



CS491/691: Introduction to Aerial Robotics

Topic: Sampling-based Motion Planning

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The motion planning problem

- ▶ Consider a dynamical control system defined by an ODE of the form:

$$\frac{dx}{dt} = f(x, u), x(0) = x_{init} \quad (1)$$

- ▶ Where is x the state, u is the control.
- ▶ Given an obstacle set X_{obs} , and a goal set X_{goal} , the objective of the motion planning problem is to find, if it exists, a control signal u such that the solution of (1) satisfies $x(t) \notin X_{obs}$ for all $t \in \mathbb{R}^+$, and $x(t) \in X_{goal}$ for all $t > T$, for some finite $T \geq 0$. Return failure if no such control signal exists.

- ▶ Basic problem in robotics
- ▶ Provably hard: a basic version of it (the Generalized Piano Mover's problem) is known to be PSPACE-hard.

Motion planning in practice

- ▶ Many methods have been proposed to solve such problems in practical applications:
 - ▶ **Algebraic planners:** Explicit representation of obstacles. Use complicated algebra (visibility computations/projections) to find the path. Complete, but impractical.
 - ▶ **Discretization + graph search:** Analytic/grid-based methods do not scale well to high dimensions. Graph search methods (A*, D*, etc.) can be sensitive to graph size. Resolution complete.
 - ▶ **Potential fields/navigation functions:** Virtual attractive forces towards the goal, repulsive forces away from the obstacles. No completeness guarantees; unless “navigation functions” are available – very hard to compute in general.
- ▶ These algorithms achieve tractability by foregoing completeness altogether, or achieving weaker forms of it, e.g. resolution completeness.

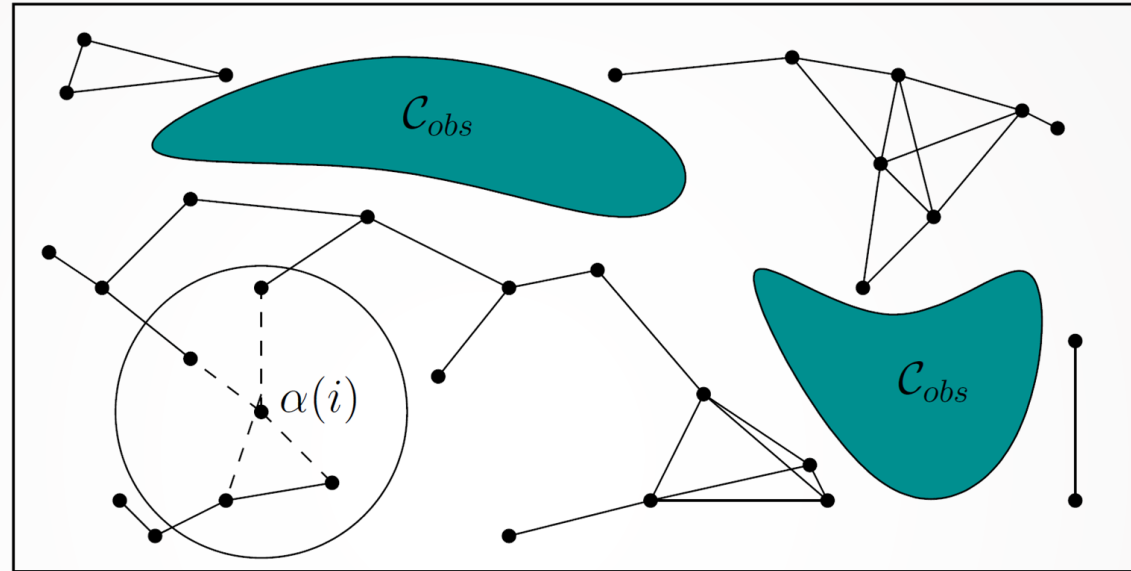
Sampling-based algorithms

- ▶ A recently proposed class of motion planning algorithms that has been very successful in practice is based on (batch or incremental) sampling methods: solutions are computed based on samples drawn from some distribution. Sampling algorithms retain some form of completeness, e.g., probabilistic or resolution completeness.
- ▶ Incremental sampling methods are particularly attractive:
 - ▶ Incremental sampling algorithms lend themselves easily to real-time, on-line implementation.
 - ▶ Applicable to very generic dynamical systems.
 - ▶ Do not require the explicit enumeration of constraints.
 - ▶ Adaptively multi-resolution methods (i.e. make your own grid as you go along, up to the necessary resolution).

Probabilistic RoadMaps (PRM)

- ▶ Introduced by Kavraki and Latombe in 1994.
- ▶ Mainly geared towards “multi-query” motion planning problems.
- ▶ **Idea:** build (offline) a graph (i.e., the roadmap) representing the “connectivity” of the environment – use this roadmap to find paths quickly at run-time.
- ▶ **Learning/pre-processing phase:**
 - ▶ Sample n points from $X_{free} = [0,1]^d \setminus X_{obs}$.
 - ▶ Try to connect these points using a fast “local planner” (e.g. ignore obstacles).
 - ▶ If connection successful (i.e. no collisions), add an edge between the points.
- ▶ **At run-time:**
 - ▶ Connect the start and end goal to the closest nodes in the roadmap.
 - ▶ Find a path on the roadmap.
- ▶ *First planner ever to demonstrate the ability to solve generic planning problems in > 4-5 dimensions!*

Probabilistic RoadMap example



- **“Practical” algorithm:**

- Incremental construction.
 - Connects points within a radius r , starting from “closest” ones.
 - Do not attempt to connect points that are already on the same connected component of the RPM.
- *What kind of properties does this algorithm have? Will it find a solution if there is one? Will that be an optimal solution? What is the complexity of the algorithm?*

Probabilistic Completeness

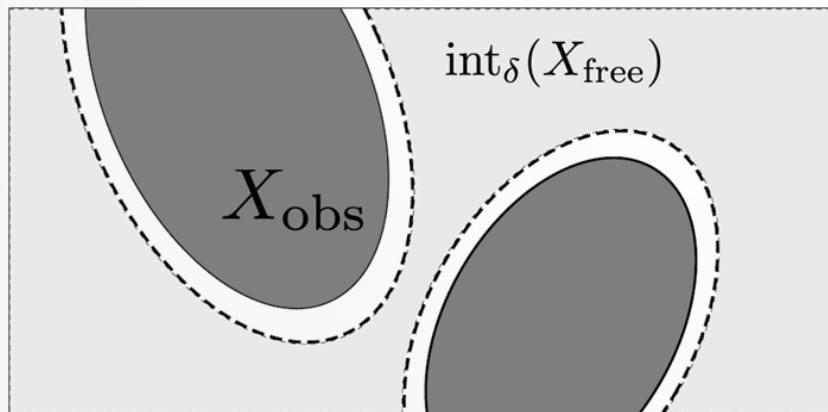
► Definition – Probabilistic Completeness:

► An algorithm ALG is probabilistically complete if, for any robustly feasible motion planning problem defined by $P = (X_{free}, x_{init}, X_{goal})$, then:

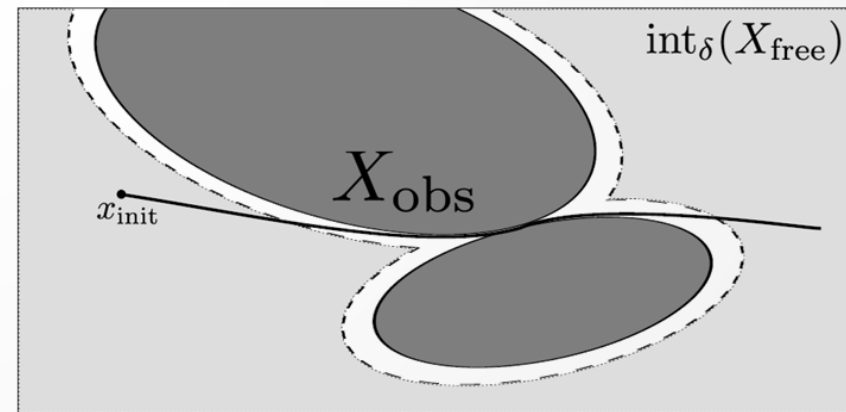
$$\lim_{N \rightarrow \infty} \Pr(\text{ALG returns a solution } P) = 1$$

