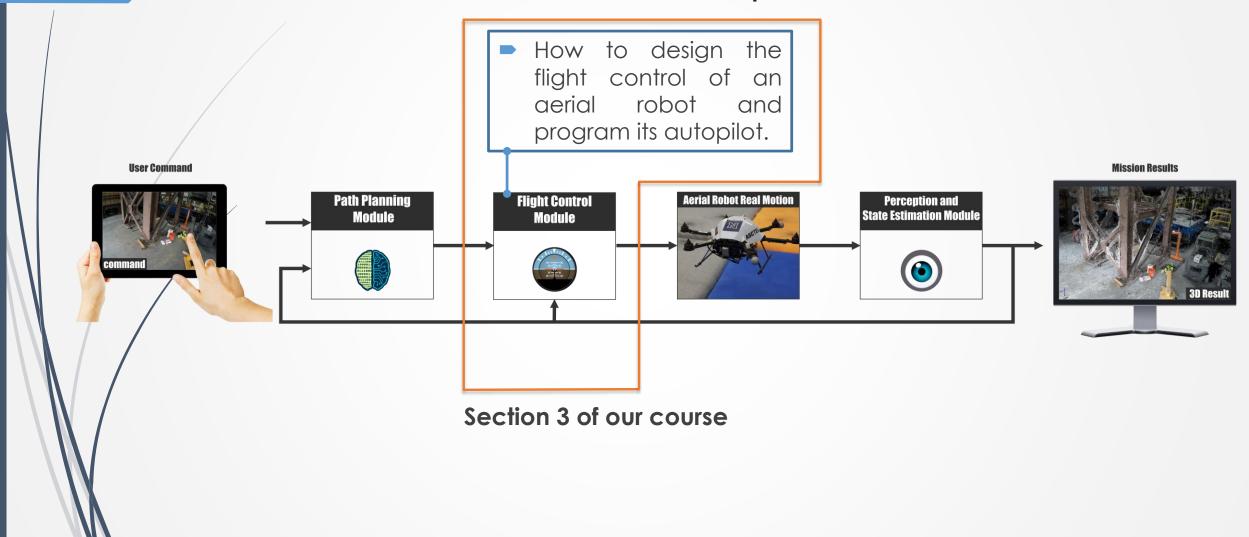


The Aerial Robot Loop



What is it all about?

Control theory is an interdisciplinary branch of engineering and mathematics that deals with the behavior of dynamical systems with inputs, and how their behavior is modified by feedback.



What is it all about?

- Control theory is an interdisciplinary branch of engineering and mathematics that deals with the behavior of dynamical systems with inputs, and how their behavior is modified by feedback.
- To do that in a systematic way, we should develop a **model-based** approach on control synthesis.



MAV Dynamics

To append the forces and moments we need to combine their formulation with

$$\begin{bmatrix} \dot{p}_n \\ \dot{p}_e \\ \dot{p}_d \end{bmatrix} = \mathcal{R}_b^v \begin{bmatrix} u \\ v \\ w \end{bmatrix}, \ \mathcal{R}_b^v = \begin{bmatrix} c_{\theta}c_{\psi} & s_{\phi}s_{\theta}c_{\psi} - c_{\phi}s_{\psi} & c_{\phi}s_{\theta}c_{\psi} + s_{\phi}s_{\psi} \\ c_{\theta}s_{\psi} & s_{\phi}s_{\theta}s_{\psi} + c_{\phi}c_{\psi} & c_{\phi}s_{\theta}s_{\psi} - s_{\phi}c_{\psi} \\ -s_{\theta} & s_{\phi}c_{\theta} & c_{\phi}c_{\theta} \end{bmatrix}$$

$$\begin{bmatrix} \dot{u} \\ \dot{v} \\ \dot{w} \end{bmatrix} = \begin{bmatrix} rv - qw \\ pw - ru \\ qu - pv \end{bmatrix} + \frac{1}{m} \begin{bmatrix} f_x \\ f_y \\ f_z \end{bmatrix}$$

$$\begin{bmatrix} \dot{\phi} \\ \dot{\theta} \\ \dot{\psi} \end{bmatrix} = \begin{bmatrix} 1 & \sin \phi \tan \theta & \cos \phi \tan \theta \\ 0 & \cos \phi & -\sin \phi \\ 0 & \sin \phi \sec \theta & \cos \phi \sec \theta \end{bmatrix} \begin{bmatrix} p \\ q \\ r \end{bmatrix}$$

$$\begin{bmatrix} \dot{p} \\ \dot{q} \\ \dot{r} \end{bmatrix} = \begin{bmatrix} \frac{J_y - J_z}{J_x} qr \\ \frac{J_z - J_x}{J_y} pr \\ \frac{J_x}{J_z} \end{bmatrix} \begin{bmatrix} p \\ q \\ r \end{bmatrix} + \begin{bmatrix} \frac{1}{J_x} M_x \\ \frac{1}{J_y} M_y \\ \frac{1}{J_z} M_z \end{bmatrix}$$

