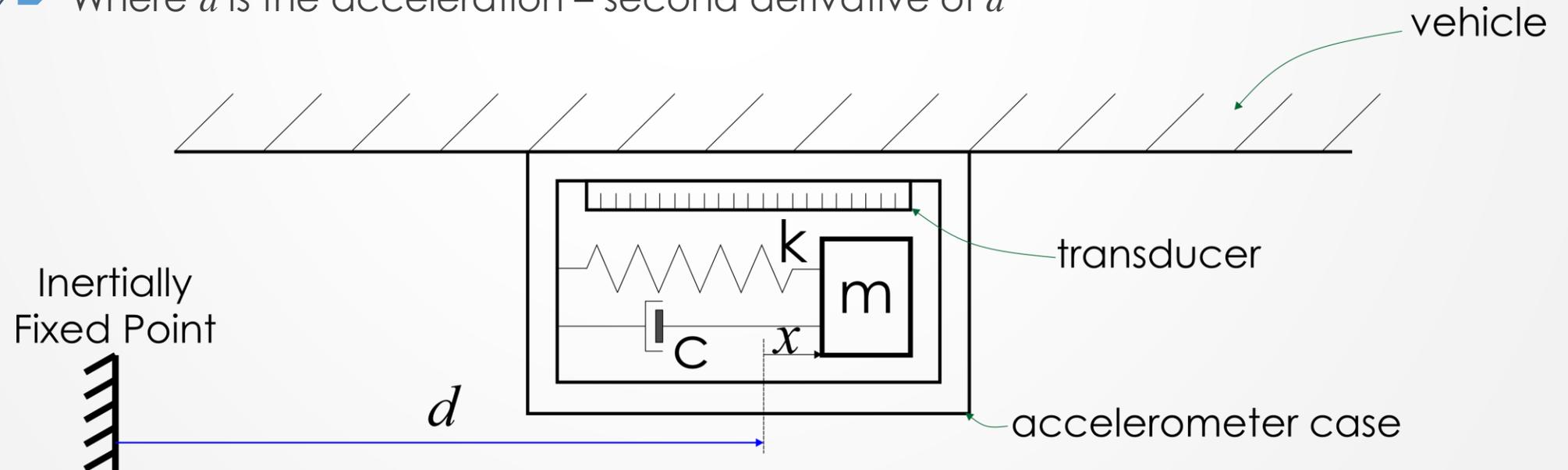


Accelerometer

- ▶ Simplified Accelerometer Model:

$$m\left(\frac{d^2}{dt^2}(d+x)\right) = F_x \Rightarrow m\left(\frac{d^2}{dt^2}(d+x)\right) = -c\frac{dx}{dt} - kx \Rightarrow$$
$$m(\ddot{d} + \ddot{x}) + c\dot{x} + kx = 0 \Rightarrow m\ddot{x} + c\dot{x} + kx = -ma$$

- ▶ Where a is the acceleration – second derivative of d

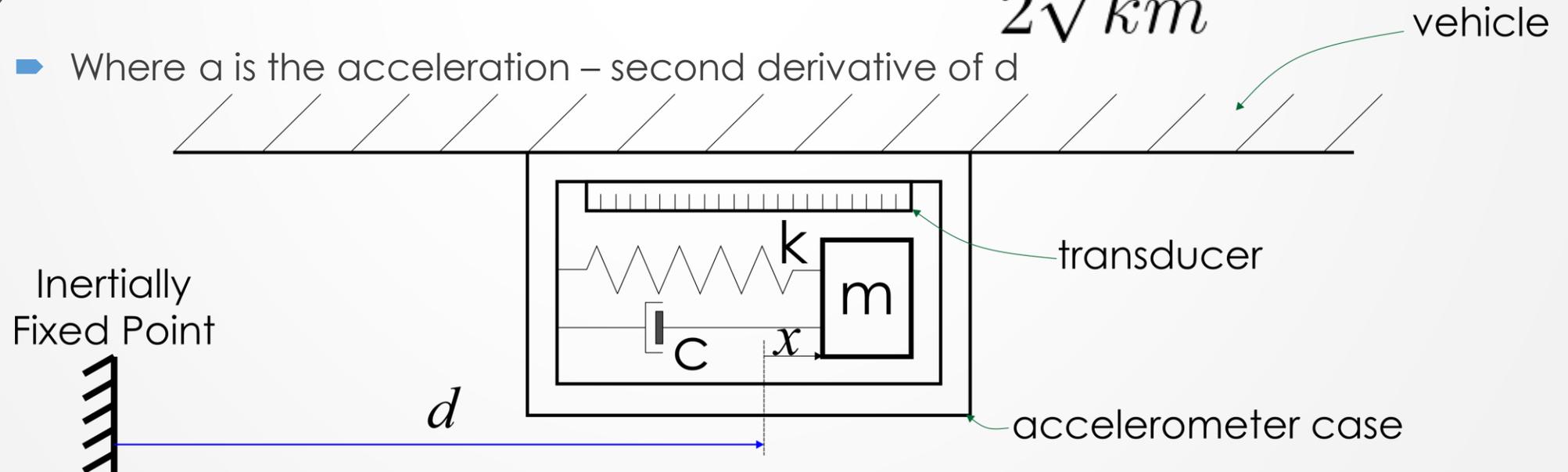


Accelerometer

- ▶ For the cases within which, the vehicle acceleration is constant, then the steady state output of the accelerometer is also constant, therefore indicating the existence and value of the acceleration.
- ▶ The **undamped natural frequency** and the **damping ratio** of the accelerometer are:

$$\omega_n = \sqrt{k/m}, \quad \zeta = \frac{c}{2\sqrt{km}}$$

- ▶ Where a is the acceleration – second derivative of d

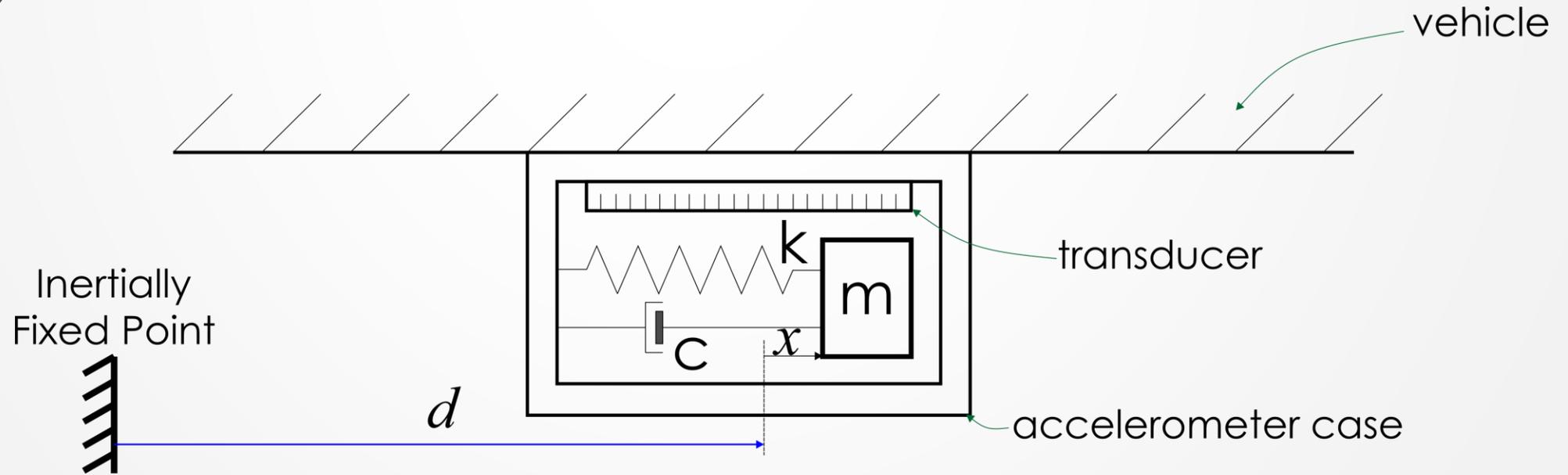


Accelerometer

- ▶ **Bias effects on accelerometers:** accelerometer measurements are degraded by scale errors and bias effects. A typical error model takes the form:

$$\mathbf{a}_{3D} = \mathbf{M}_{acc} \mathbf{a}_{3D}^m - \mathbf{a}_{bias} + \mathbf{a}_n$$

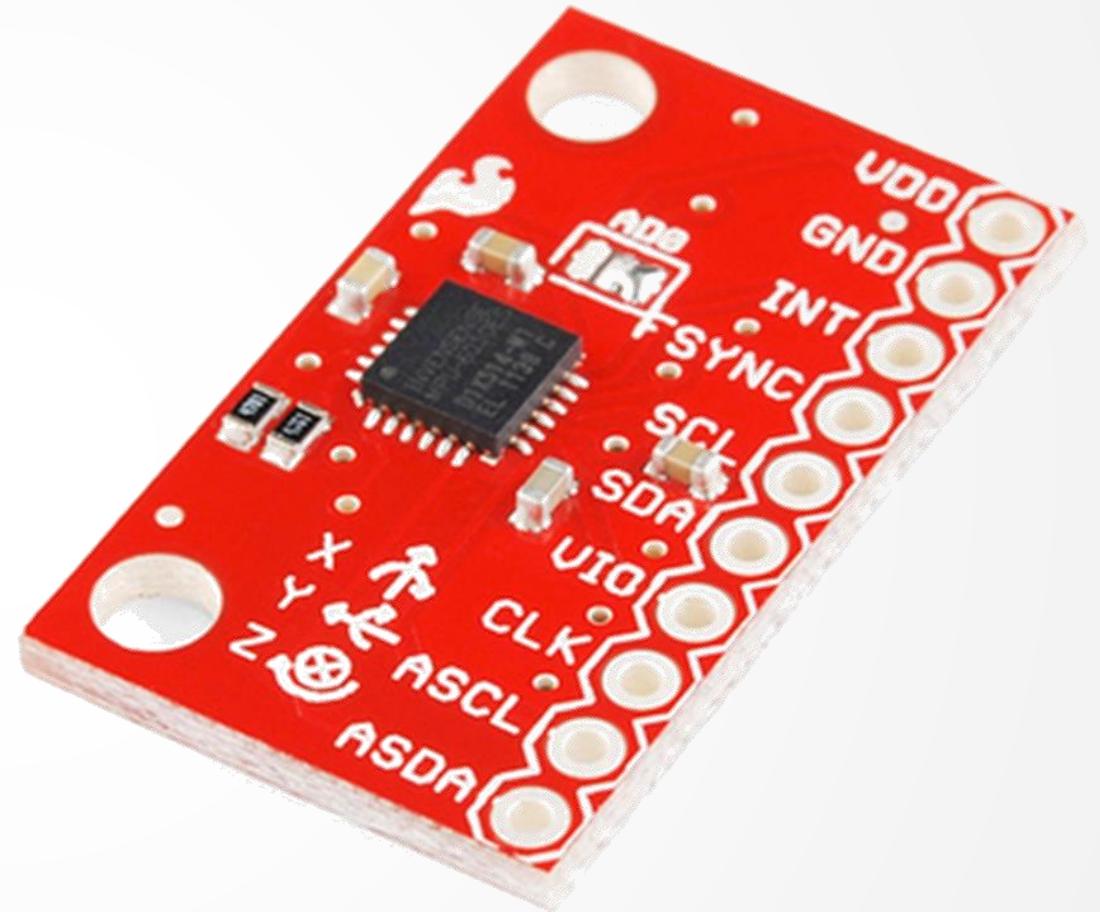
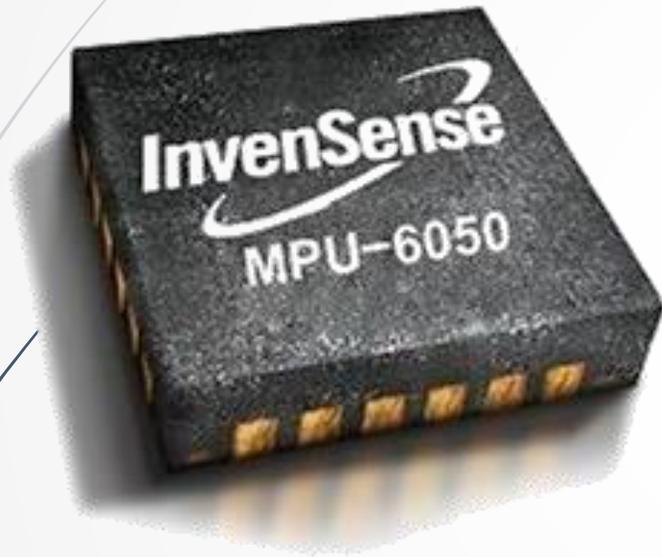
- ▶ Where a_{3D} stands for the 3-axes acceleration, M_{acc} for combined scale factor and misalignment compensation, a_{3D}^m for the measurement, a_{bias} for bias signal and a^n for zero mean noise.



Accelerometer

- ▶ MEMS Accelerometers are widely used in UAVs. But they are not the only working principle.
- ▶ **Types of accelerometers:**
 - ▶ Bulk micromachined capacitive
 - ▶ Bulk micromachined piezoelectric resistive
 - ▶ Capacitive spring mass base
 - ▶ DC response
 - ▶ Electromechanical servo (Servo Force Balance)
 - ▶ High gravity
 - ▶ High temperature
 - ▶ Laser accelerometer
 - ▶ Low frequency
 - ▶ Magnetic induction
 - ▶ Modally tuned impact hammers
 - ▶ Null-balance
 - ▶ Optical
 - ▶ Pendulous integrating gyroscopic accelerometer (PIGA)
 - ▶ Piezoelectric accelerometer
 - ▶ Quantum (Rubidium atom cloud, laser cooled)
 - ▶ Resonance
 - ▶ Seat pad accelerometers
 - ▶ Shear mode accelerometer
 - ▶ Strain gauge
 - ▶ Surface acoustic wave (SAW)
 - ▶ Surface micromachined capacitive (MEMS)
 - ▶ Thermal (submicrometre CMOS process)
 - ▶ Triaxial
 - ▶ Vacuum diode with flexible anode[38]
 - ▶ potentiometric type
 - ▶ LVDT type accelerometer

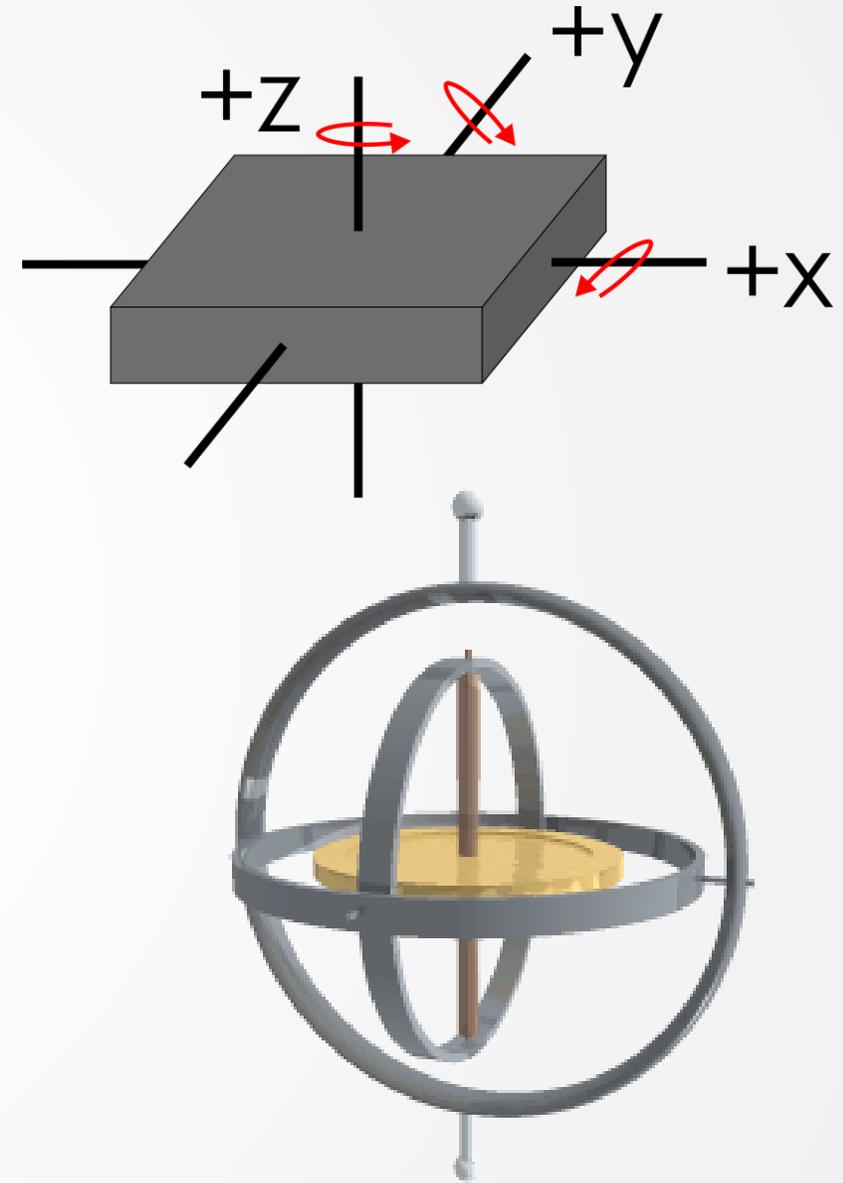
Accelerometer



- ▶ That is a complete IMU, 3-axes accelerometer, 3-axes gyroscope, 3-axes magnetometer. Overall it is much smaller than a coin!