► A “relaxed” notion of completeness

► Applicable to motion planning problems with a robust solution. A robust solution remains a valid solution even when the obstacles are “dilated” by small δ .



robust



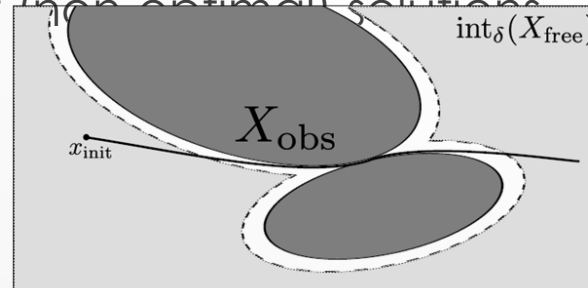
NOT robust

Asymptotic Optimality

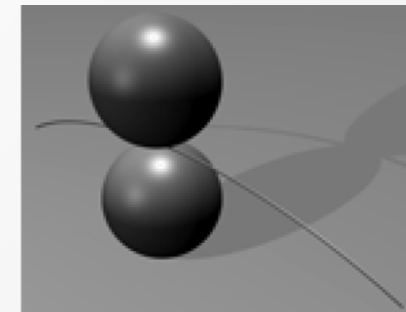
- ▶ Definition – Asymptotic Optimality:
- ▶ An algorithm ALG is asymptotically optimal if, for any motion planning problem defined by $P = (X_{free}, x_{init}, X_{goal})$ and function c that admit a robust optimal solution with finite cost c^* ,

$$P \left(\left\{ \lim_{i \rightarrow \infty} Y_i^{ALG} = c^* \right\} \right) = 1$$

- ▶ The function c associates to each path σ a non-negative $c(\sigma)$, e.g. $c(\sigma) = \int_{\sigma} X(s) ds$
- ▶ The definition is applicable to optimal motion planning problem with a robust optimal solution. A robust optimal solution is such that it can be obtained as a limit of robust (non-optimal) solutions.



NOT robust



robust



Complexity

- ▶ How can we measure complexity for an algorithm that does not necessarily terminate?
- ▶ Treat the number of samples as the “size of the input” (Everything else stays the same).
- ▶ Also, complexity per sample: how much effort (time/memory) is needed to process one sample.
- ▶ Useful for comparison of sampling-based algorithms.
- ▶ Cannot compare with deterministic, complete algorithms.

Simple PRM (sPRM)

sPRM Algorithm

```
 $V \leftarrow \{x_{init}\} \cup \{SampleFree_i\}_{i=1,\dots,N-1}; E \leftarrow \emptyset;$   
foreach  $v \in V$  do:  
     $U \leftarrow Near(G = (V, E), v, r) \setminus \{v\};$   
    foreach  $u \in U$  do:  
        if  $CollisionFree(v, u)$  then  $E \leftarrow E \cup \{(v, u), (u, v)\}$   
return  $G = (V, E);$ 
```

- ▶ The simplified version of the PRM algorithm has been shown to be probabilistically complete.
- ▶ Moreover, the probability of success goes to 1 exponentially fast, if the environment satisfies “good visibility” conditions.
- ▶ New key concept: combinatorial complexity vs “visibility”.

Remarks on PRM

- ▶ sPRM is probabilistically complete and asymptotically optimal.
- ▶ PRM is probabilistically complete but NOT asymptotically optimal.
- ▶ Complexity for N samples: $O(N^2)$.
- ▶ Practical complexity-reduction tricks:
 - ▶ k-nearest neighbors: connect to the k nearest neighbors. Complexity $O(N \log N)$. (Finding nearest neighbors takes $\log N$ time.)
 - ▶ Bounded degree: connect at most k nearest neighbors among those within radius r .
 - ▶ Variable radius: change the connection radius r as a function of N . How?

Rapidly-exploring Random Trees

- ▶ Introduced by LaValle and Kuffner in 1998.
- ▶ Appropriate for single-query planning problems.
- ▶ Idea: build (online) a tree, exploring the region of the state space that can be reached from the initial condition.
- ▶ At each step: sample one point from X_{free} , and try to connect it to the closest vertex in the tree.
- ▶ Very effective in practice, “Voronoi bias”.