MAV Dynamics

MAV forces in the body frame:

$$\mathbf{f}_b = \begin{bmatrix} f_x \\ f_y \\ f_z \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \sum_{i=1}^6 T_i \end{bmatrix} - \mathcal{R}_v^b \begin{bmatrix} 0 \\ 0 \\ mg \end{bmatrix}$$

Moments in the body frame:

$$\mathbf{m}_{b} = \begin{bmatrix} M_{x} \\ M_{y} \\ M_{z} \end{bmatrix} = \begin{bmatrix} ls_{30} & l & ls_{30} & -ls_{30} & -l & ls_{30} \\ -lc_{60} & 0 & lc_{60} & lc_{60} & 0 & -lc_{60} \\ -k_{m} & k_{m} & -k_{m} & k_{m} & -k_{m} & k_{m} \end{bmatrix}$$

MAV Dynamics

MAV forces in the body frame:

$$\mathbf{f}_{b} = \begin{bmatrix} f_{x} \\ f_{y} \\ f_{z} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ \sum_{i=1}^{6} T_{i} \end{bmatrix} - \mathcal{R}_{v}^{b} \begin{bmatrix} 0 \\ 0 \\ mg \end{bmatrix}$$

Moments in the body frame:

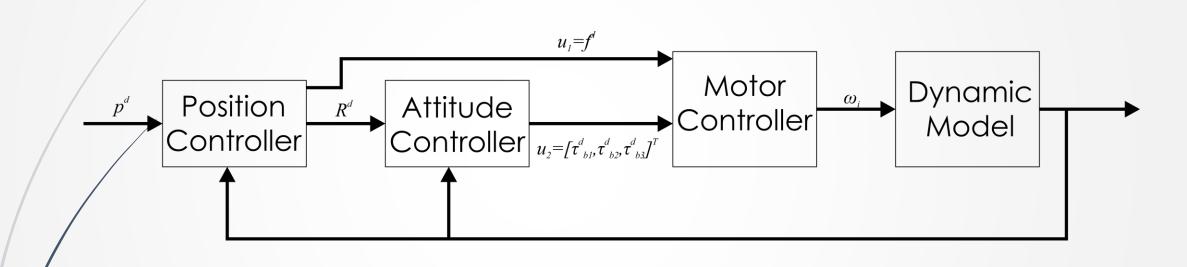
$$\mathbf{m}_{b} = \begin{bmatrix} M_{x} \\ M_{y} \\ M_{z} \end{bmatrix} = \begin{bmatrix} ls_{30} & l & ls_{30} & -ls_{30} & -l & ls_{30} \\ -lc_{60} & 0 & lc_{60} & lc_{60} & 0 & -lc_{60} \\ -k_{m} & k_{m} & -k_{m} & k_{m} & -k_{m} & k_{m} \end{bmatrix}$$

Bx

 30^{o}

60°

Control System Block Diagram



Simplified loop

Fast Nonlinear Model Predictive Control for Multicopter Attitude Tracking on SO(3)

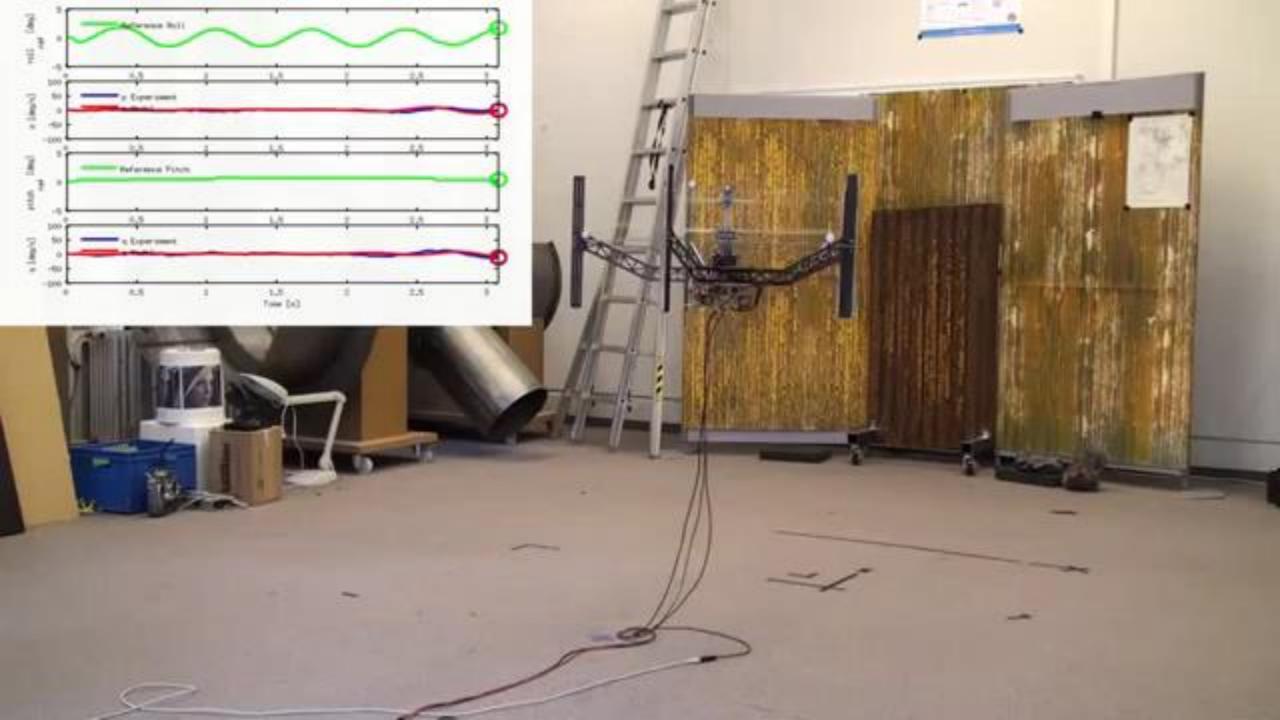
Mina Kamel, Kostas Alexis, Markus Achtelik and Roland Siegwart