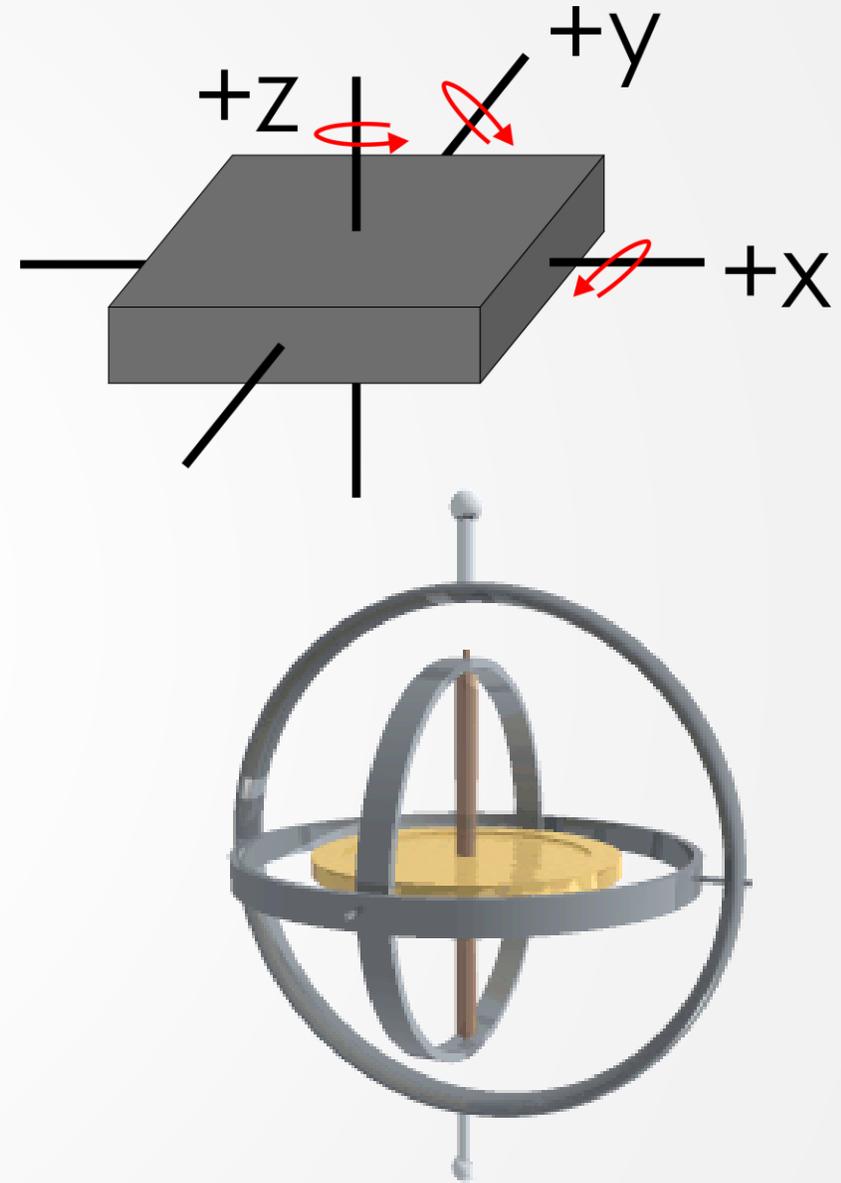
Gyroscope

- ▶ **A gyroscope is - conceptually - a spinning wheel in which the axis of rotation is free to assume any possible orientation.** When rotating, the orientation of this axis remains unaffected by tilting or rotation of the mounting, according to the conservation of angular momentum. Due to this principle, a gyroscope can lead to the measurement of orientation and its rate of change. The word comes from the Greek "γύρος" and σκοπεύω which mean "circle" and "to look" correspondingly.
- ▶ Nowadays, we are mostly using gyroscopes that are based on different operating principles. In aviation we especially focus on MEMS gyroscopes or solid-state ring lasers, and fibre optic gyroscopes. In small-scale aerial robotics, we mostly care for MEMS gyroscopes.



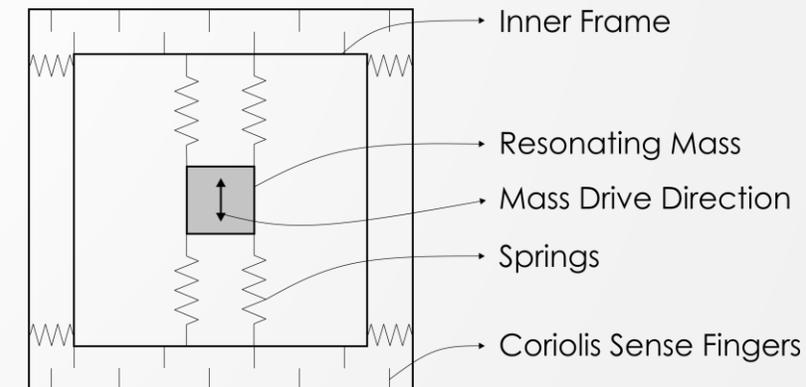
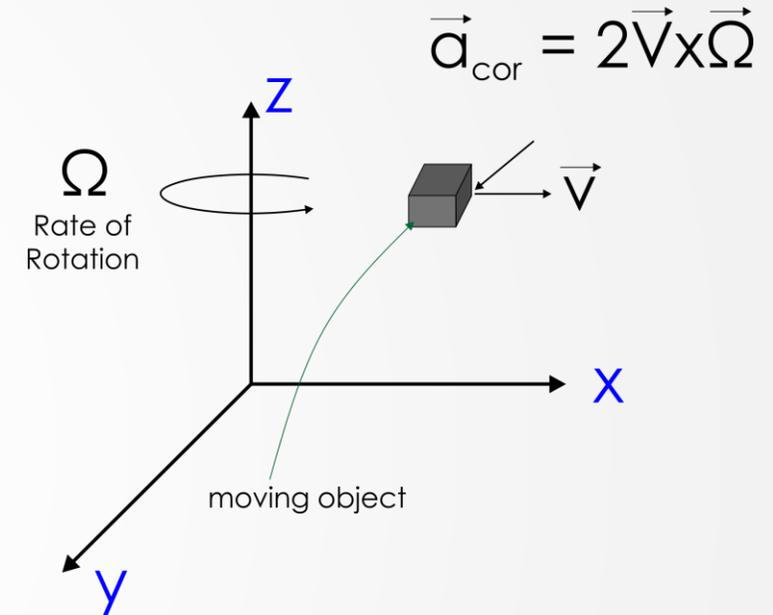
Gyroscope

- ▶ A classical rotary gyroscope relies on the **law of conservation of angular momentum**.
 - ▶ **The total angular momentum of a system remains constant in both magnitude and direction of the resultant external torque acting upon the system is zero.**
- ▶ Gyroscopes exploiting this principle, typically consist of a spinning disk or mass on an axle, which is then mounted on a series of gimbals. Each of these gimbals provides the spinning disk an additional degree of freedom.
- ▶ Therefore, as long as the gyroscope is spinning, it will maintain a constant orientation. In the case that external torques or rotations about a given axis are present in these devices, orientation can be maintained, and measurement of angular velocity can take place - due to the phenomenon of precession.
 - ▶ **The phenomenon of precession takes place when an object that is spinning about some axis (its "spin axis") has an external torque applied in a direction perpendicular to the spin axis (the input axis).** In a rotational system, when net external torques are present, the angular momentum vector (along the spin axis) will move in the direction of the applied external torque vector. Consequently, the spin axis rotates about an axis that is perpendicular to both the input axis and the spin axis (this is now the output axis).
- ▶ This rotation about the output axis is then sensed and fed back to the input axis where a motor-like device applies torque in the opposite direction therefore canceling the precession of the gyroscope and maintaining its orientation.
 - ▶ To measure rotation rate, counteracting torque is pulsed at periodic time intervals. Each pulse represents a fixed step of angular rotation, and the pulse count in a fixed time interval will be proportional to the angle change θ over that time period.



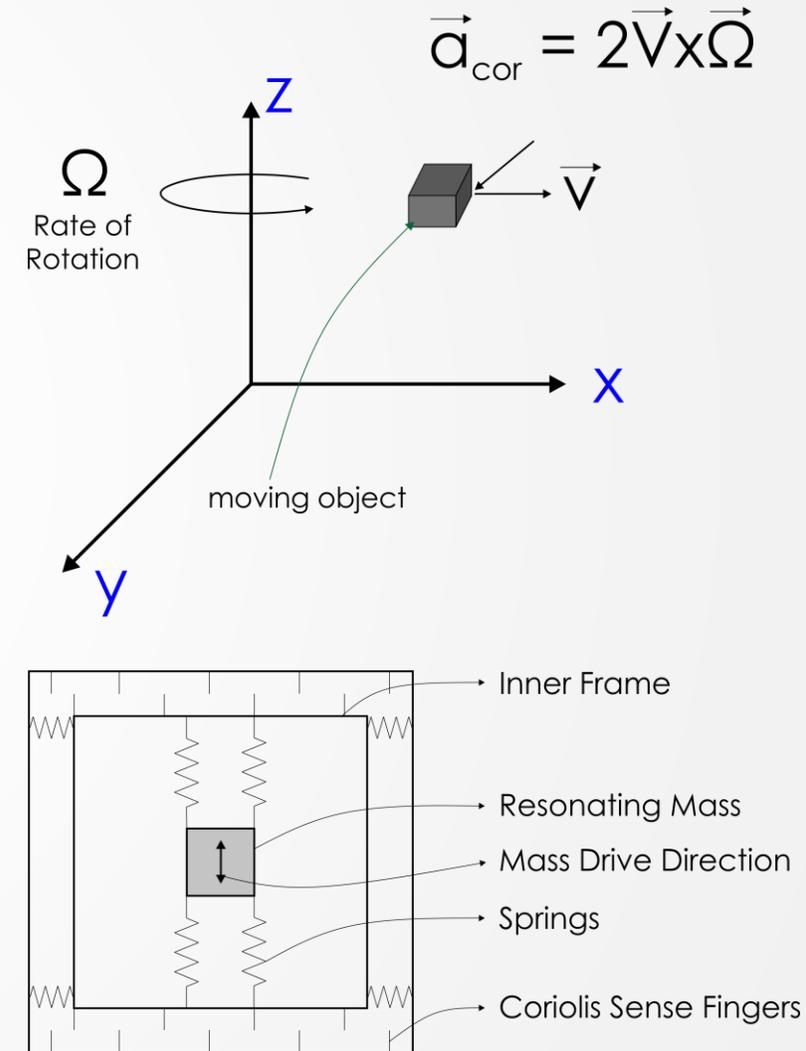
Gyroscope

- MEMS gyroscopes are micro vibrating structures that base their operation the phenomenon of **Coriolis force**.
- In a rotating system, every point rotates with the same rotational speed. As one approaches the axis of rotation of this system, the rotational speed remains the same, but the speed in the direction perpendicular to the rotation axis decreases.
 - In order to travel along a straight line towards or away from the axis of rotation, lateral speed must be adjusted in order to maintain the same relative angular position on the body.
 - The Coriolis force corresponds to the product of the object mass (whose longitude is to be maintained) times the acceleration that leads to the required slowing down or speeding up.
 - The Coriolis force is proportional to both the angular velocity of the rotating object, as well as to the velocity of the object moving towards or away from the axis of rotation.**



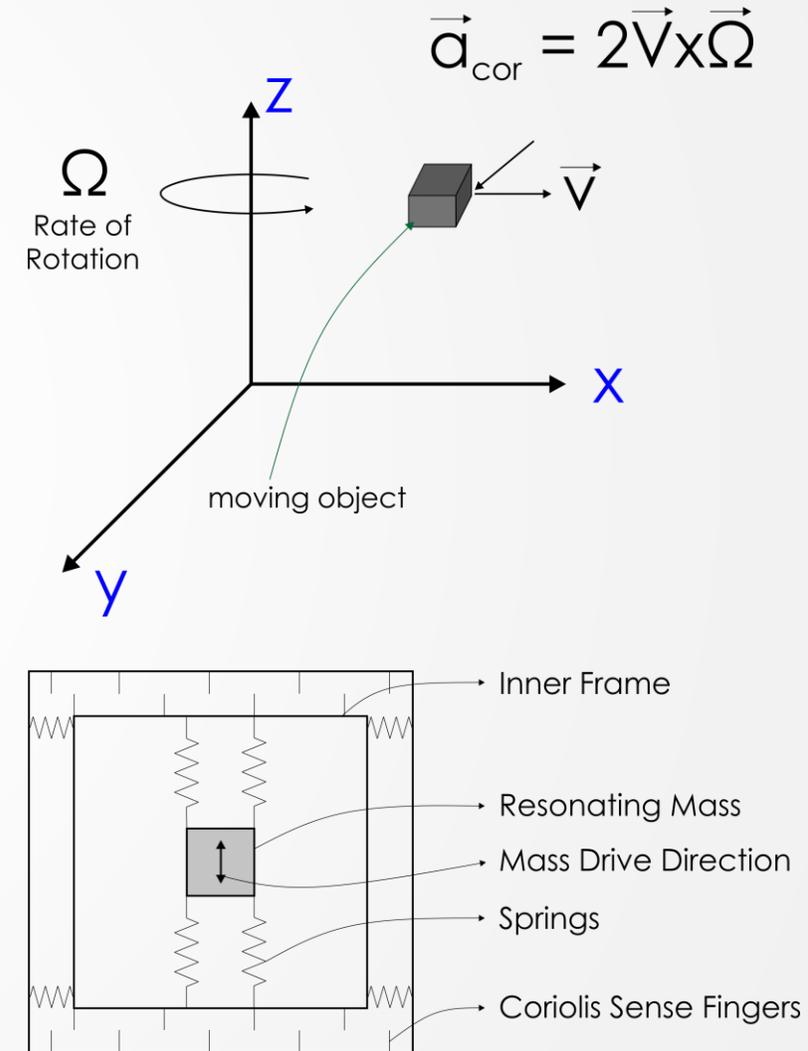
Gyroscope

- ▶ **Fabrication:** a micro-machined mass which is connected to an outer housing by a pair of springs. This outer housing is then connected to the fixed circuit board using a second set of orthogonal springs.
 - ▶ The test mass is continuously driven sinusoidally along the first set of springs. As any rotation of the system will induce Coriolis acceleration in the mass, it will subsequently push it in the direction of the second set of springs.
 - ▶ As the mass is driven away from the axis of rotation, the mass will be pushed perpendicularly in one direction, and as it is driven back toward the axis of rotation, it will be pushed in the opposite direction, due to the Coriolis force acting on the mass.
- ▶ **Coriolis force sensing:** Coriolis force is sensed and detected by capacitive sense fingers that are integrated along the test mass housing and the rigid structure.
 - ▶ **As the test mass is pushed by the Coriolis force, a differential capacitance will develop and will be detected as the sensing fingers are brought closer together.** When the mass is pushed in the opposite direction, different sets of sense fingers are brought closer together.
 - ▶ The sensor can detect both the magnitude as well as the direction of the angular velocity of the system.