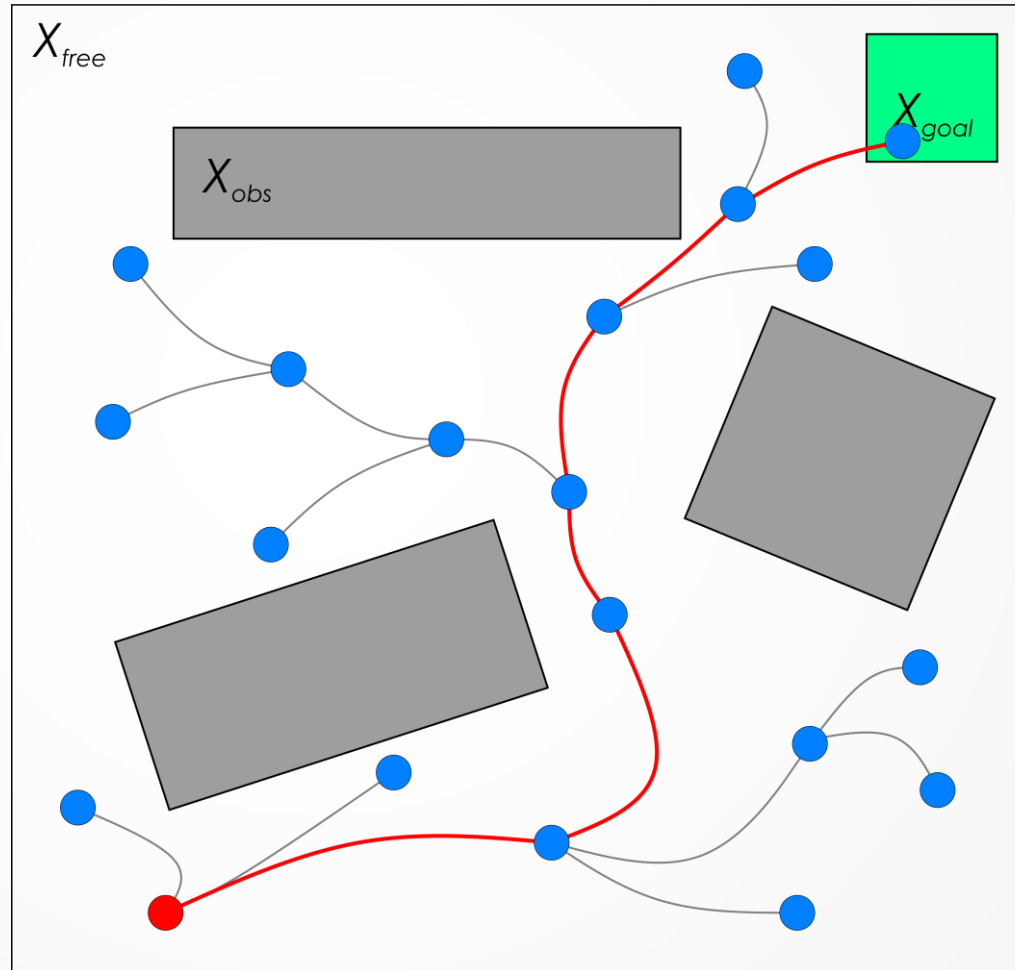
Rapidly-exploring Random Trees

RRT

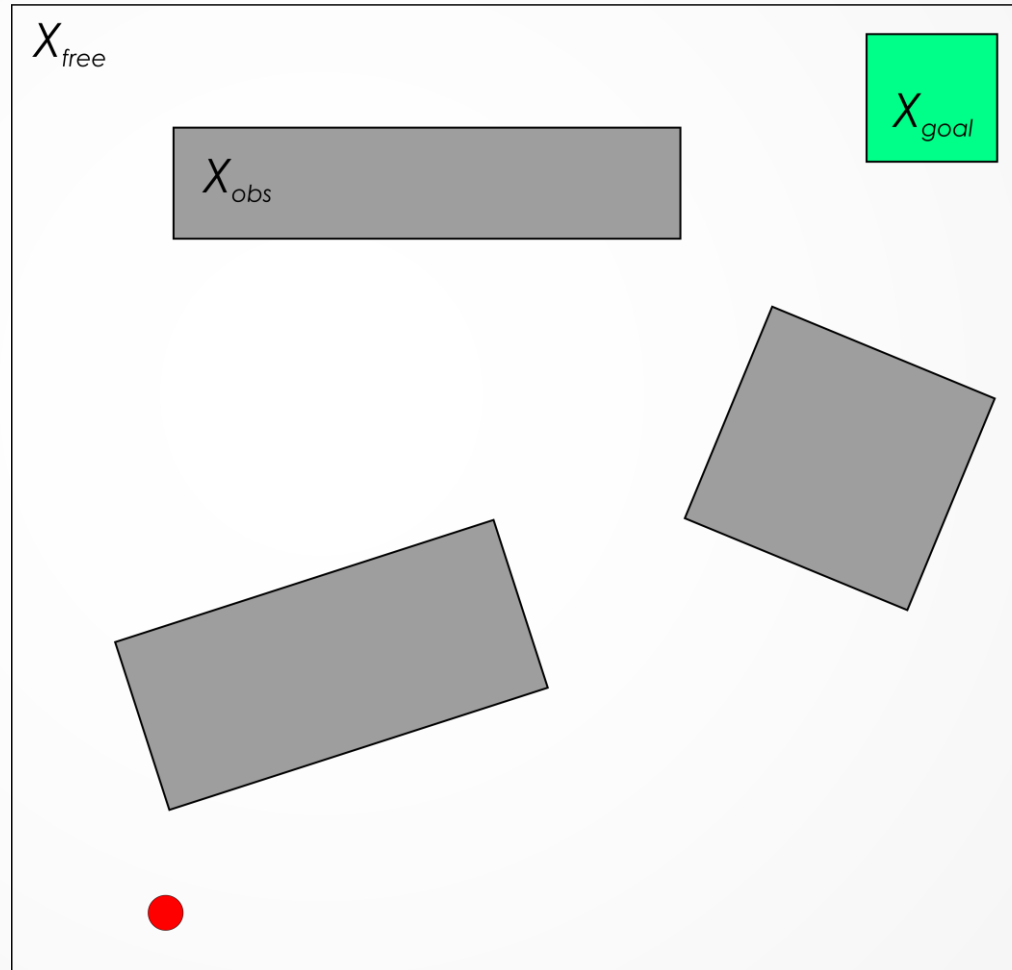
```
 $V \leftarrow \{x_{init}\}; E \leftarrow 0;$   
for  $i=1, \dots, N$  do:  
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     $x_{nearest} \leftarrow \text{Nearest}(G = (V, E), x_{rand});$   