Position tracking without one propeller







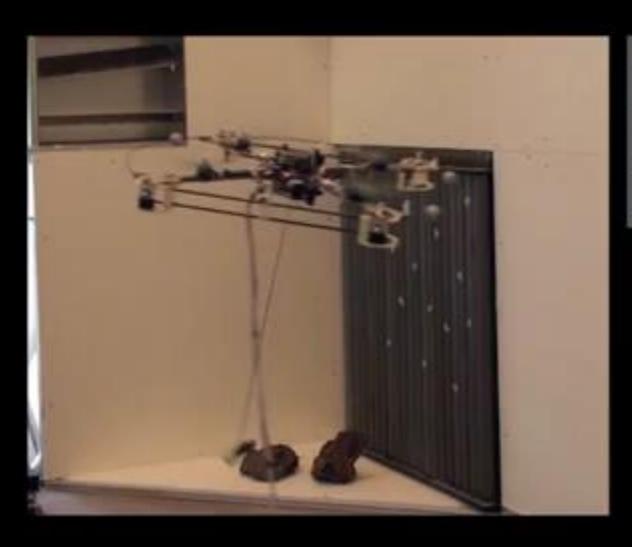


Test Flight Days #9
 (May 5th & 6th 2014)

Aircraft: AtlantikSolar UAV Prototype Location: Tuggen, Switzerland Flights performed: 5 Tests: Autopilot Waypoint-following



Slung Load Operations - disturbance of the Load Test-case using the ASLquad



Vehicle: ASLquad

Type of trajectory: Position hold

Nature of disturbance: Disturbance introduced from a 0.16kg slung load which is externally disturbed

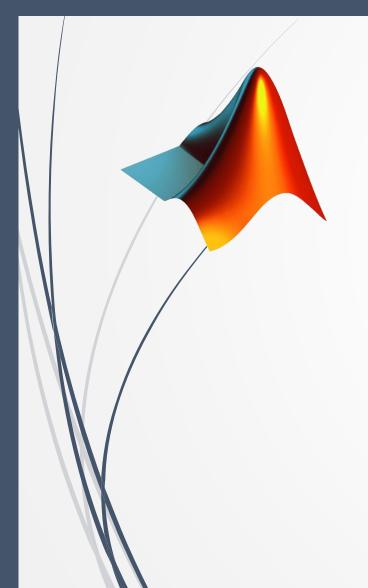
Corresponding results using the UPAT-TTR unmanned rotorcraft are also presented later on in the same video sequence





ETH Manipulator

Code Examples and Tasks



- <u>https://github.com/unr-arl/drones_demystified/tree/master/matlab/control-systems/gain-scheduled-three-loop-aircraft-autopilot</u>
- <u>https://github.com/unr-arl/drones_demystified/tree/master/matlab/control-systems/lqr</u>
- <u>https://github.com/unr-arl/drones_demystified/tree/master/matlab/control-systems/pid-cruise-control</u>
- <u>https://github.com/unr-arl/drones_demystified/tree/master/matlab/control-systems/pid</u>

Find out more

- http://www.autonomousrobotslab.com/pid-control.html
- <u>http://www.autonomousrobotslab.com/lqr-control.html</u>
- http://www.autonomousrobotslab.com/linear-model-predictive-control.html
- <u>http://ctms.engin.umich.edu/CTMS/index.php?example=InvertedPendulum</u> <u>§ion=ControlStateSpace</u>

<u>http://www.autonomousrobotslab.com/literature-and-links1.html</u>