Gyroscope

- ▶ **Bias effects on Gyros:** The biggest problem with gyros (and what essentially constraints us from simply performing integrating actions on their measurements), is the existence of bias effects. Bias are mostly caused by:
 - ▶ Drive excitation feedthrough
 - ▶ Output electronics offsets
 - ▶ Bearing torques
- ▶ **Biases are present in three forms** - as far as their expression and time evolution is concerned - namely:
 - ▶ Fixed bias ("const")
 - ▶ Bias variation from one turn-on to another (thermal), called bias stability ("BS")
 - ▶ Bias drift, usually modeled as a random walk ("BD")



Gyroscope

- As the bias effect are additive, we may write:

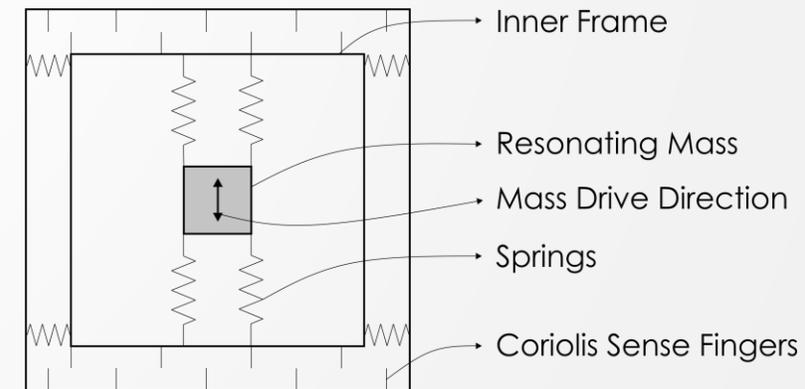
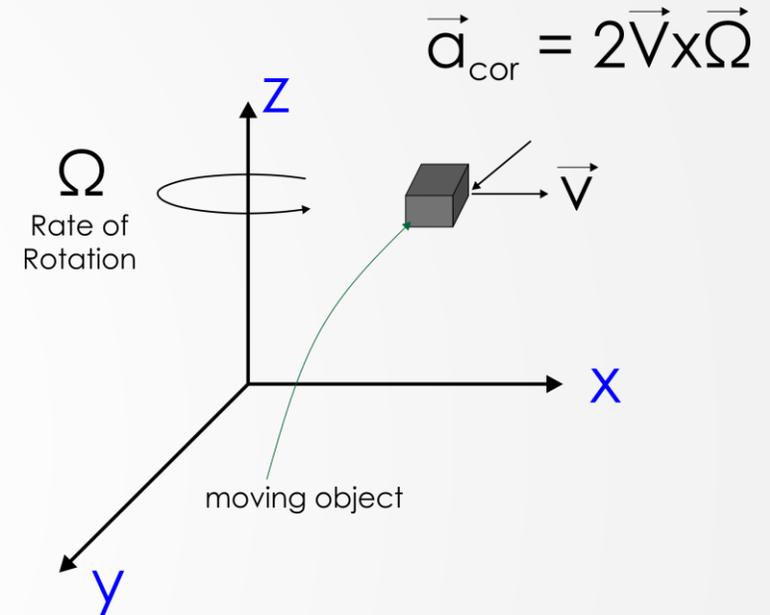
$$\delta\omega_{bias} = \delta\omega_{const} + \delta\omega_{BS} + \delta\omega_{BD}$$

$$\frac{d}{dt}\omega_{BD} = \omega(t); \omega \sim N(O, Q)$$

- Where Q is known
- Error model a single-axis gyroscope:**

$$\omega_{1D} = k_g \omega_{1D}^m - \omega_{bias} + \omega_n$$

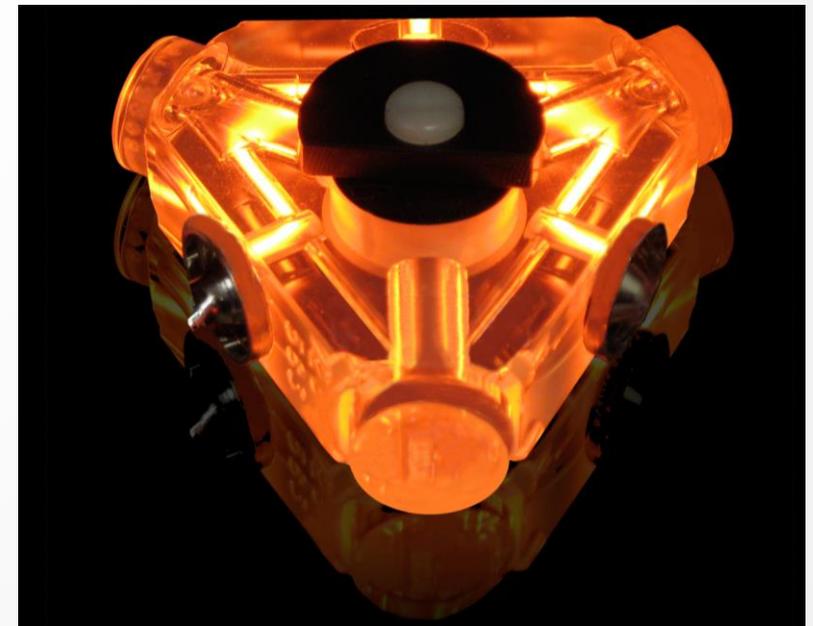
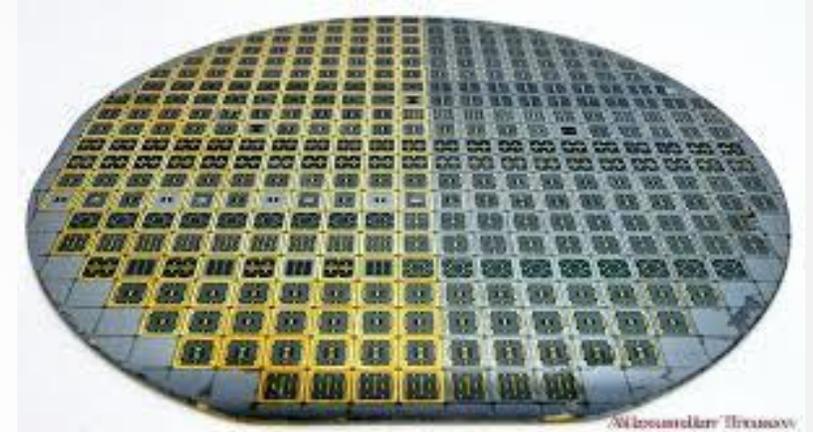
- ω_{bias} : bias model
 $\dot{\omega}_{bias} = n_\omega, E[n_\omega] = 0, E[n_\omega(t)n_\omega^T(t')] = n(t-t'), E[n_\omega(t)n_\omega^T(t')] = 0$
- ω_n : noise model
 $\omega_n : E[\omega_n] = 0, E[\omega_n(t)\omega_n^T(t')] = N_r\delta(t-t')$



Gyroscope

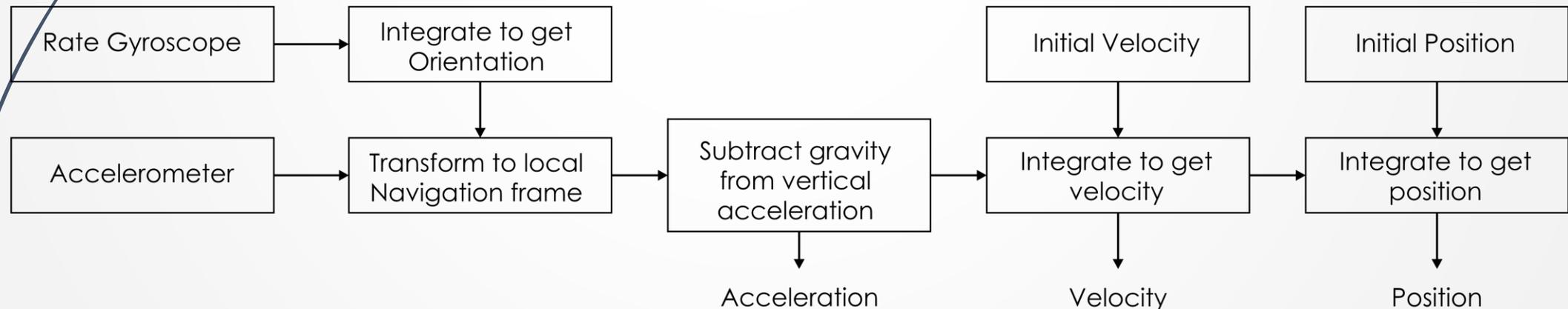
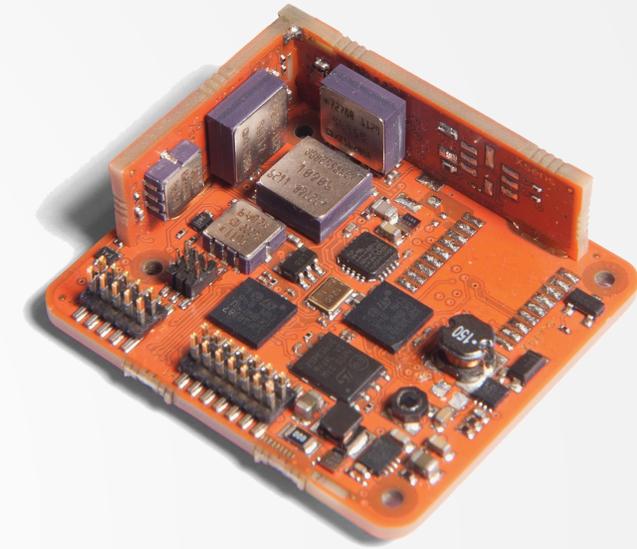
Types of gyroscopes:

- ▶ Gyrostat
- ▶ Micro ElectroMechanical Systems (MEMS)
- ▶ Fibre Optic Gyroscope (FOG)
- ▶ Hemispherical Resonator Gyroscope (HRG)
- ▶ Vibrating Structure Gyroscope (VSG)
- ▶ Dynamically Tuned Gyroscope (DTG)
- ▶ Ring Laser Gyroscope (RLG)
- ▶ London moment gyroscope



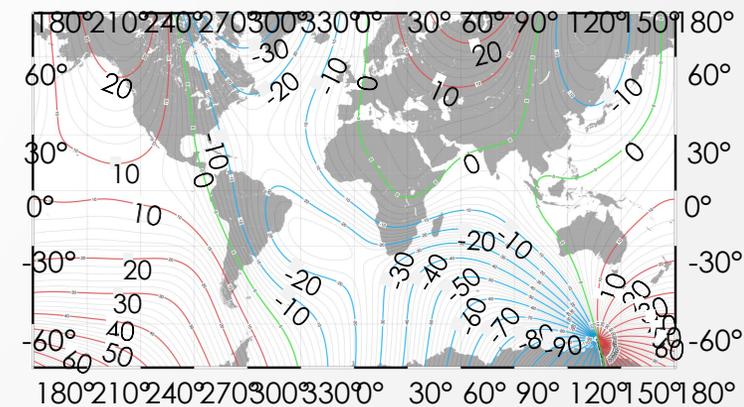
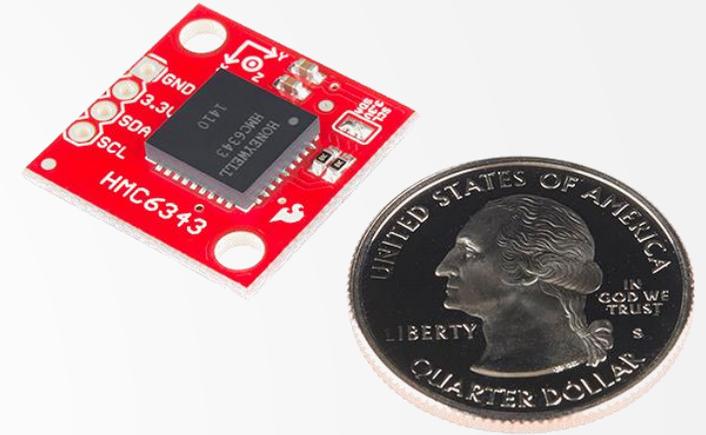
IMU

- ▶ It uses gyroscopes and accelerometers to estimate the relative pose (position and orientation), velocity and acceleration of a moving vehicle with respect to an inertial frame.
- ▶ In order to estimate the motion, the gravity vector must be subtracted and the initial velocity has to be known.
- ▶ After long periods of operation, drifts occur: need external reference to cancel it.



Magnetometer

- ▶ A magnetometer is a type of sensor that measures the strength and direction of the local magnetic field. The magnetic field measured will be a combination of both the earth's magnetic field and any magnetic field created by nearby objects. The magnetic field is measured in the sensor reference frame.
- ▶ The earth's magnetic field is a self sustaining magnetic field that resembles a magnetic dipole with one end near the Earth's geographic North Pole and the other near the earth's geographic South Pole. The strength of this magnetic field varies across the Earth with strengths as low as 0.3 Gauss in South America to over 0.6 Gauss in northern Canada.



Magnetometer

- ▶ Heading is the sum of the magnetic declination angle and the magnetic heading:

$$\psi = \delta + \psi_m$$

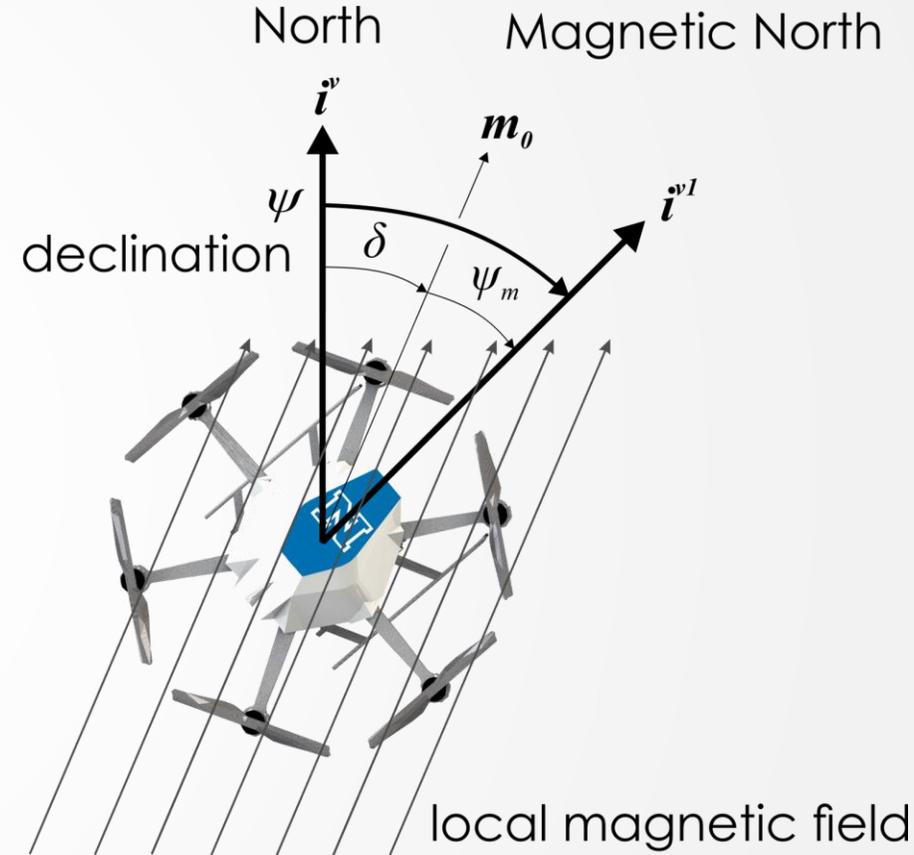
- ▶ Magnetic heading determined from measurements of body-frame components of magnetic field projected onto the horizontal plane:

$$\mathbf{m}_0^{v1} = \begin{bmatrix} m_{0x}^{v1} \\ m_{0y}^{v1} \\ m_{0z}^{v1} \end{bmatrix} = \mathcal{R}_b^{v1}(\phi, \theta) \mathbf{m}_0^b = \mathcal{R}_{v2}^{v1}(\theta) \mathcal{R}_b^{v2}(\phi) \mathbf{m}_0^b \Rightarrow$$