     $x_{new} \leftarrow \text{Steer}(x_{nearest}, x_{rand});$   
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         $V \leftarrow V \cup \{x_{new}\}; E \leftarrow E \cup \{(x_{nearest}, x_{new})\};$   
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- ▶ The RRT algorithm is probabilistically complete
- ▶ The probability of success goes to 1 exponentially fast, if the environment satisfies certain “good visibility” conditions.

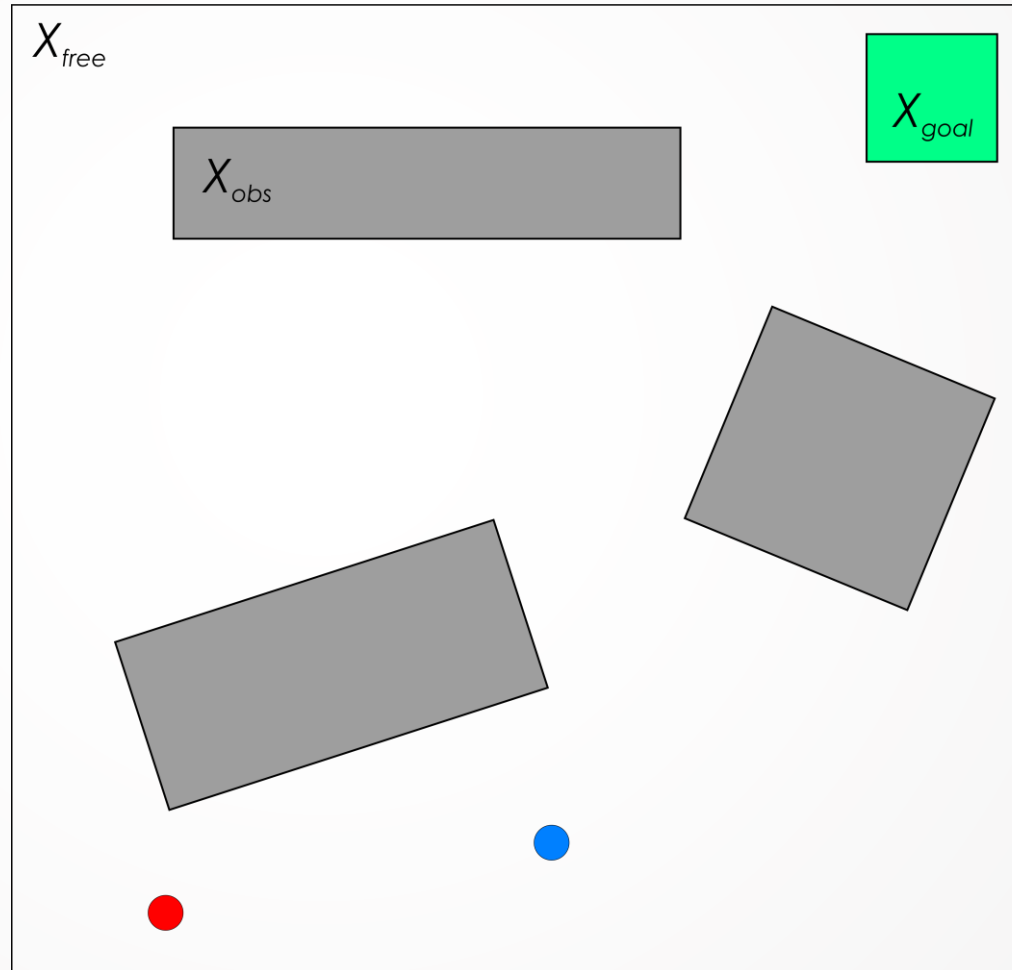
Rapidly-exploring Random Trees (RRTs)



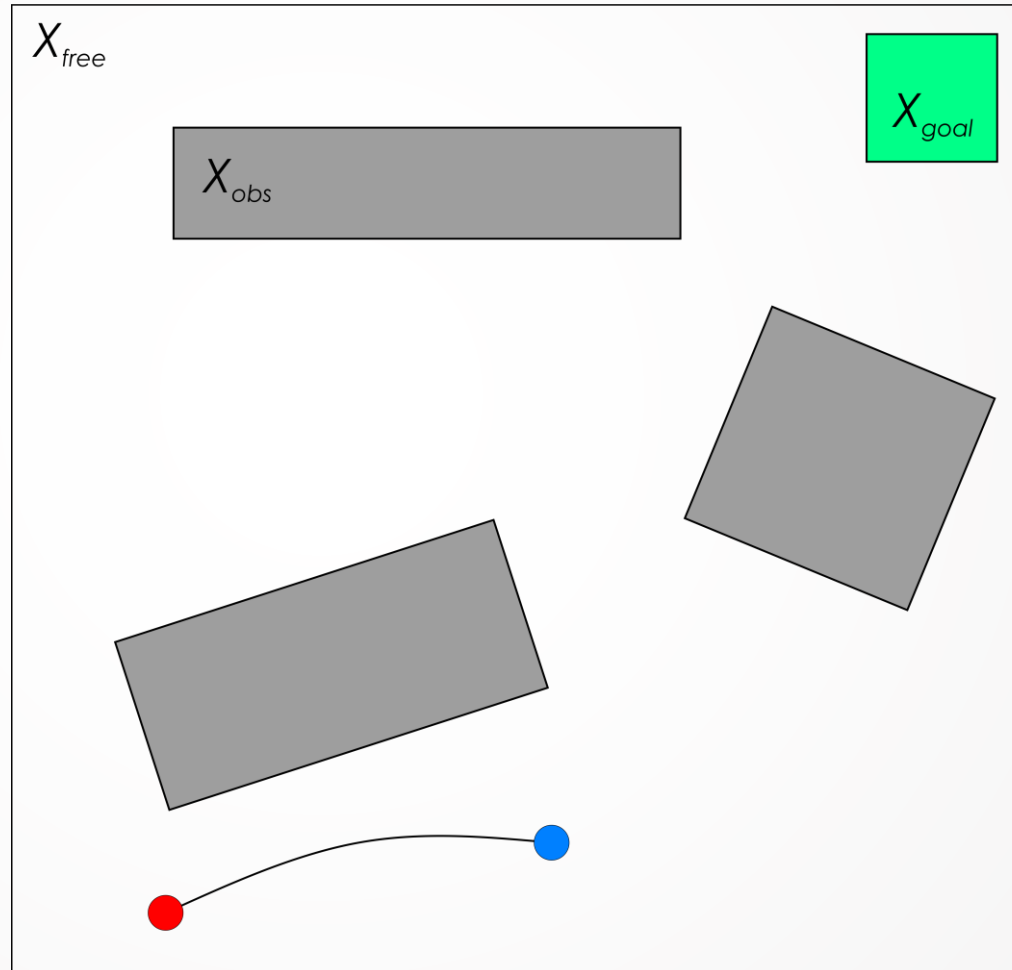
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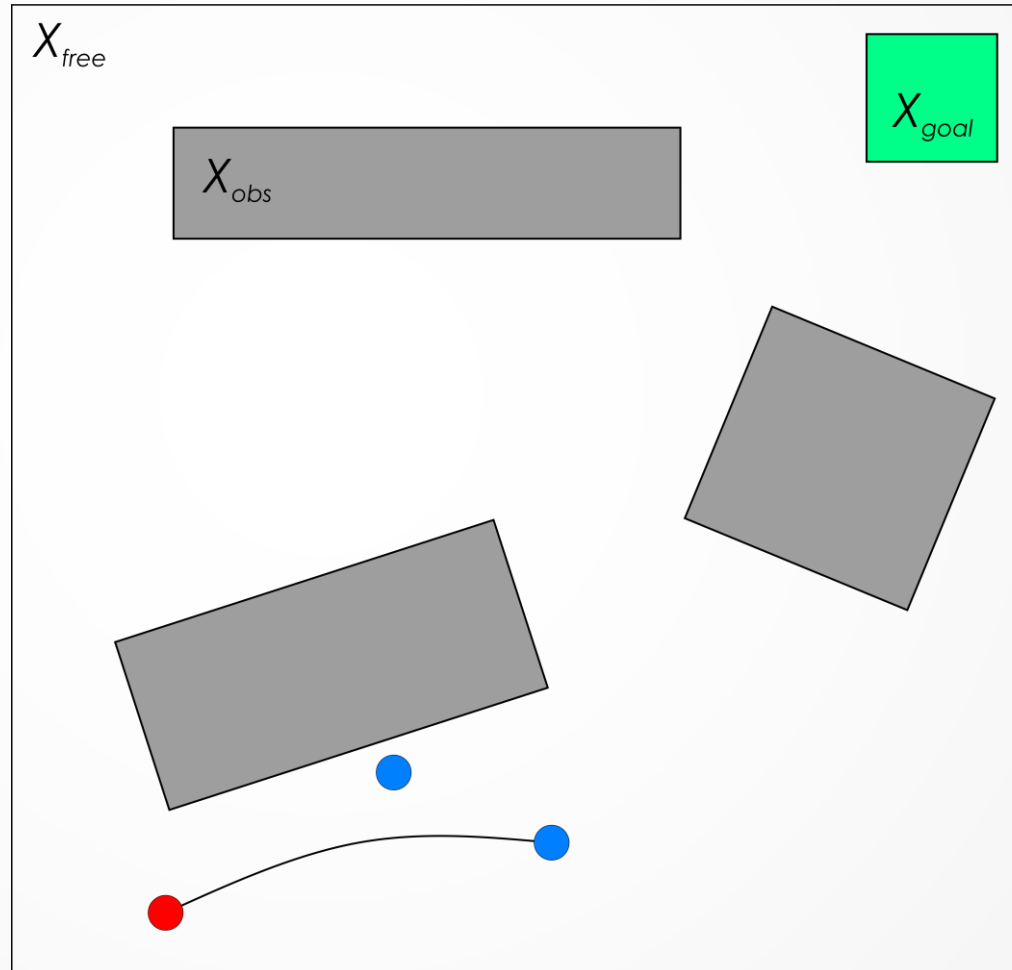
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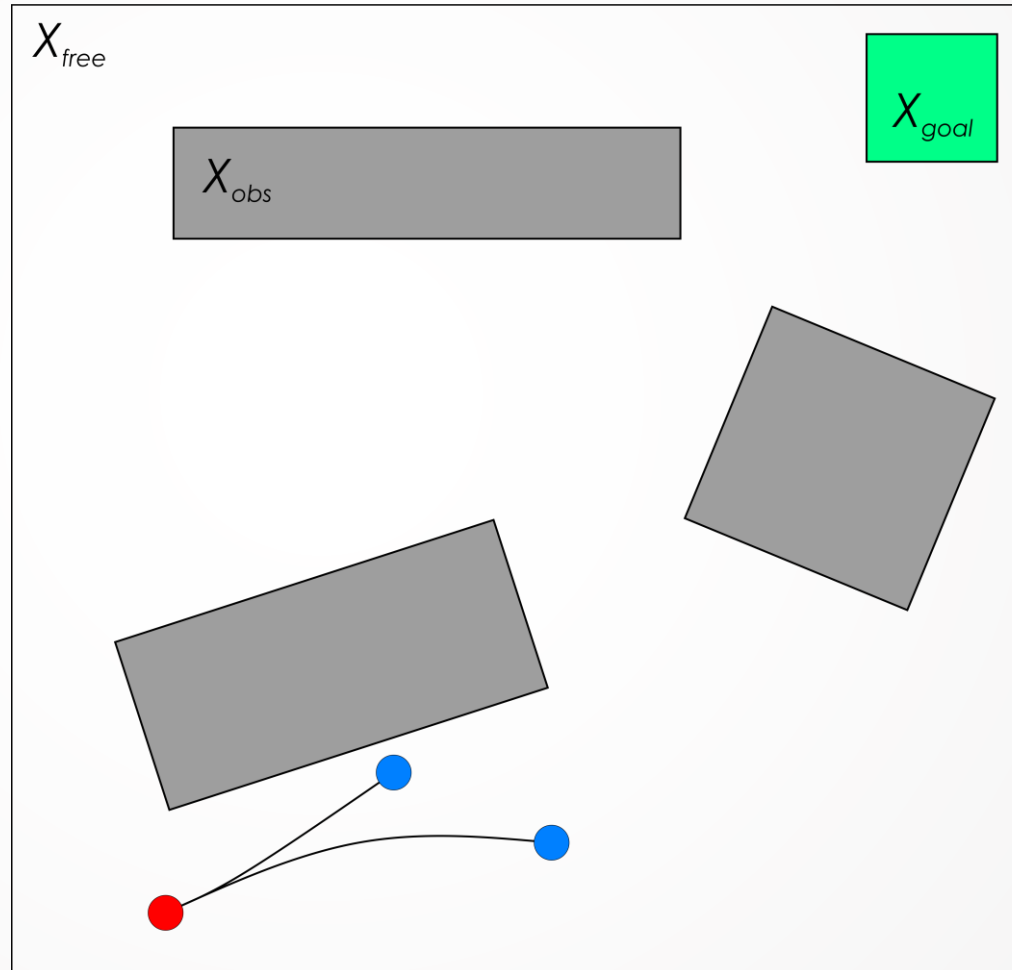
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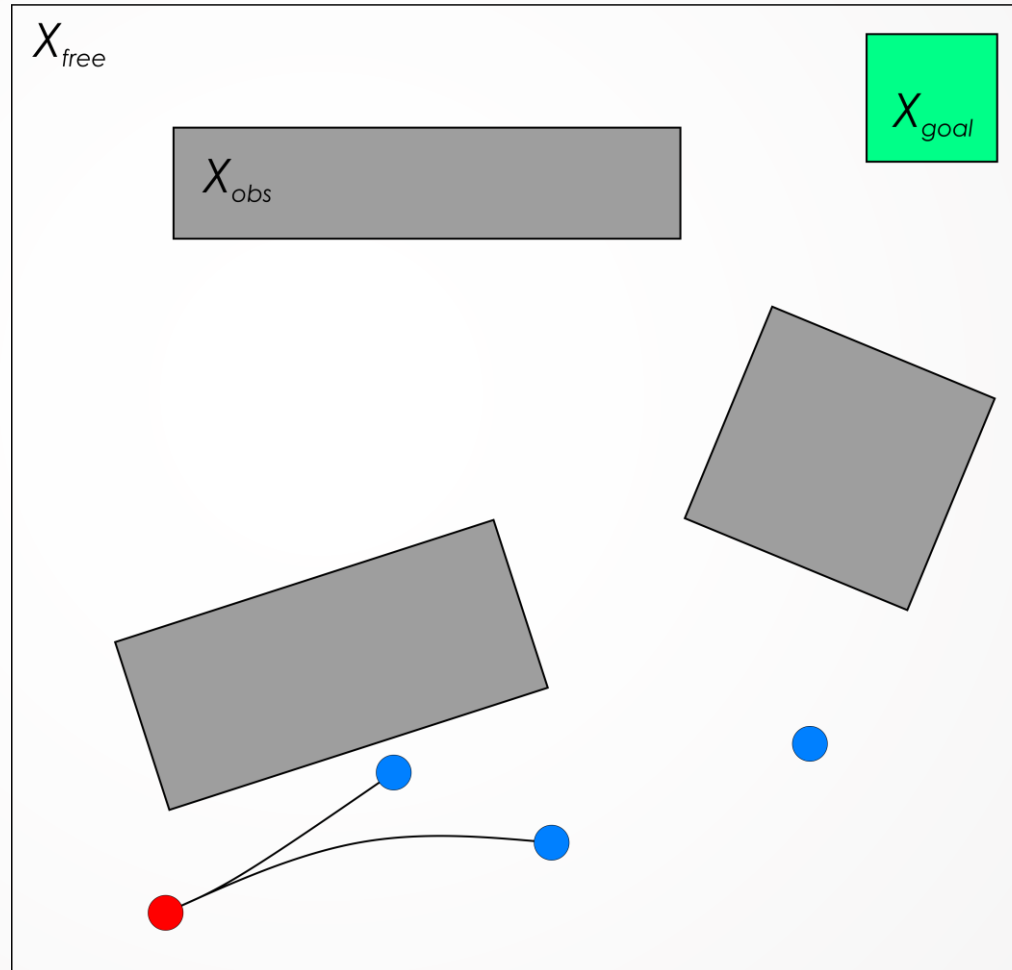
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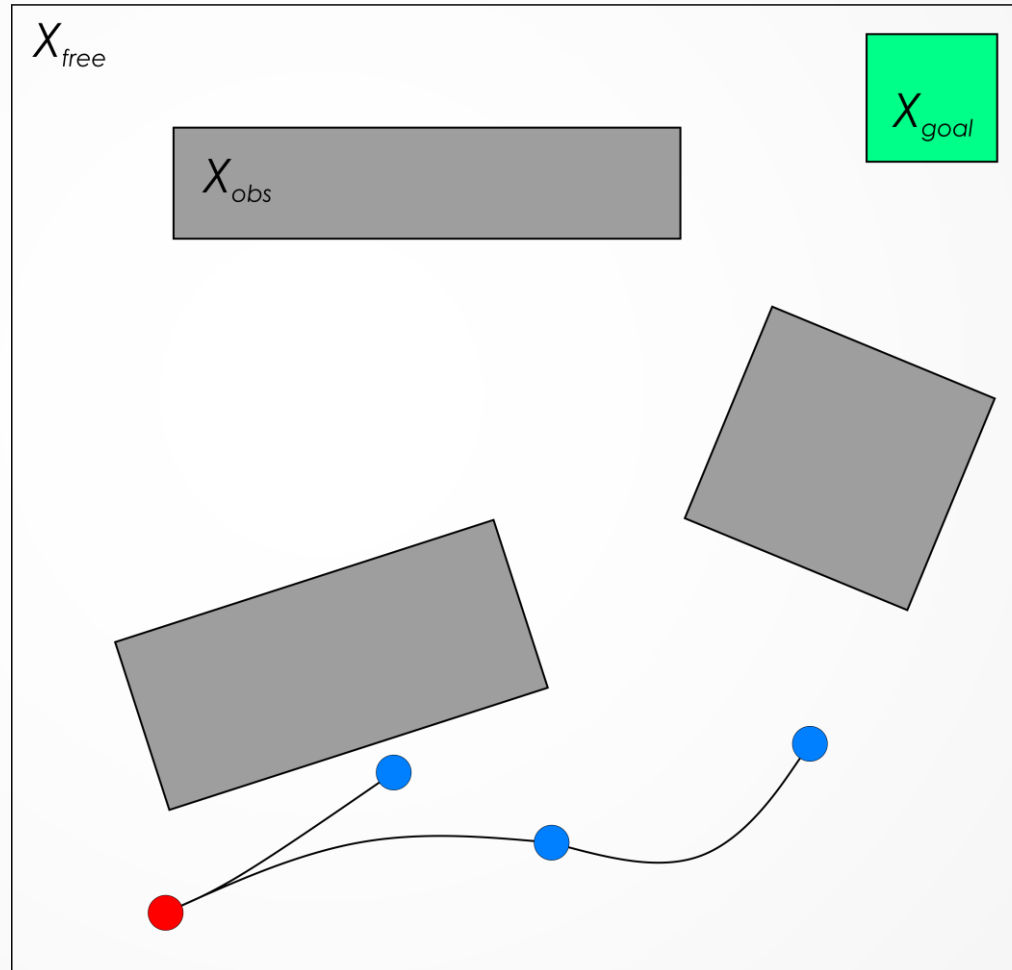
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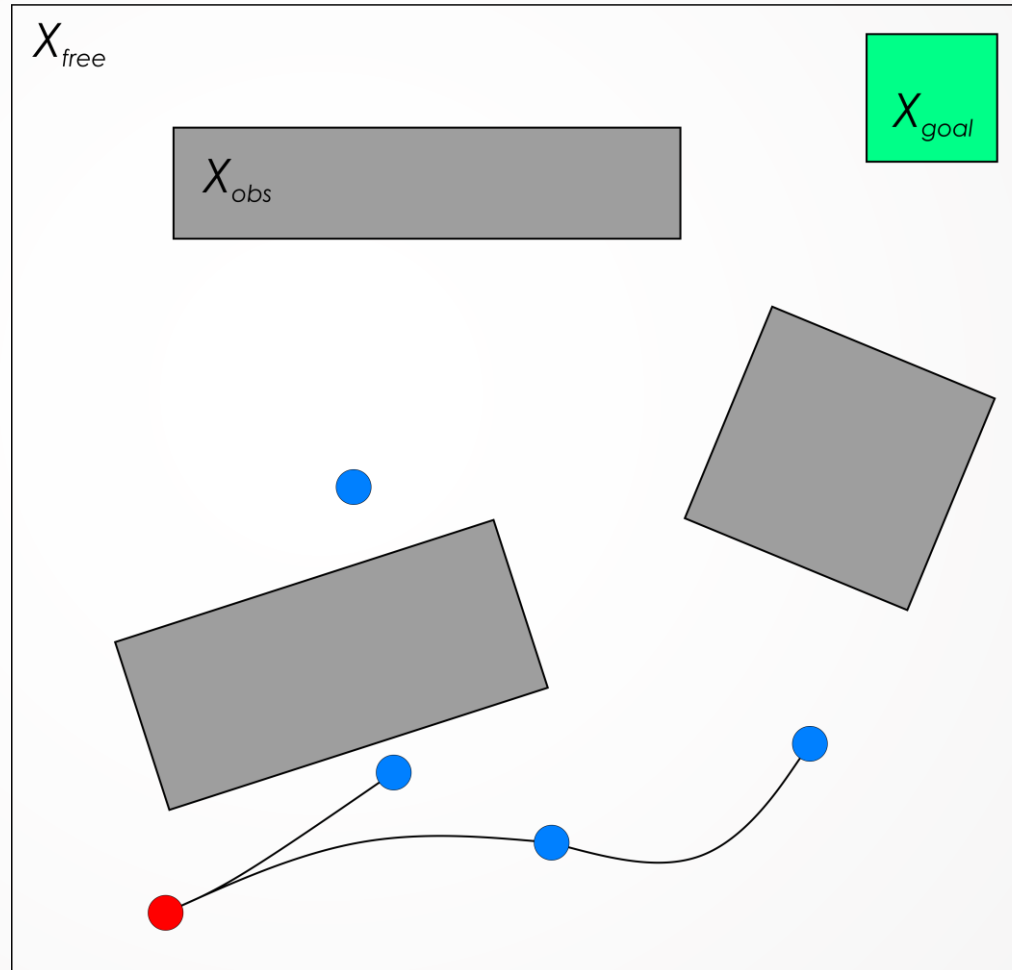