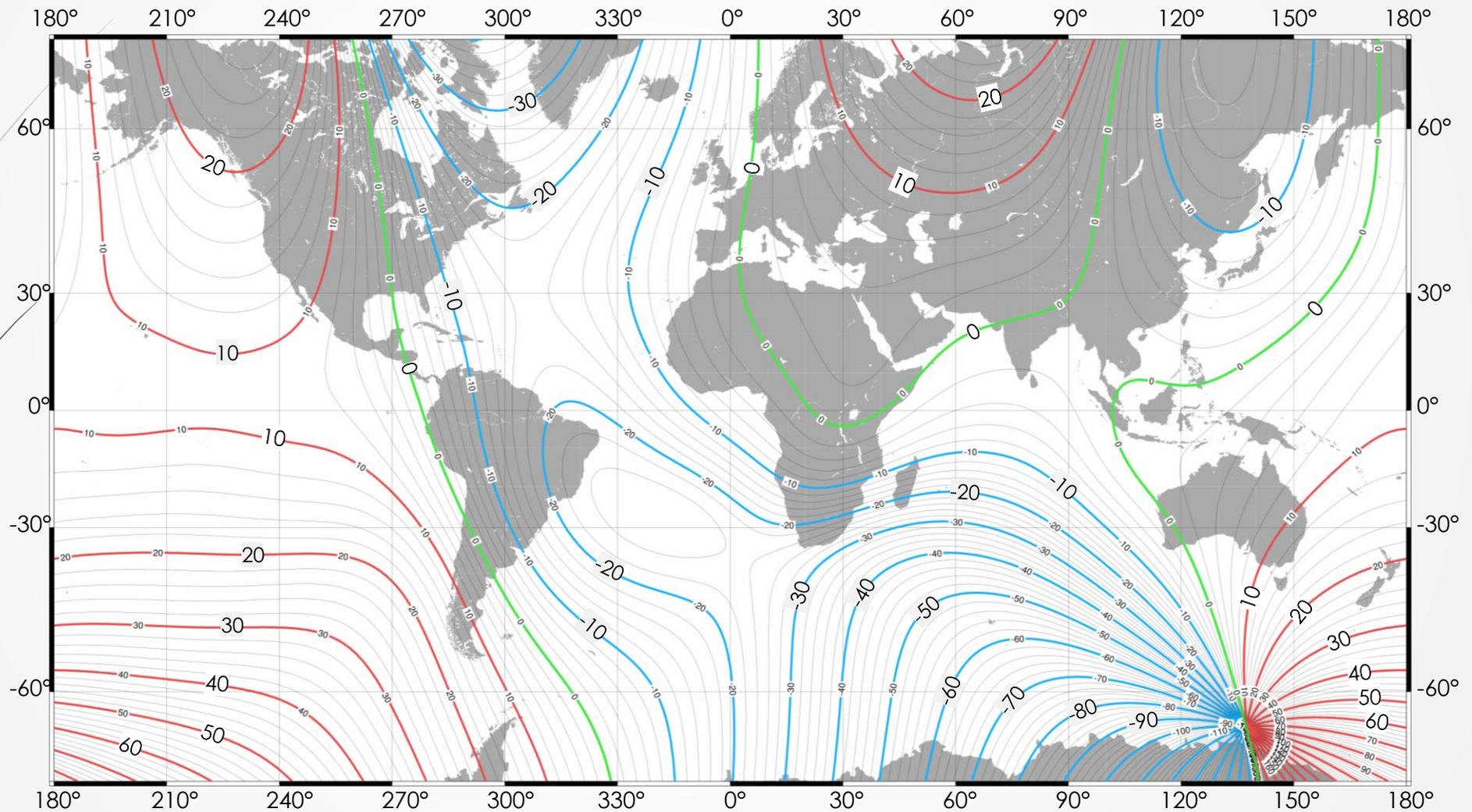
$$\begin{bmatrix} m_{0x}^{v1} \\ m_{0y}^{v1} \\ m_{0z}^{v1} \end{bmatrix} = \begin{bmatrix} c_\theta & s_\theta s_\phi & s_\theta c_\phi \\ 0 & c_\phi & -s_\phi \\ -s_\theta & c_\theta s_\phi & c_\theta c_\phi \end{bmatrix} \mathbf{m}_0^b$$

- ▶ Solving for heading:

$$\psi = -\arctan 2(m_{0y}^{v1}, m_{0x}^{v1})$$



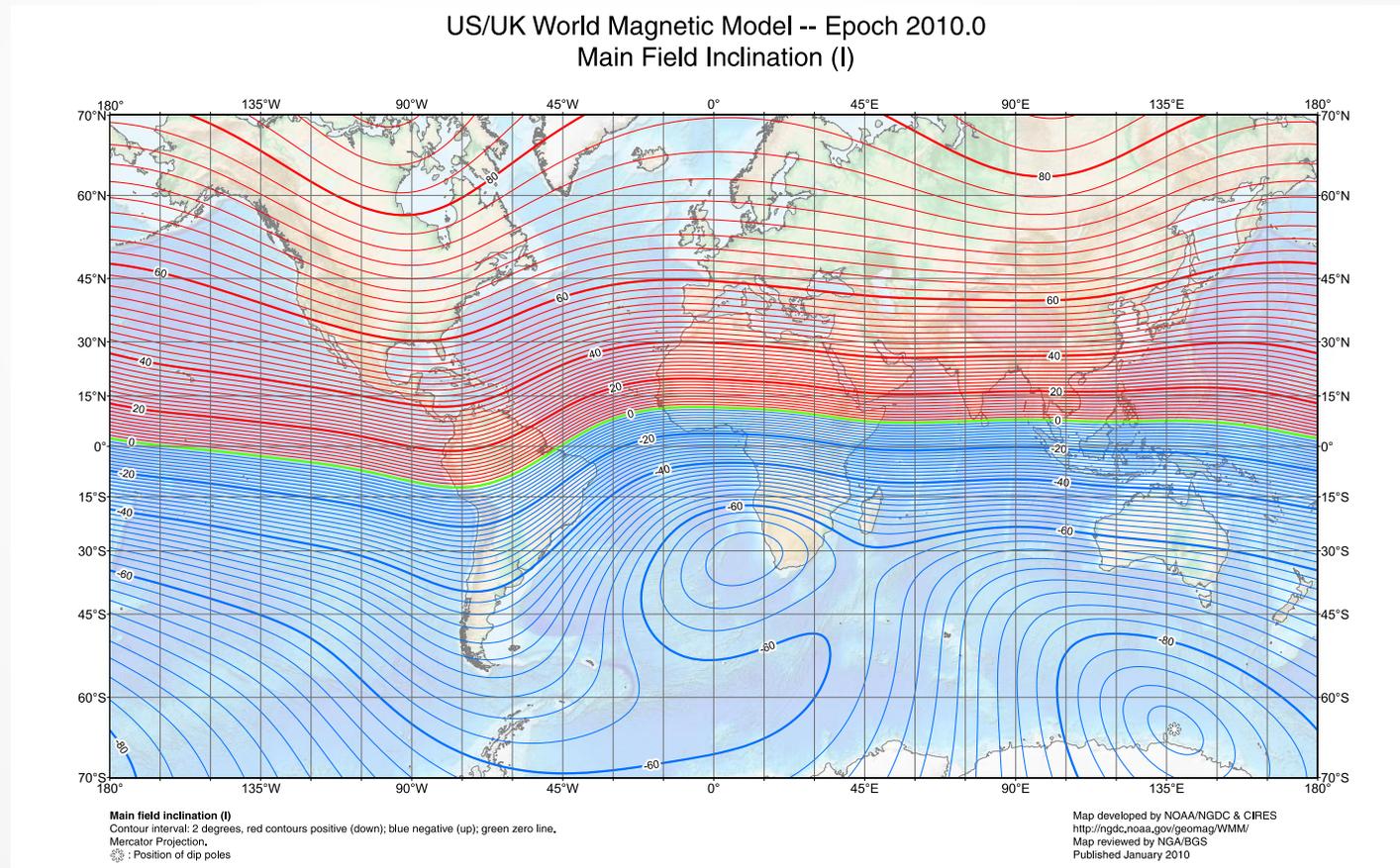
Magnetic Declination Variation



World Magnetic Model, National Geophysical Data Center

Magnetic Inclination

Magnetic dip or magnetic inclination is the angle made by a compass needle with the horizontal at any point on the Earth's surface. Positive values of inclination indicate that the field is pointing downward, into the Earth, at the point of measurement.



Pressure Measurements

- ▶ A pressure sensor measures pressure, typically of gases or liquids. Pressure is an expression of the force required to stop a fluid from expanding, and is usually stated in terms of force per unit area. A pressure sensor usually acts as a transducer; it generates a signal as a function of the pressure imposed.
- ▶ **Pressure sensing:**
 - ▶ This is where the measurement of interest is pressure, expressed as a force per unit area. This is useful in weather instrumentation, aircraft, automobiles, and any other machinery that has pressure functionality implemented.
- ▶ **Altitude sensing:**
 - ▶ This is useful in aircraft, rockets, satellites, weather balloons, and many other applications. All these applications make use of the relationship between changes in pressure relative to the altitude.



Pressure Measurements

- ▶ The basic equation of hydrostatics is:

$$P_2 - P_1 = \rho g(z_2 - z_1)$$

- ▶ Using the ground as reference, and assuming constant air density gives:

$$P - P_{ground} = -\rho g(h - h_{ground}) = -\rho g h_{AGL}$$

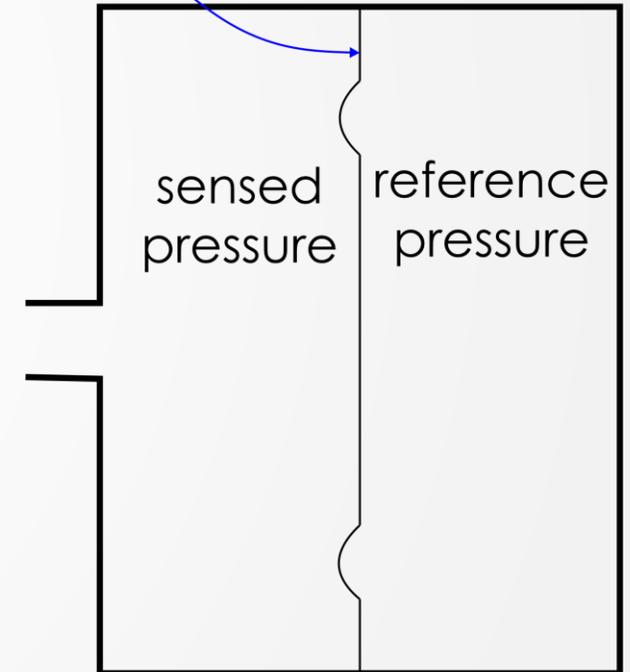
- ▶ AGL: Above Ground Level
- ▶ Below 11,000m, the barometric formula can be used:

$$P = P_0 \left[\frac{T_0}{T_0 + L_0 h_{ASL}} \right]^{\frac{gM}{RL_0}}$$

- ▶ Where:

- ▶ P_0 : standard pressure at sea level
- ▶ T_0 : standard temperature at sea level
- ▶ L_0 : rate of temperature decrease
- ▶ g : gravitational constant
- ▶ R : universal gas constant for air
- ▶ M : standard molar mass of atmospheric air (takes into account change in density with altitude and temperature)

strain-sensing
diaphragm



Pressure Measurements

- ▶ Altitude Measurement:

- ▶ We usually assume that the density is constant (valid for small altitude variations):

$$y_{abspres} = (P_{ground} - P) + \beta_{abspres} + \eta_{abspres} = \rho g h_{AGL} + \beta_{abspres} + \eta_{abspres}$$

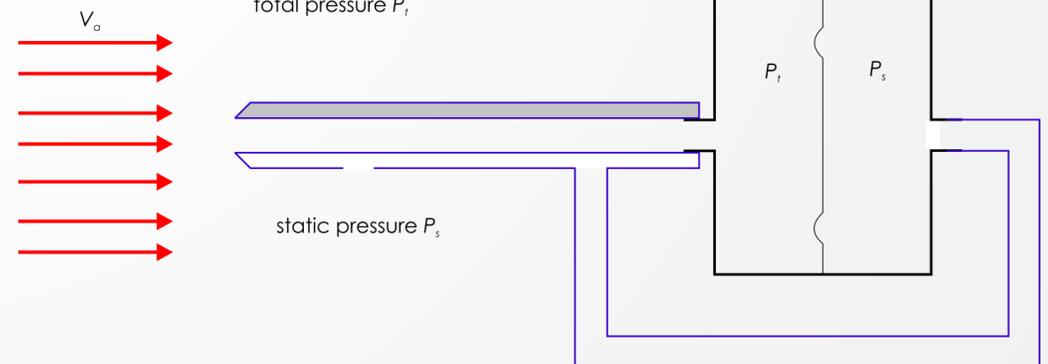
- ▶ Airspeed Measurement:

- ▶ From Bernoulli's equation:

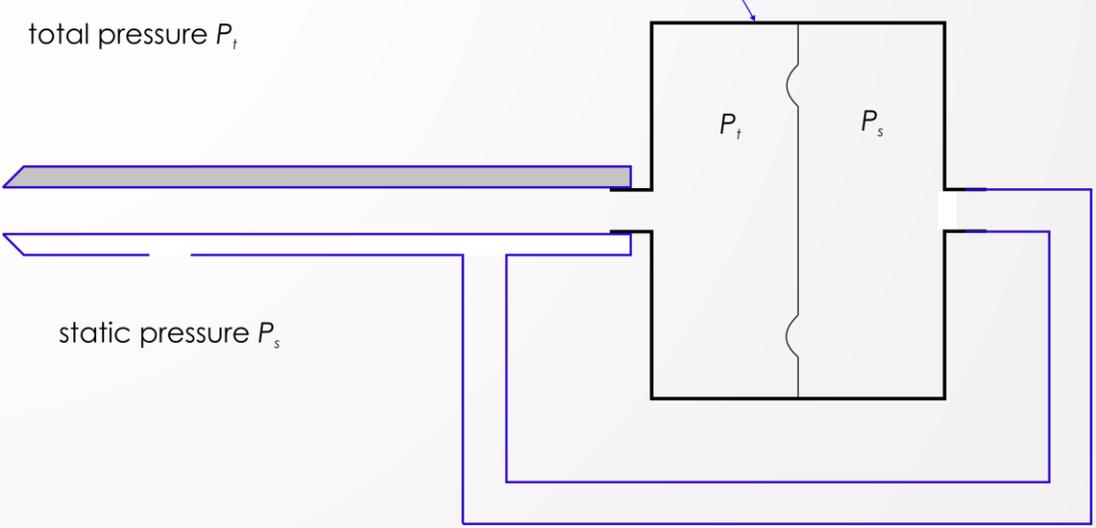
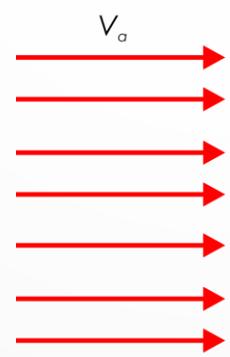
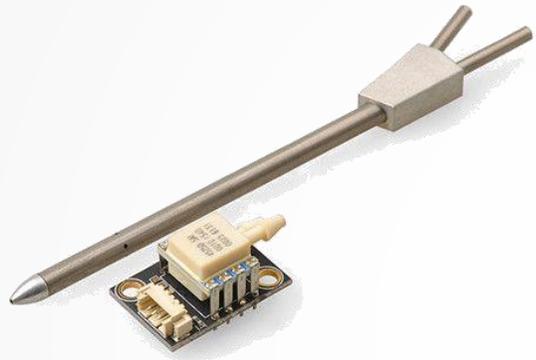
$$P_t = P_s + \frac{\rho V_a^2}{2} \Rightarrow \frac{\rho V_a^2}{2} = P_t - P_s$$

- ▶ Pitot-static pressure sensor measures dynamic pressure

$$y_{diffpres} = \frac{\rho V_a^2}{2} + \beta_{diffpres} + \eta_{diffpres}$$

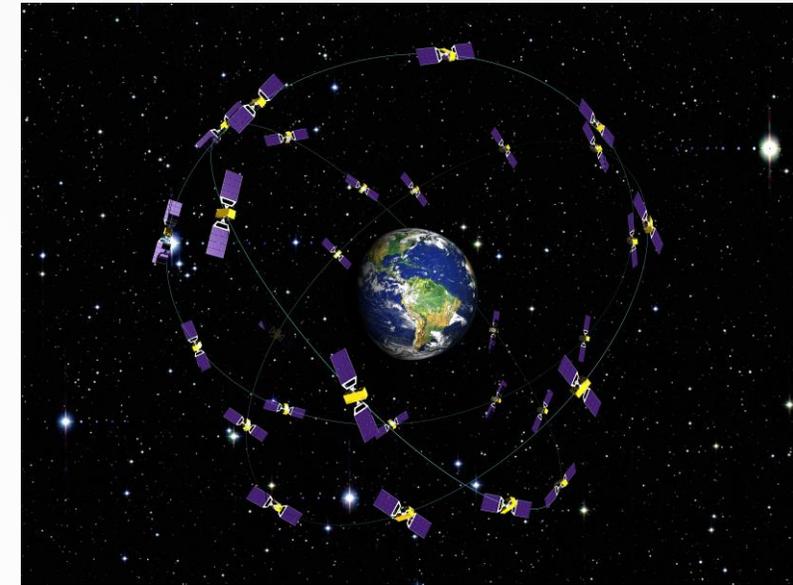


Pressure Measurements



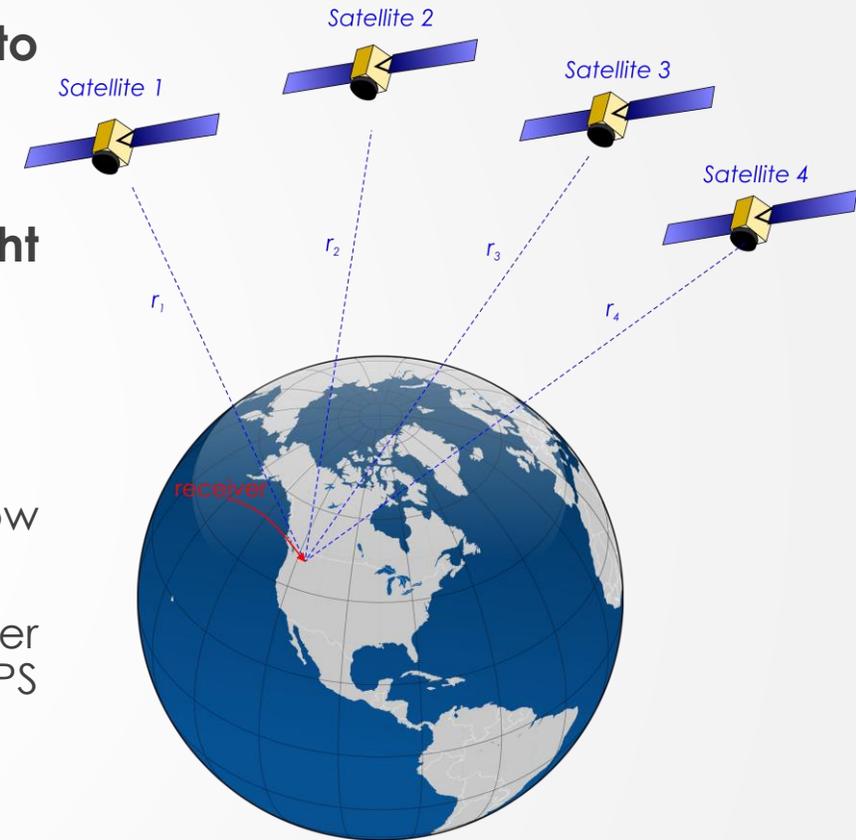
Global Positioning System

- ▶ 24 Satellites orbiting the Earth (*and some back-ups*).
- ▶ Altitude set at 20,180km
- ▶ Any point on Earth's surface can be seen by at least 4 satellites at all times.
- ▶ Time-of-Flight of radio signal from 4 satellites to receiver in 3 dimensions.
- ▶ 4 range measurements needed to account for clock offset error.
- ▶ 4 nonlinear equations in 4 unknown results:
 - ▶ Latitude
 - ▶ Longitude
 - ▶ Altitude
 - ▶ Receiver clock time offset

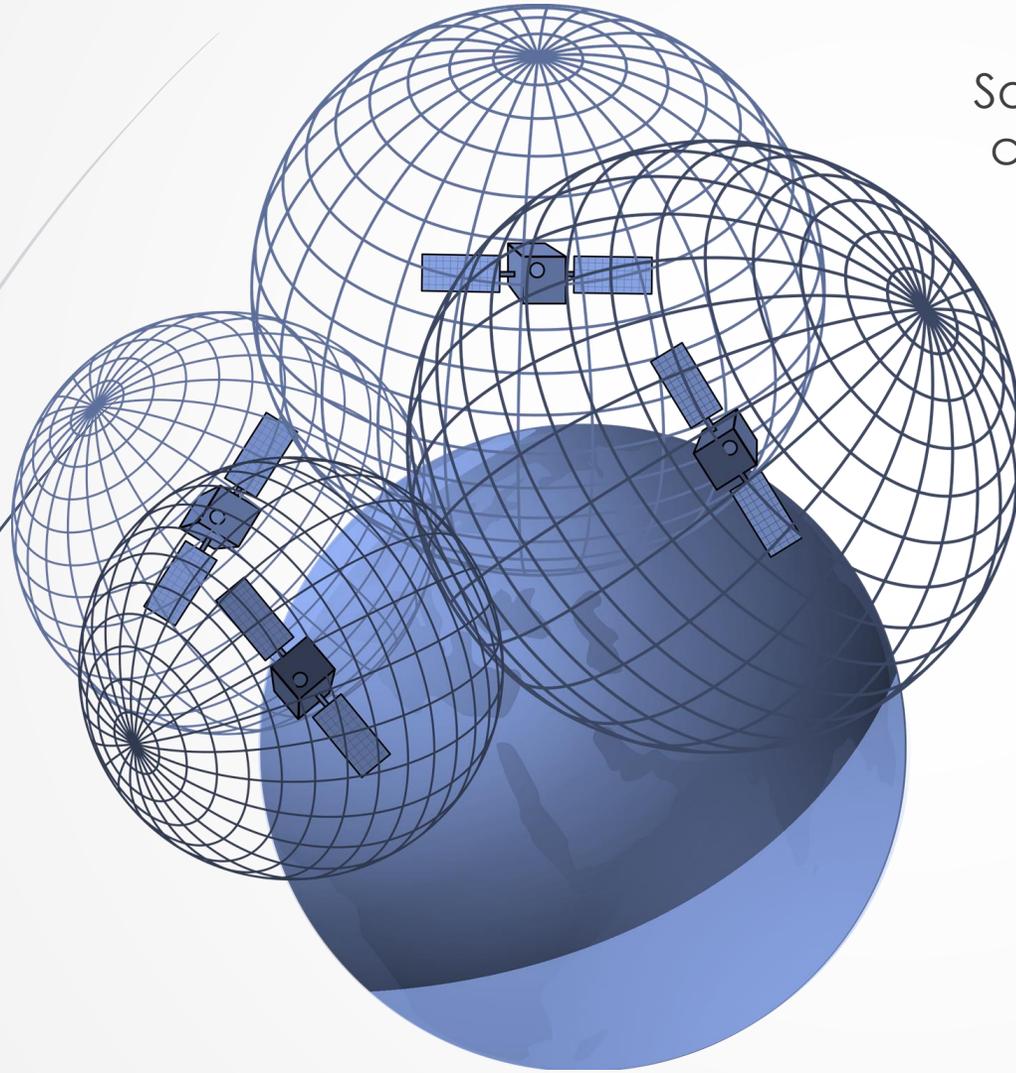


Global Positioning System

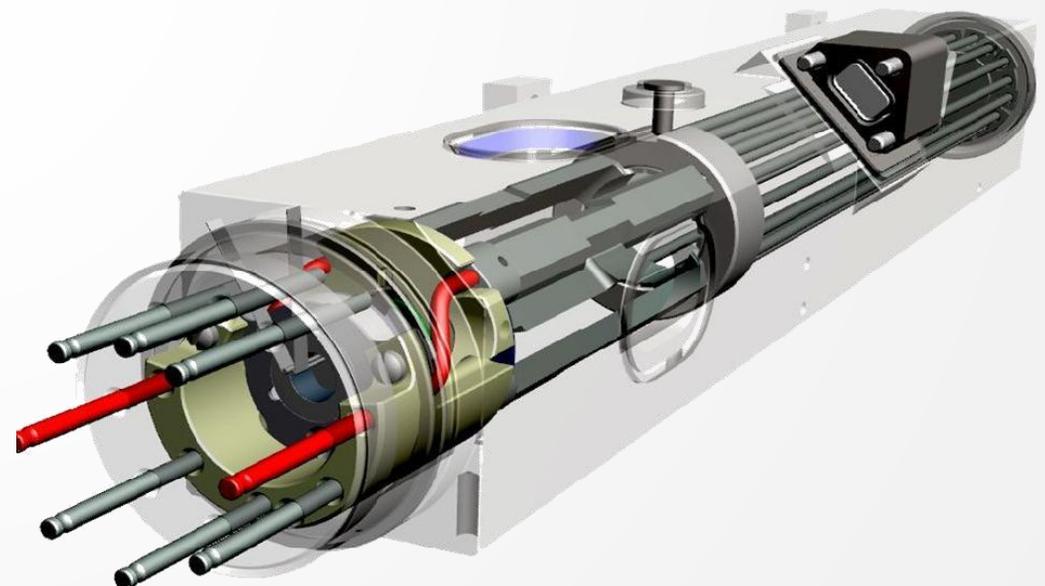
- ▶ **Time-of-Flight of the radio signal from satellite to receiver used to calculate pseudorange.**
 - ▶ Called pseudorange to distinguish it from true range.
- ▶ **Numerous sources of error in time-of-flight measurement:**
 - ▶ Ephemeris Data – errors in satellite location
 - ▶ Satellite clock – due to clock drift.
 - ▶ Ionosphere – upper atmosphere, free electrons slow transmission of the GPS signal.
 - ▶ Troposphere – lower atmosphere, weather (temperature and density) affect speed of light, GPS signal transmission.
 - ▶ Multipath Reception – signals not following direct path
 - ▶ Receiver measurement – limitations in accuracy of the receiver timing.
- ▶ **Small timing errors can result in large position deviations:**
 - ▶ 10ns timing error leads to 3m pseudorange error.



GPS Trilateration

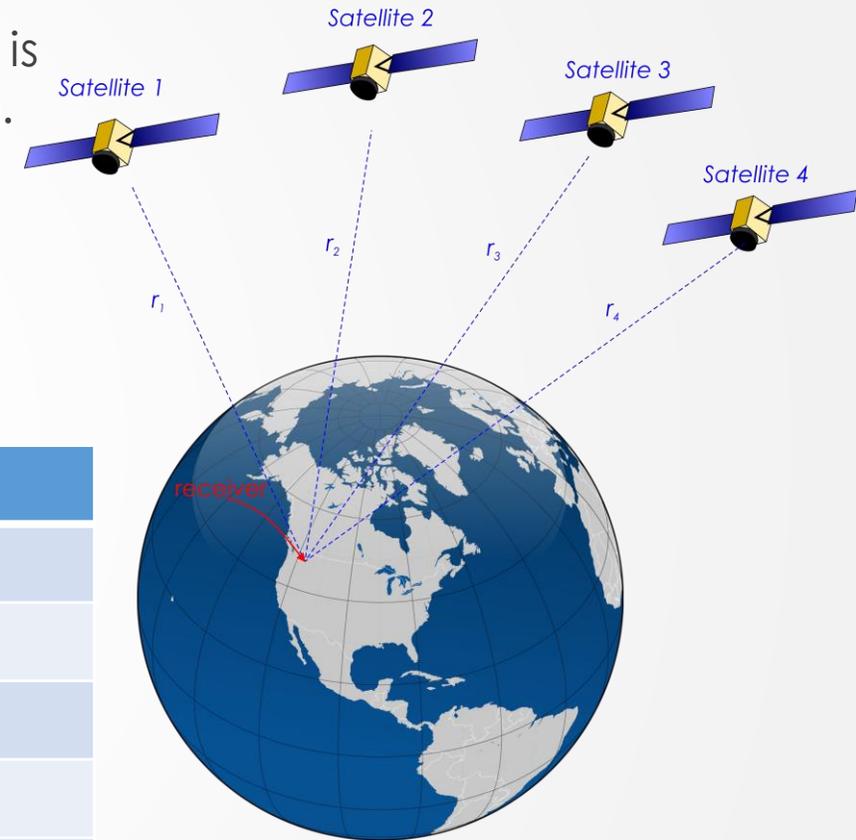


Some math and an atomic clock-based “stopwatch”



GPS Error Characterization

- ▶ Cumulative effect of GPS pseudorange errors is described by the **User-Equivalent Range Error (UERE)**.
- ▶ **UERE has two components:**
 - ▶ Bias
 - ▶ Random

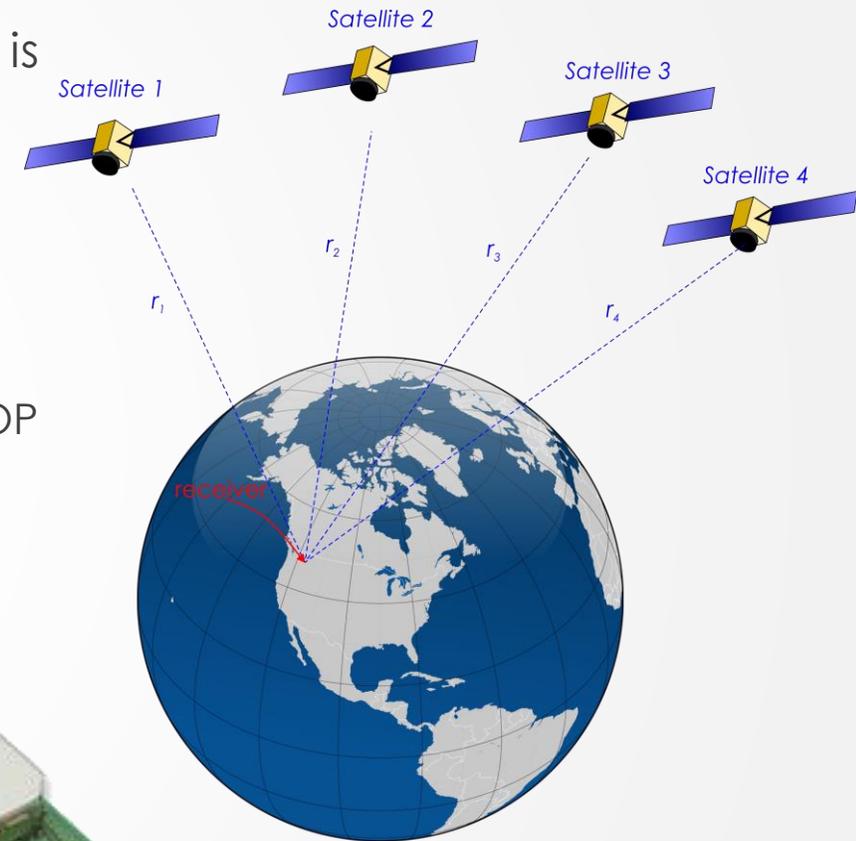


1σ , in m

Error source	Bias	Random	Total
Ephemeris data	2.1	0.0	2.1
Satellite clock	2.0	0.7	2.1
Ionosphere	4.0	0.5	4.0
Troposphere monitoring	0.5	0.5	0.7
Multipath	1.0	1.0	1.4
Receiver measurement	0.5	0.2	0.5
UERE, rms	5.1	1.4	5.3
Filtered UERE, rms	5.1	0.4	5.1

GPS Error Characterization

- ▶ Effect of satellite geometry on position calculation is expressed by dilution of precision (DOP).
 - ▶ Satellites close together leads to high DOP.
 - ▶ Satellites far apart leads to low **DOP**.
 - ▶ DOP varies with time.
 - ▶ Horizontal DOP (**HDOP**) is smaller than Vertical DOP (**VDOP**):
 - ▶ Nominal HDOP = 1.3
 - ▶ Nominal VDOP = 1.8



Total GPS Error

- ▶ Standard deviation of RMS error in the north-east plane:

$$E_{n-e,rms} = \text{HDOP} \times \text{UERE}_{rms} \Rightarrow$$
$$E_{n-e,rms} = (1.3)(5.1) = 6.6\text{m}$$

- ▶ Standard deviation of RMS altitude error:

$$E_{h,rms} = \text{VDOP} \times \text{UERE}_{rms} \Rightarrow$$
$$E_{h,rms} = (1.8)(5.1) = 9.2\text{m}$$

- ▶ As expected: an **ellipsoidal error model**.

Further categorization

- ▶ Let's categorize the sensors we overviewed.

Absolute		Rate
GPS Barometer Accelerometer Magnetometer		Airspeed sensor Gyroscope
Position		Orientation
GPS Airspeed Barometer		Accelerometer Gyroscope Magnetometer
Sensor	Measures	Predicts
Accelerometer	Extracts orientation and measures acceleration	Velocity

SenseSoar

Flight Tests:
Dynamics and Onboard Avionics Evaluation
May, 24th 2013

ETH

Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology Zurich



ICARUS

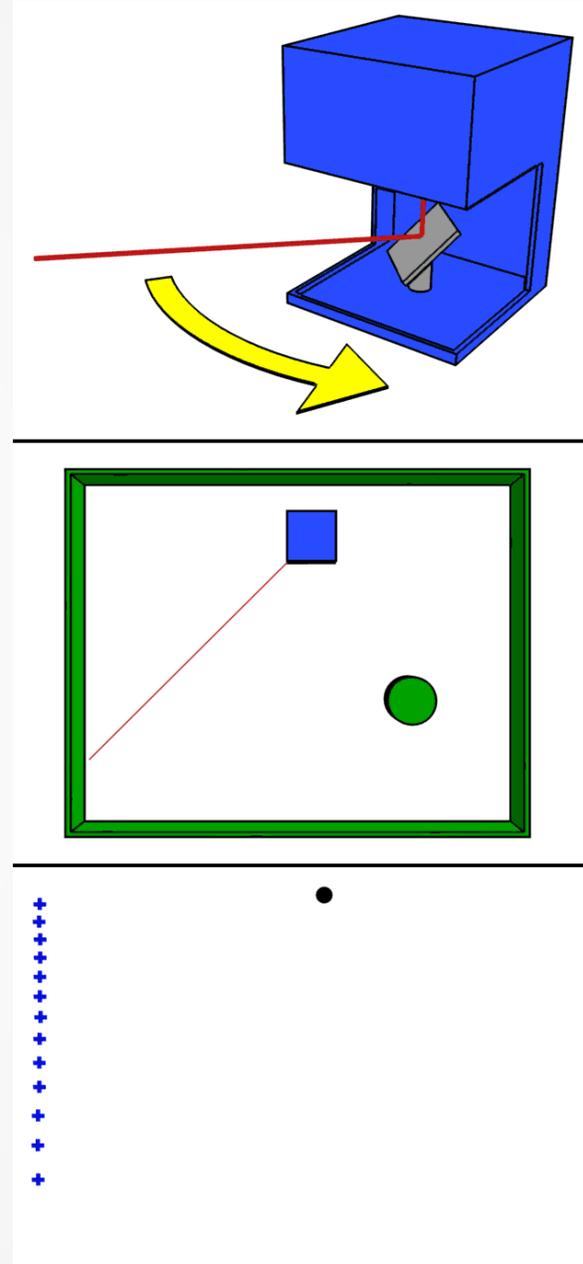
INTEGRATED COMPONENTS FOR ASSISTED RESCUE AND UNMANNED
SEARCH OPERATIONS



Autonomous Systems Lab

LiDAR

- ▶ Lidar (also written LIDAR, LiDAR or LADAR) is a surveying technology that measures distance by illuminating a target with a laser light.
- ▶ In general there are two kinds of lidar detection schemes: "incoherent" or direct energy detection (which is principally an amplitude measurement) and [coherent](#) detection (which is best for [Doppler](#), or phase sensitive measurements). Coherent systems generally use [optical heterodyne detection](#), which, being more sensitive than direct detection, allows them to operate at a much lower power but at the expense of more complex transceiver requirements.
- ▶ Main components of a LiDAR system:
 - ▶ Laser
 - ▶ Scanner and Optics
 - ▶ Photodetector and Receiver Electronics
 - ▶ Position and Navigation Systems



LiDAR



TEACH AND REPEAT IN DYNAMIC ENVIRONMENTS

Philipp Krüsi
Bastian Bücheler
François Pomerleau
Paul Furgale
Roland Siegwart

March 20, 2013



Video from ETH Zurich – Autonomous Systems Lab.