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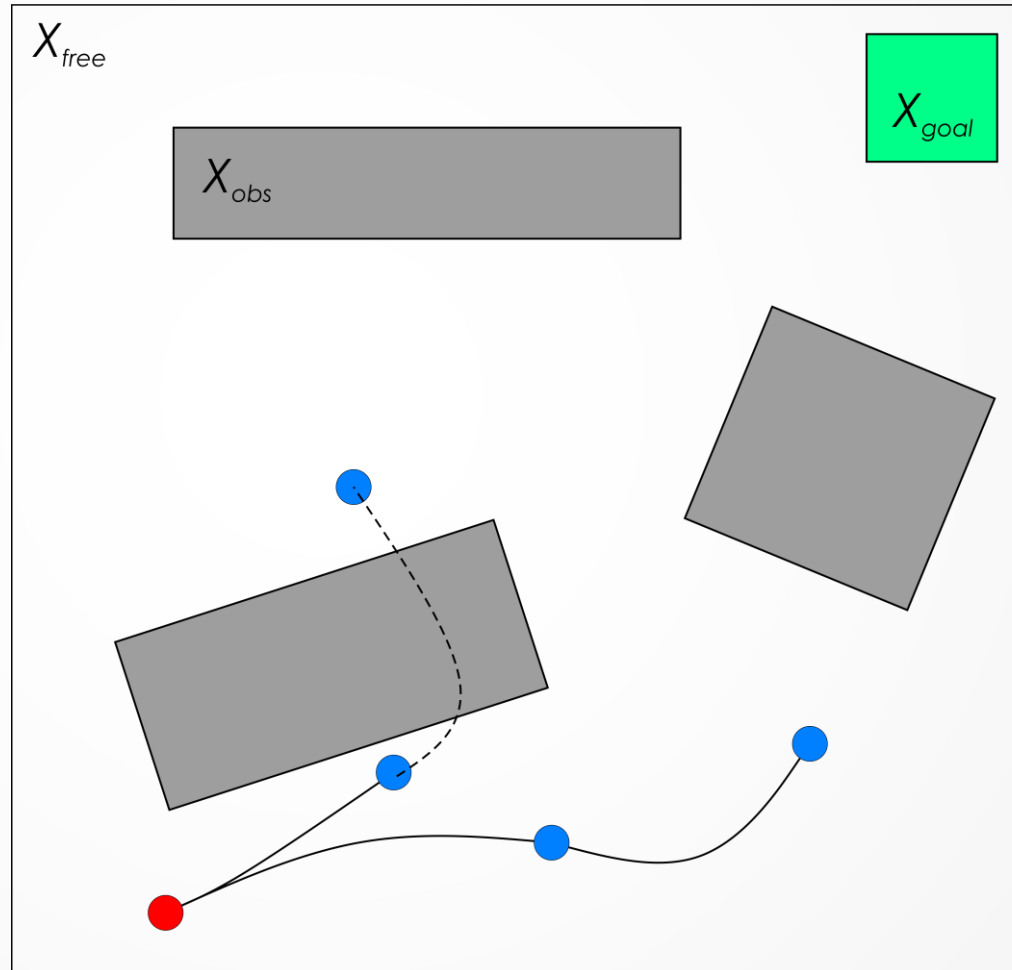
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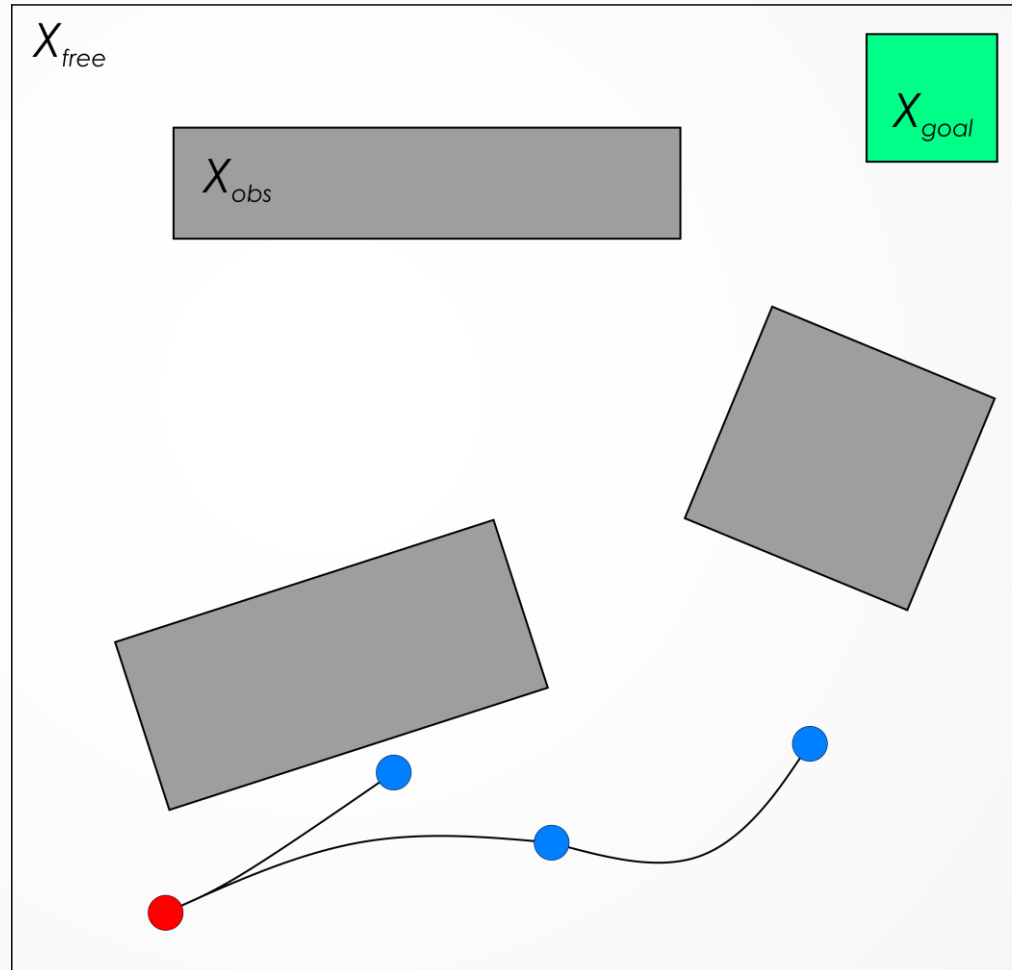
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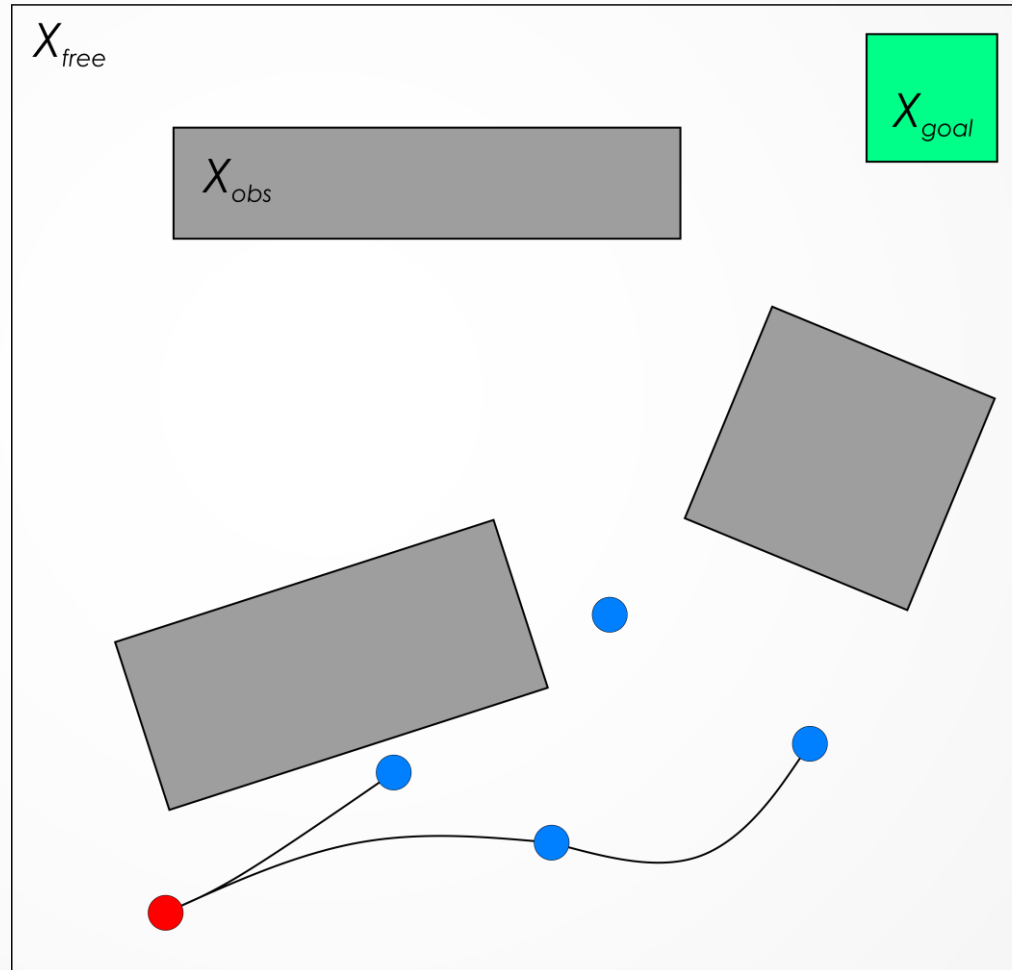