SLAM: A micro-introduction

- ▶ How can a body navigate in a previously unknown environment while constantly building and updating a map of its workspace using on board sensors only?
- ▶ When is SLAM necessary?
 - ▶ When a robot must be truly autonomous (no direct/indirect human feedback).
 - ▶ When there is no prior/insufficient knowledge about the environment.
 - ▶ When we cannot place beacons and cannot use external positioning systems (e.g. GPS).
 - ▶ When the robot needs to know where it is.

This micro-introduction is largely based on the mini-introduction provided by Dr. Margarita Chli - http://www.roboticsschool.ethz.ch/airobots/programme/presentations/SLAM_printable.pdf

SLAM: A micro-introduction

- ▶ An unbiased map is necessary for localizing the robot
 - ▶ Pure localization with a known map
 - ▶ SLAM: no a priori knowledge of the robot's workspace
- ▶ An accurate position estimate is necessary for building a map of the environment
 - ▶ Mapping with known robot poses
 - ▶ SLAM: the robot poses have to be estimated along the way
- ▶ The problem of localization is the invert of the problem of mapping, but have to be solved simultaneously by the robot.
 - ▶ A great challenge.



SLAM: A micro-introduction

- ▶ Challenge: track the motion of a robot (based on a sensor such as a camera) while it is moving?

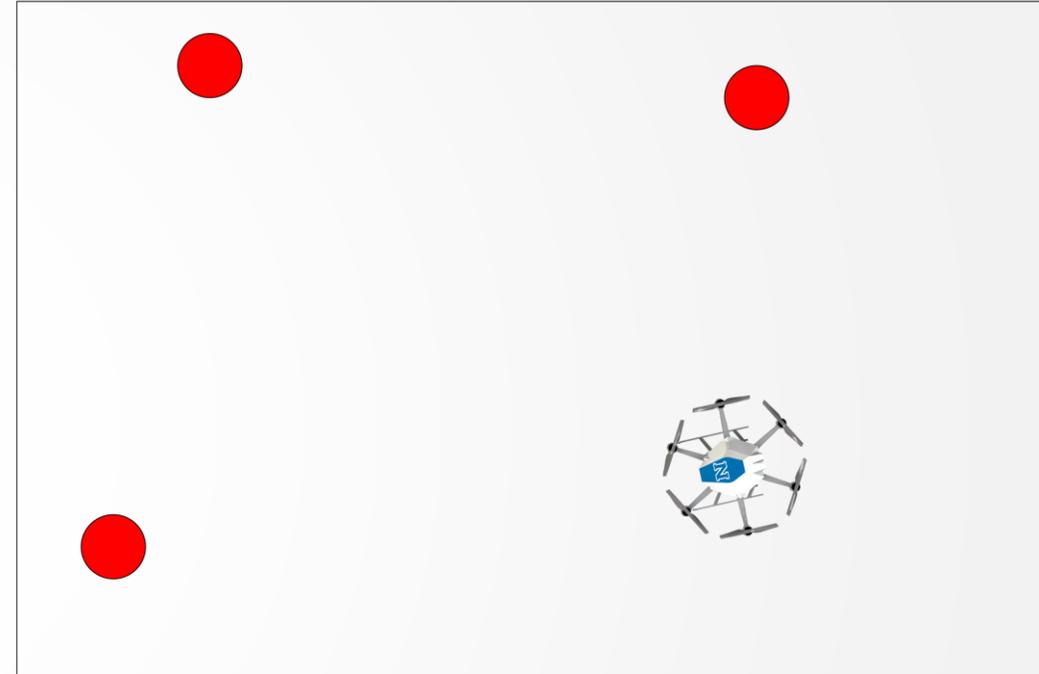
Obstacle avoidance
is key to navigate UAVs indoors
without line of sight

Video from Skybotix AG,
ETH Zurich – Autonomous Systems Lab

- ▶ Pick natural scene features to serve as landmarks (the case in most modern SLAM systems).
- ▶ Range sensing (LiDAR/Sonar/Radar/Time-of-Flight cameras): points, line segments, 3D planes, corners.
- ▶ Vision: point features, lines, textures surfaces.
- ▶ Key: features must be distinctive & recognizable from different viewpoints.

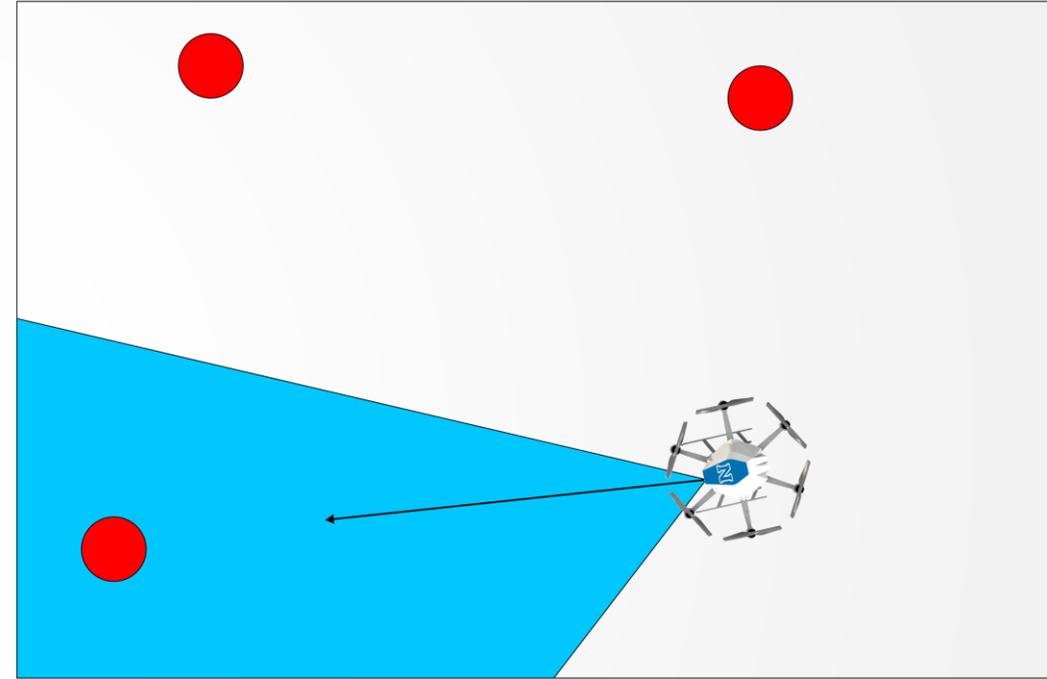
SLAM: A micro-introduction

- ▶ Use internal representations for:
 - ▶ The positions of landmarks (: map)
 - ▶ The camera parameters
- ▶ Assumption; Robot's uncertainty at starting position is zero



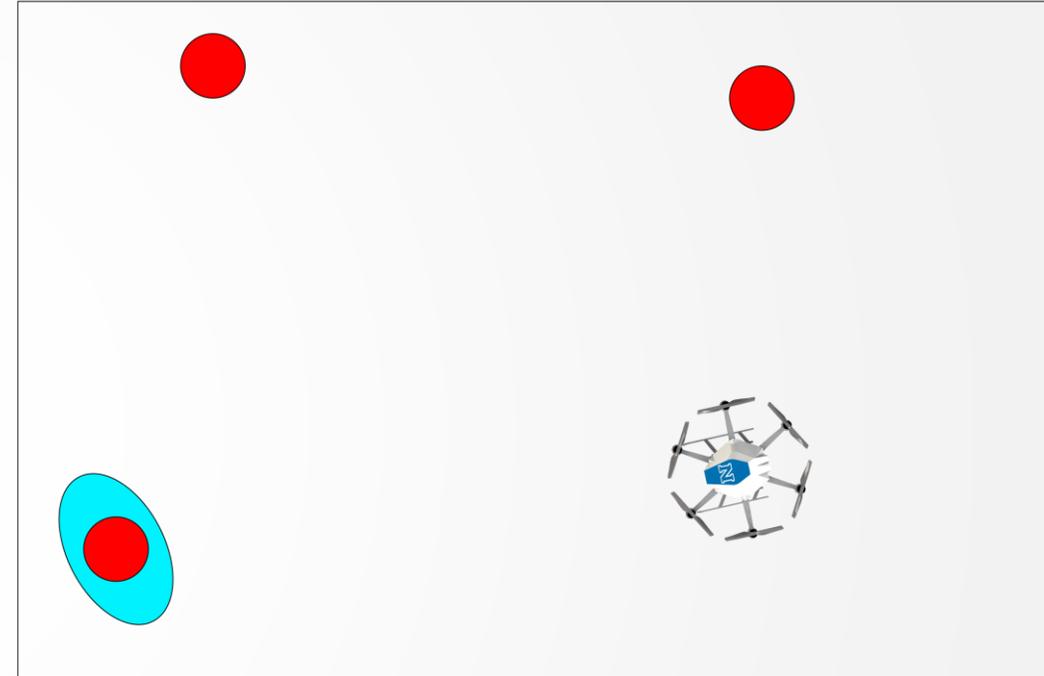
SLAM: A micro-introduction

- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations



SLAM: A micro-introduction

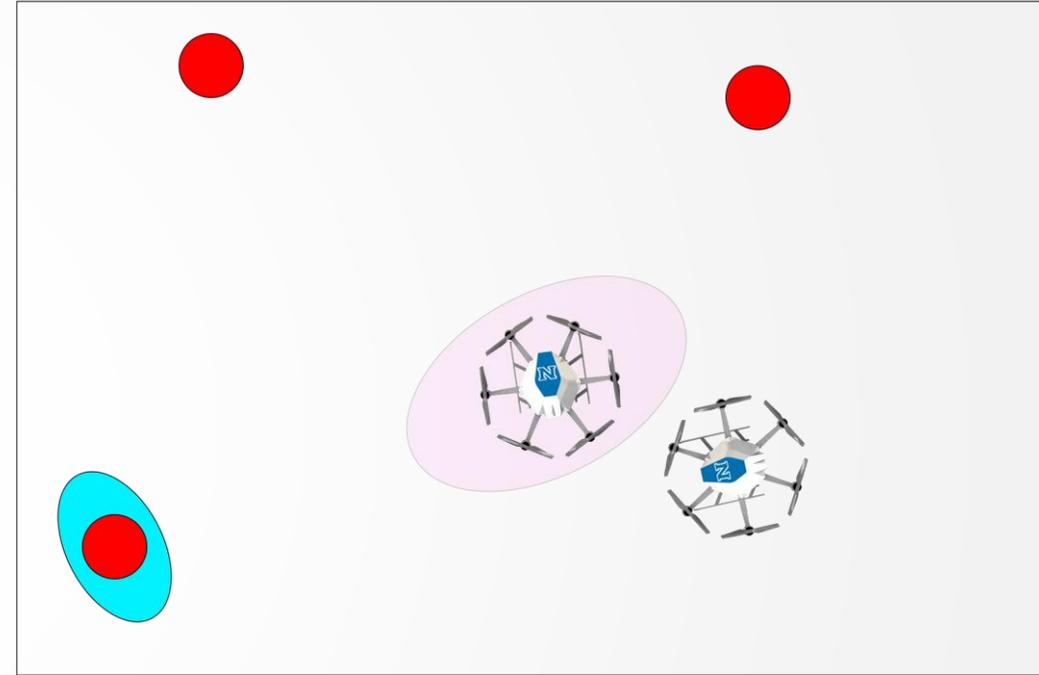
- ▶ The robot observes a feature which is mapped with an uncertainty related to the **measurement model**.



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

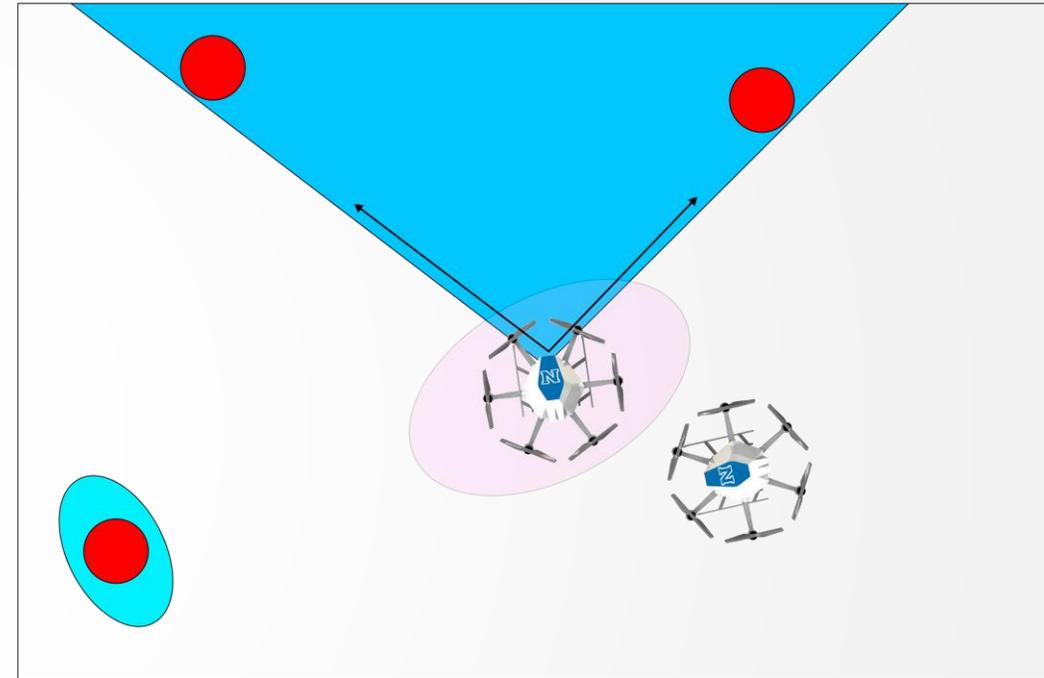
- ▶ As the robot moves, its pose uncertainty increases, obeying the robot's motion model.



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

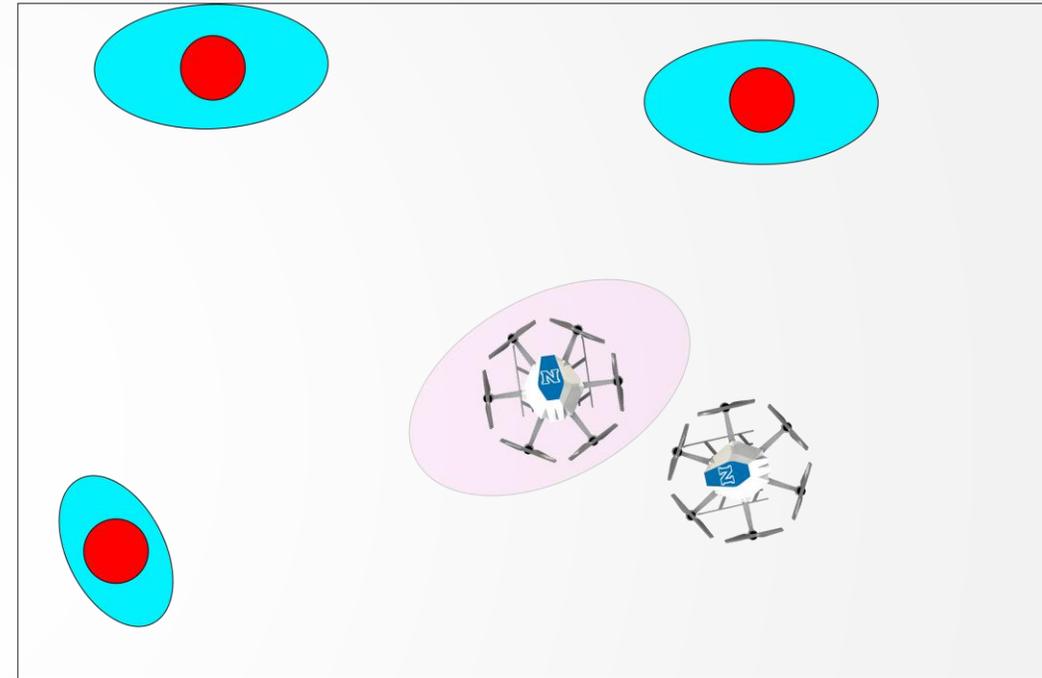
- ▶ Robot observes two new features.



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

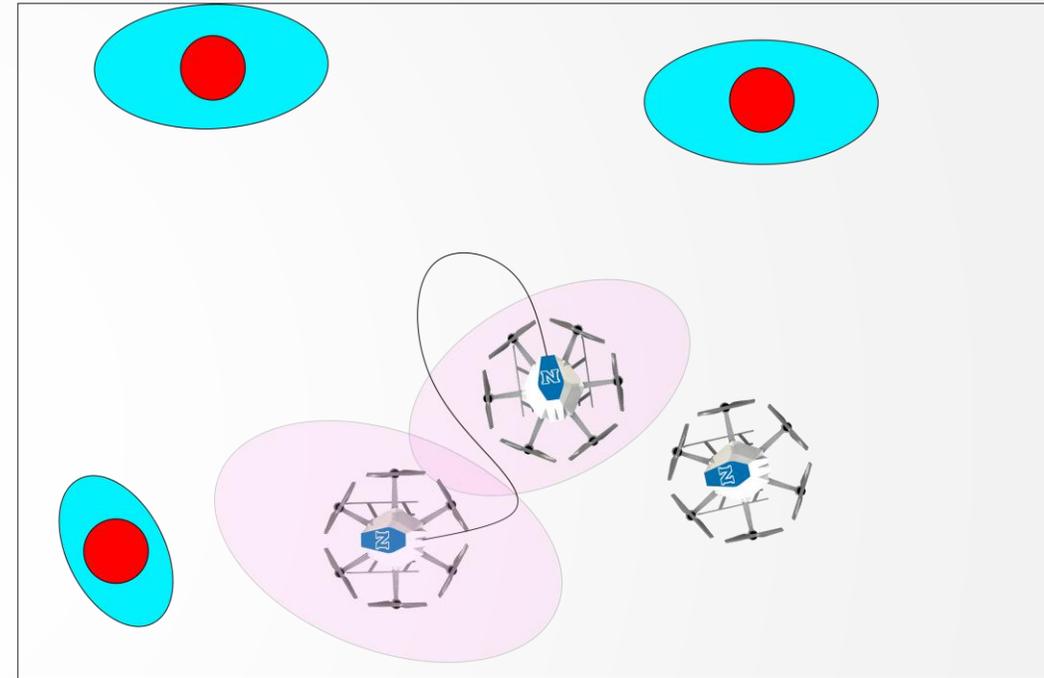
- ▶ Their position uncertainty results from the **combination** of the measurement error with the robot pose uncertainty.
- ▶ Map becomes **correlated** with the robot pose estimate



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

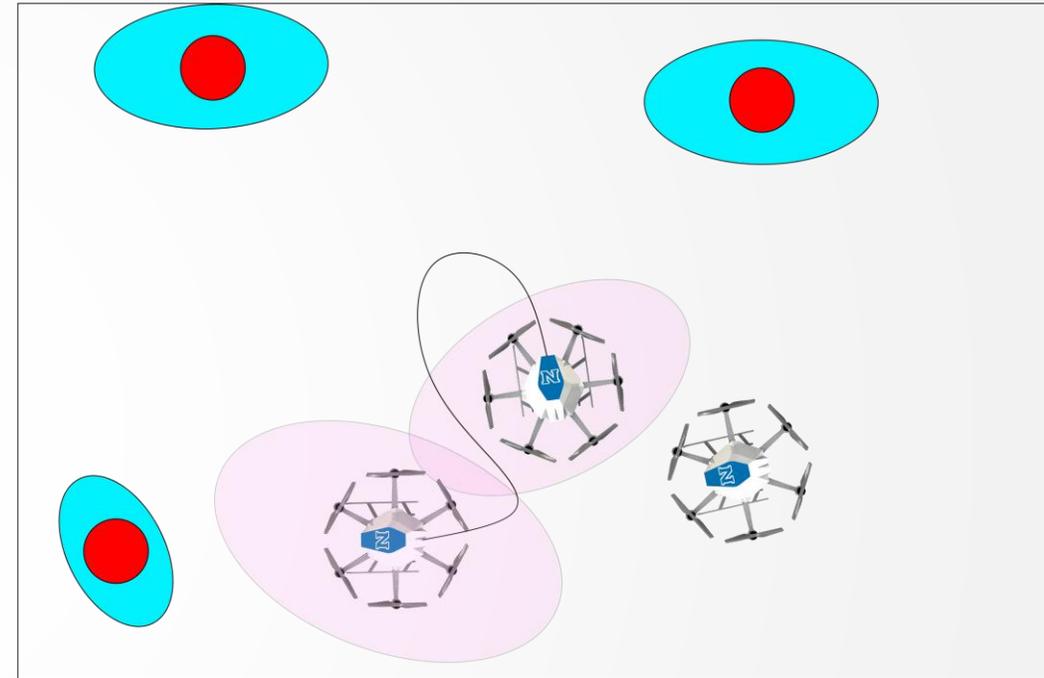
- ▶ Robot moves again and its uncertainty increases (motion model)



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

- ▶ Robot moves again and its uncertainty increases (motion model)

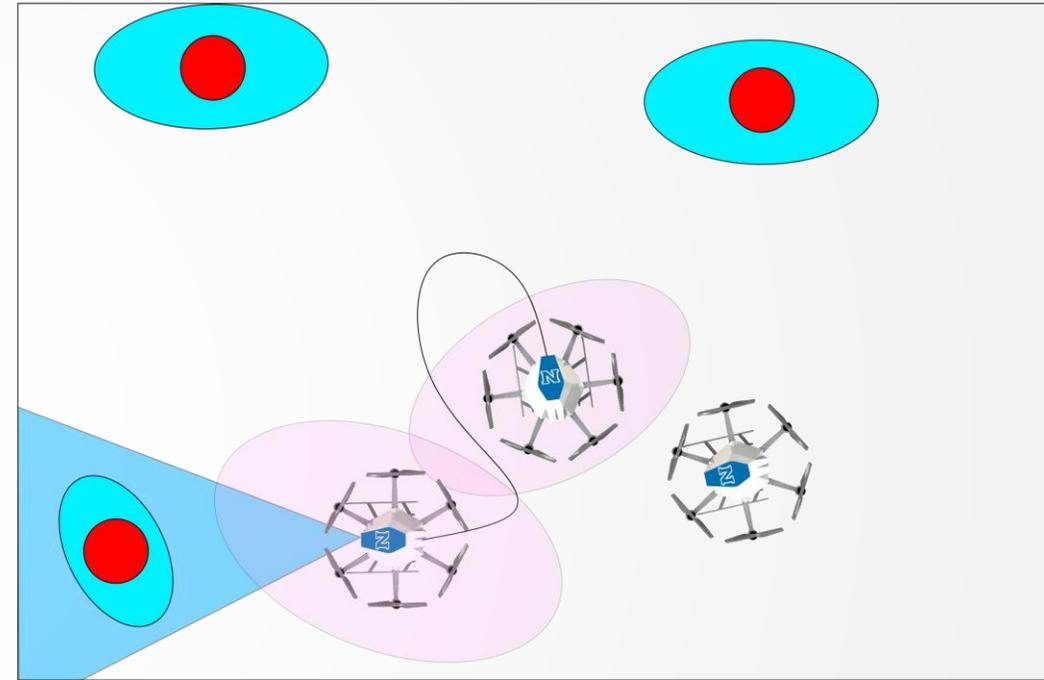


- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

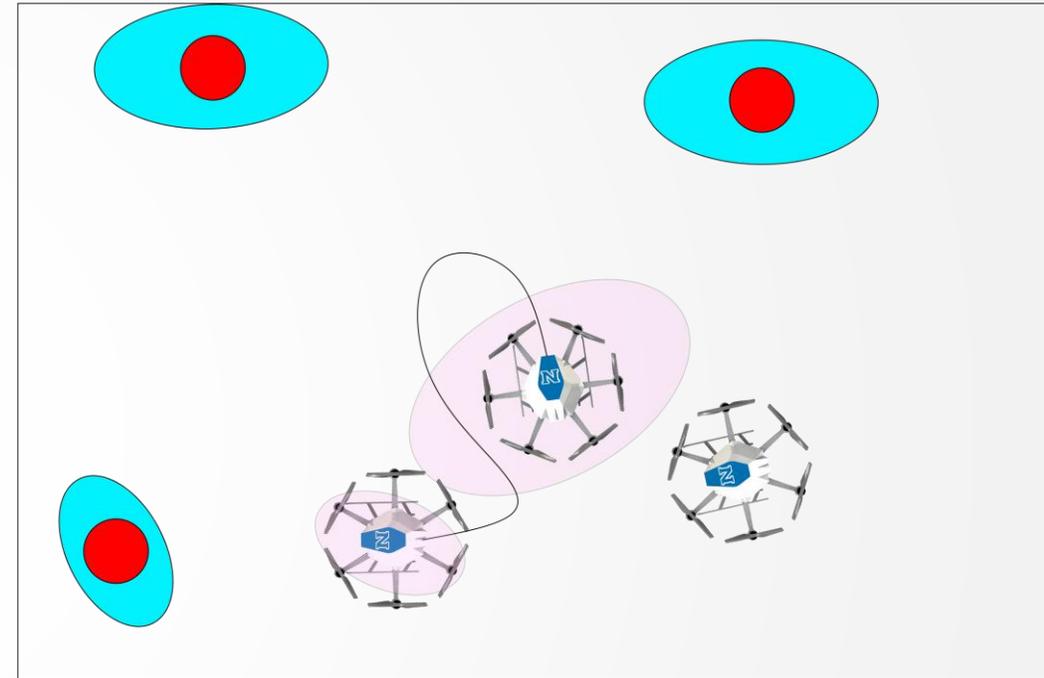
- ▶ Robot re-observes an old feature
 - ▶ Loop closure detection

- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations



SLAM: A micro-introduction

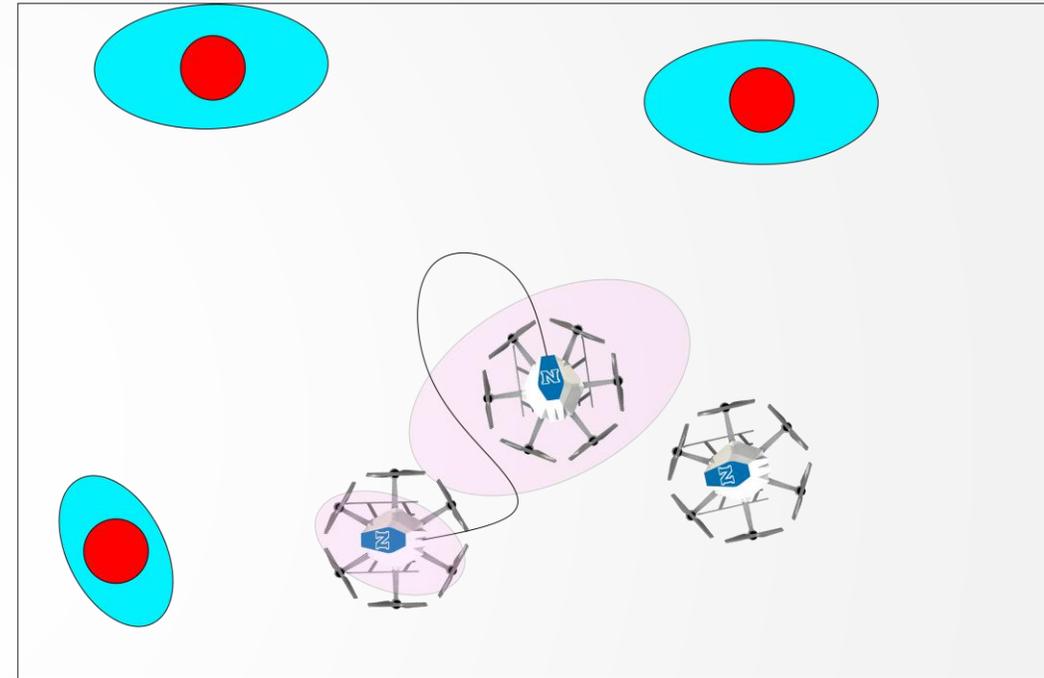
- ▶ Robot updates its position: the resulting pose estimate becomes correlated with the feature location estimates.
- ▶ Robot's uncertainty shrinks and so does the uncertainty in the rest of the map.



- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

- ▶ Robot updates its position: the resulting pose estimate becomes correlated with the feature location estimates.
- ▶ Robot's uncertainty shrinks and so does the uncertainty in the rest of the map.



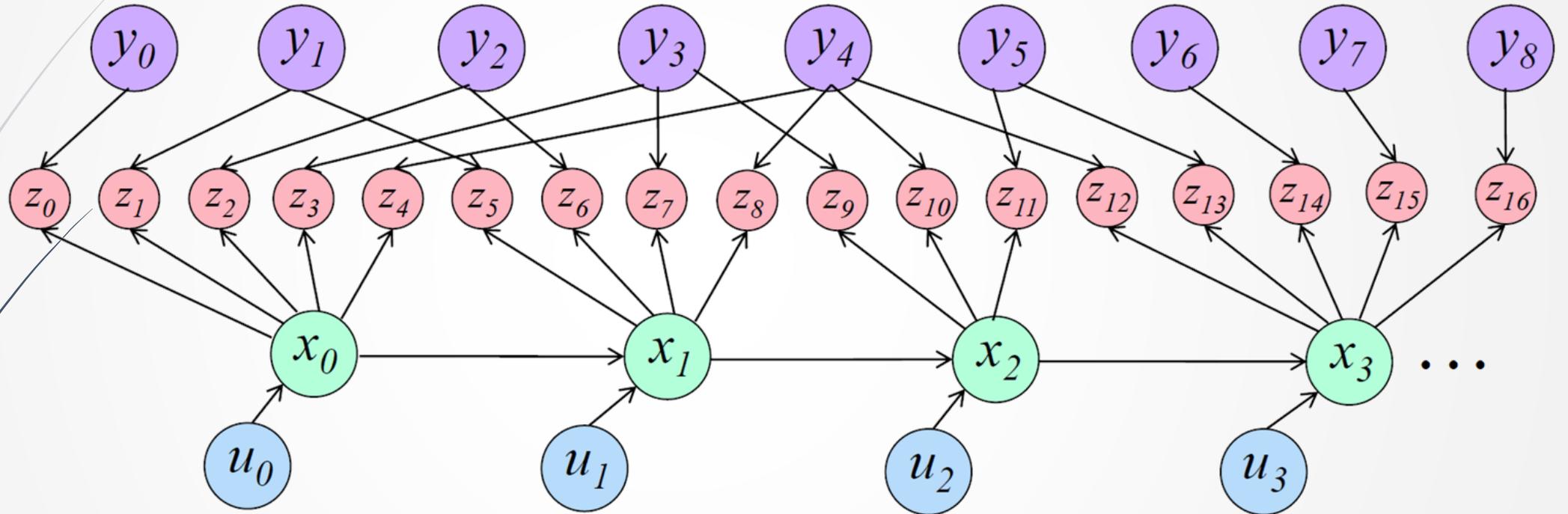
- ▶ On every frame:
 - ▶ **Predict** how the robot has moved
 - ▶ **Measure**
 - ▶ **Update** the internal representations

SLAM: A micro-introduction

- ▶ SLAM Probabilistic formulation
- ▶ Robot **pose** at time t : x_t
 - ▶ Robot **path** up to this time: $\{x_0, x_1, \dots, x_t\}$
- ▶ Robot **motion** between $t-1$ and t : u_t (control inputs/proprioceptive sensor readings)
 - ▶ Sequence of relative motions $\{u_0, u_1, \dots, u_t\}$
- ▶ The **true map** of the environment: $\{y_0, y_1, \dots, y_N\}$
- ▶ At each time t the robot makes measurements z_i
 - ▶ Set of all **measurements** (observations): $\{z_0, z_1, \dots, z_k\}$
- ▶ The Full SLAM problem
 - ▶ Estimate the posterior: $p(x_{0:t}, y_{0:n} / z_{0:k}, u_{0:t})$
- ▶ The Online SLAM problem
 - ▶ Estimate the posterior: $p(x_t, y_{0:n} / z_{0:k}, u_{0:t})$

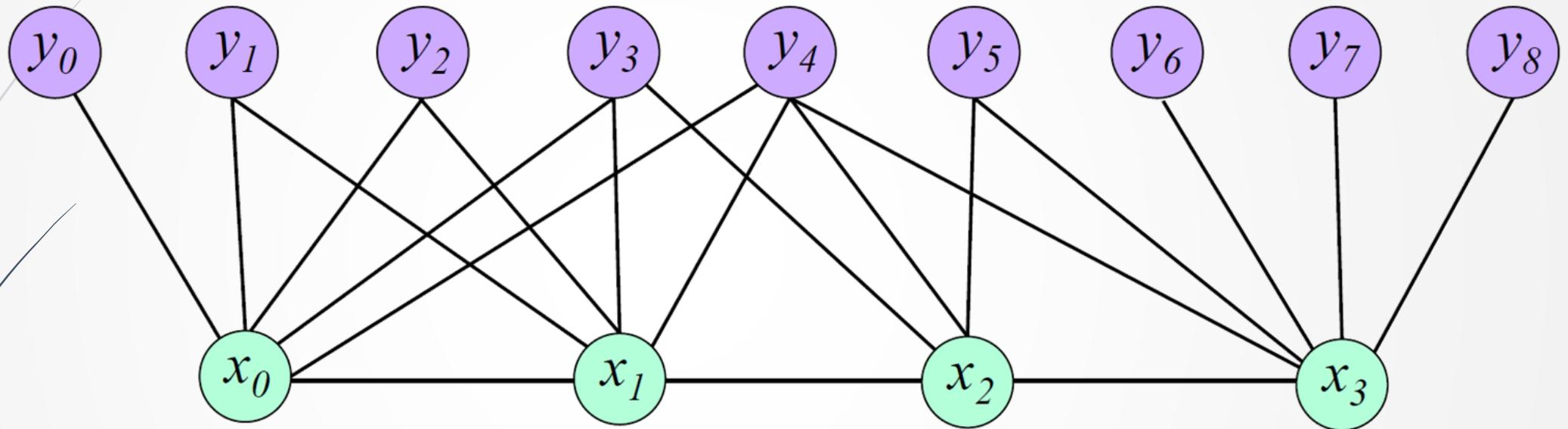
SLAM: A micro-introduction

- Slam graphical representation



SLAM: A micro-introduction

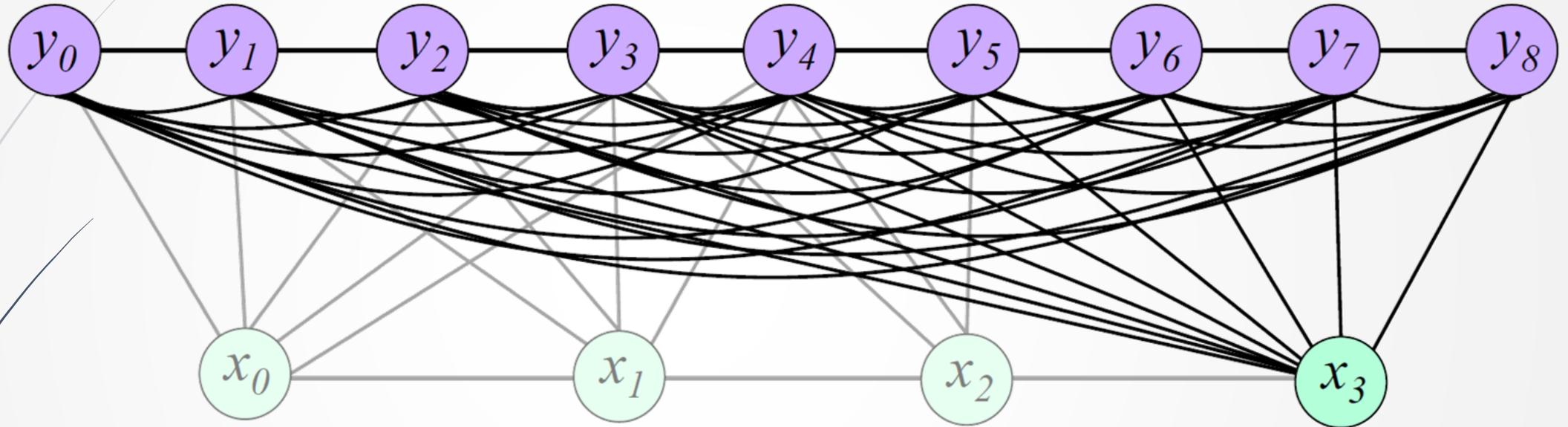
- SLAM Approaches: Full graph optimization (bundle adjustment)



- Eliminate observations & control-input nodes and solve for the constraints between poses and landmarks.
- Globally consistent solution, but infeasible for large-scale SLAM.
- If real-time is a requirement :: we need to **sparsify** this graph.

SLAM: A micro-introduction

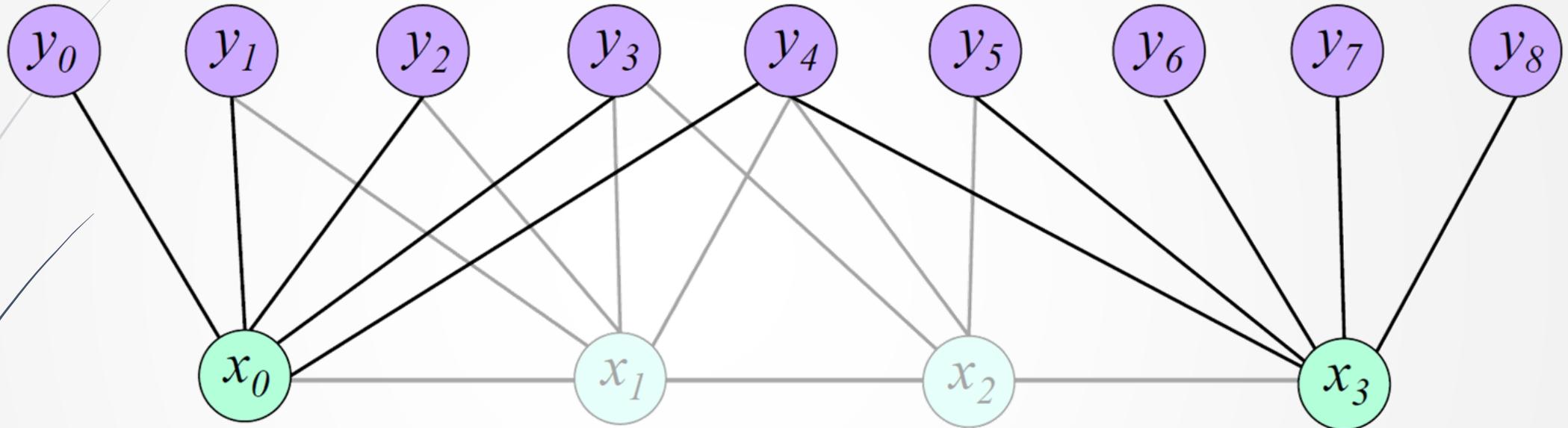
- SLAM Approaches: Filtering



- Eliminate all past poses: “summarize” all experience with respect to the last pose, using a **state vector** and the associated **covariance matrix**.

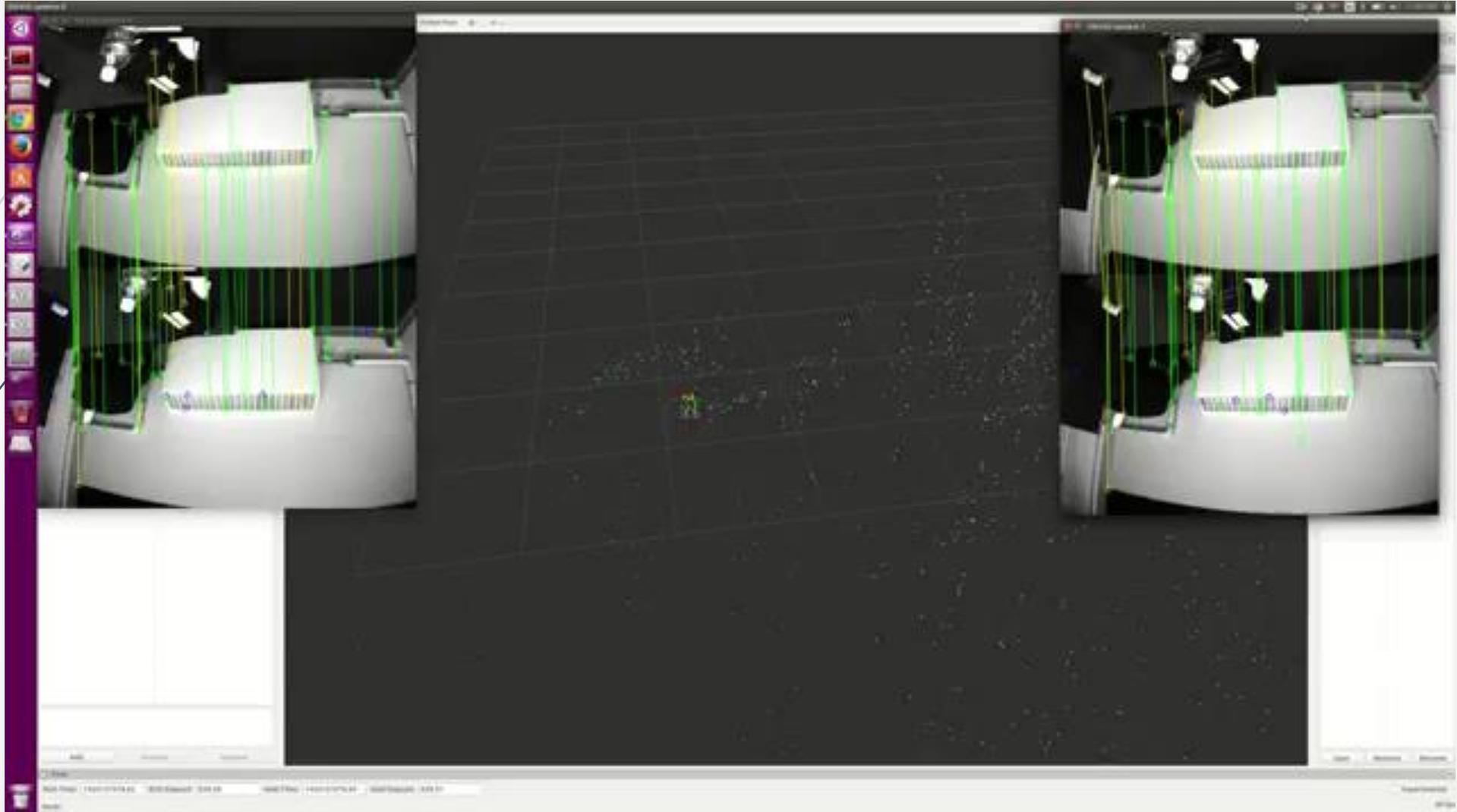
SLAM: A micro-introduction

- SLAM Approaches: Key-frames



- Retain the most “representative” poses (key-frames) and their dependency links – optimize the resulting graph.

SLAM: A micro-introduction



https://github.com/ethz-asl/okvis_ros

Recent Research Results

AtlantikSolar

Test Flight Day #24
(May 18th 2015)

Aircraft: AtlantikSolar UAV Prototype (AS-P)
Location: Rothenthurm, Switzerland
Flights performed: 3

Mission: High-fidelity 3-D mapping of area using pre-computed paths with guaranteed coverage



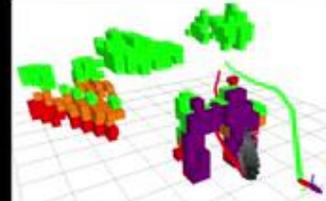
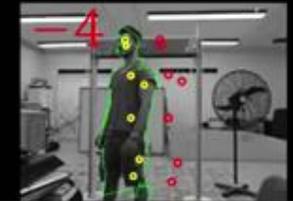
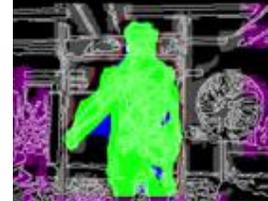
ETH

Eidgenössische Technische Hochschule Zürich
Swiss Federal Institute of Technology, Zurich



Autonomous Robotic Aerial Tracking, Avoidance, and Seeking of a Mobile Human Subject

Christos Papachristos, Dimos Tzoumanikas, Kostas Alexis, and Anthony Tzes



Not only on Flying Robots....

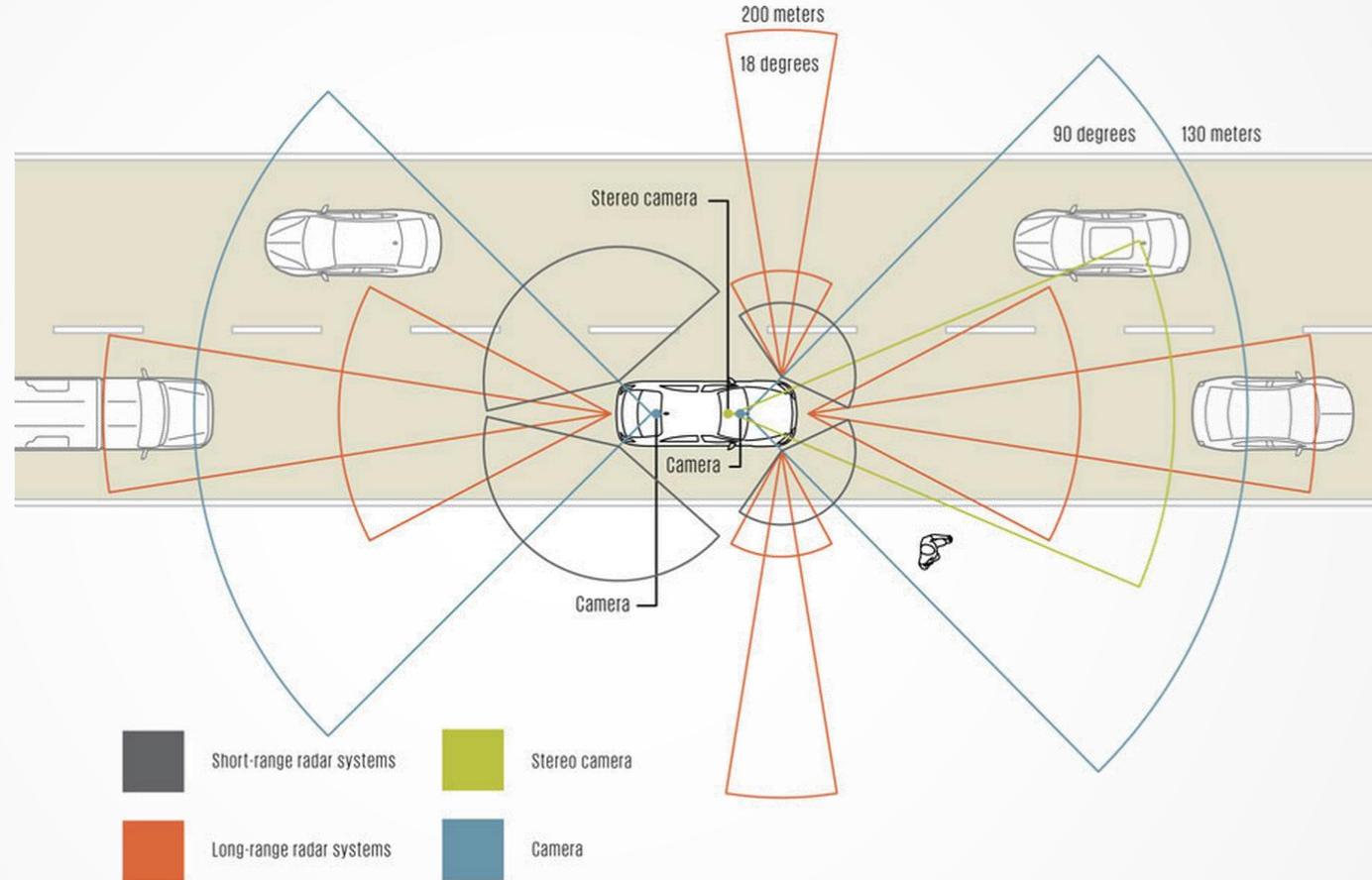


Illustration: John MacNeill

Sensors of different capabilities cover 360 degrees, with overlapping fields of view.

https://forums.teslamotors.com/en_HK/forum/forums/model-s-will-be-able-autosteer-will-require-more-sensors-semiautonomous-driving



Find out more

- <http://www.kostasalexis.com/inertial-sensors.html>
- <http://px4.io/>
- <http://www.vectornav.com/support/library/imu-and-ins>
- <http://www.sensorwiki.org/>
- <http://margaritachli.com/research.html>

- <https://www.doc.ic.ac.uk/~ajd/Robotics/RoboticsResources/SLAMTutorial1.pdf>
- <https://www.doc.ic.ac.uk/~ajd/Robotics/RoboticsResources/SLAMTutorial2.pdf>

- <http://www.kostasalexis.com/literature-and-links.html>

A black and white photograph of a drone flying in the foreground. The drone is a quadcopter with a white protective cover over its camera. In the background, there is a construction site with several large cranes and a building under construction. The scene is slightly blurred, suggesting motion or a shallow depth of field.

Thank you!

Please ask your question!