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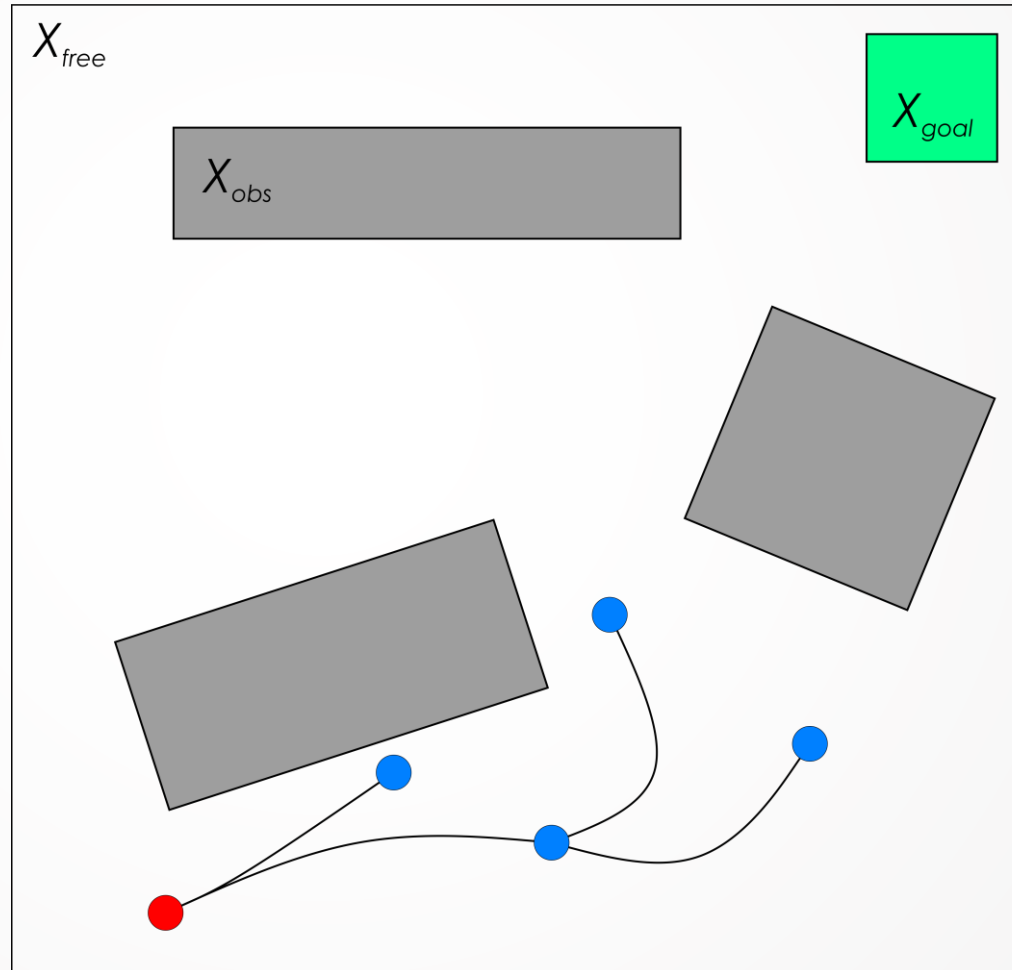
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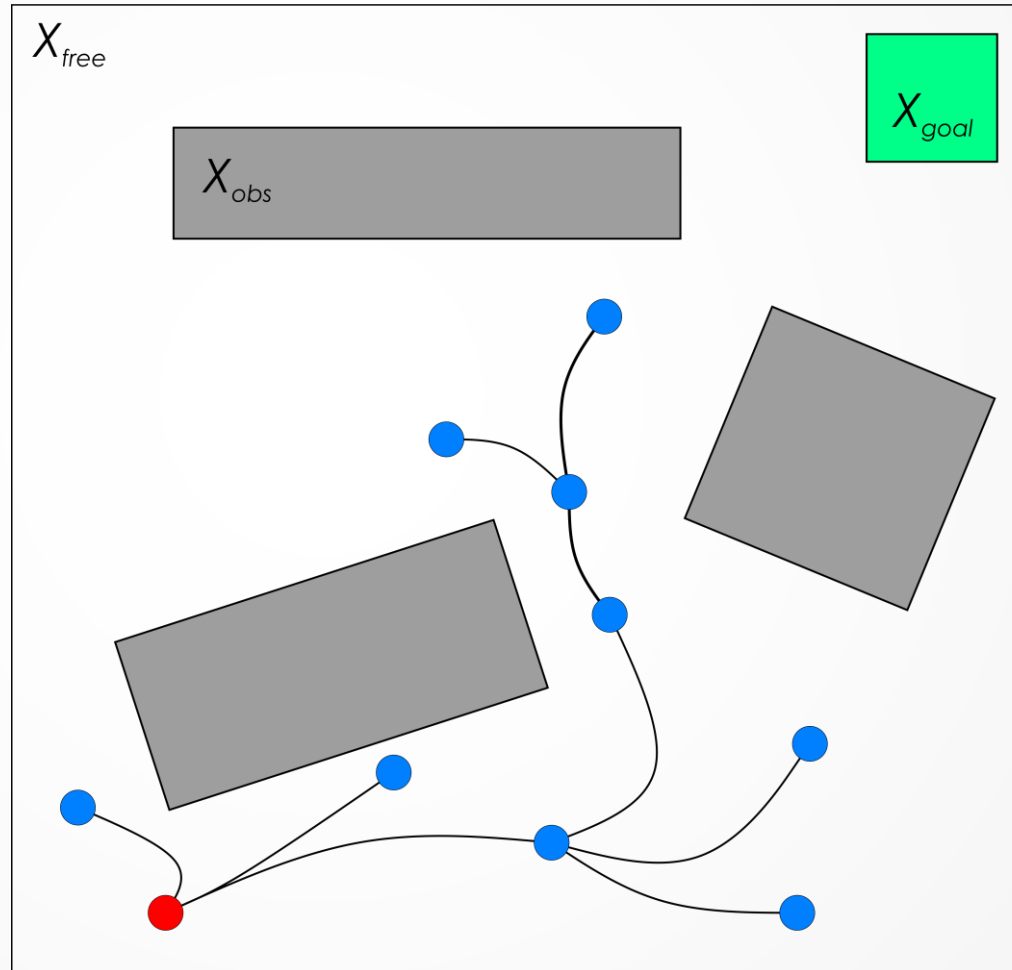
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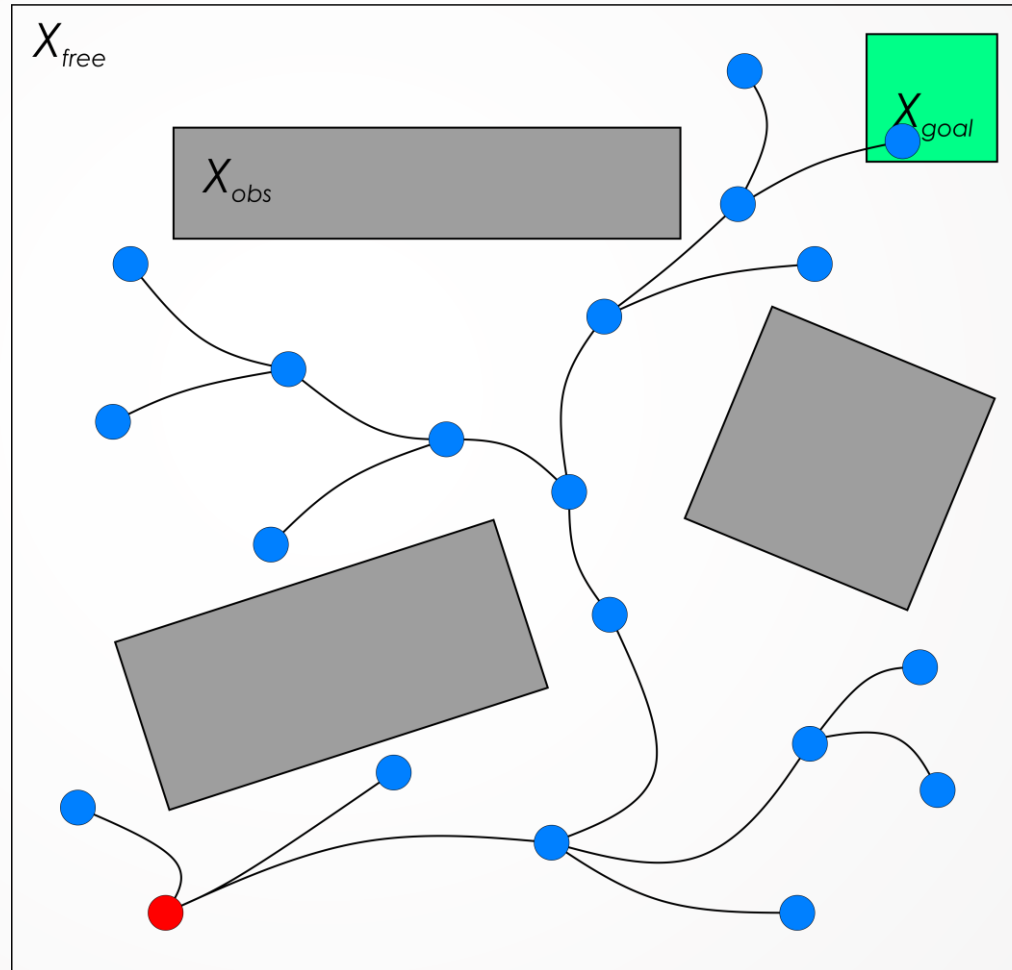
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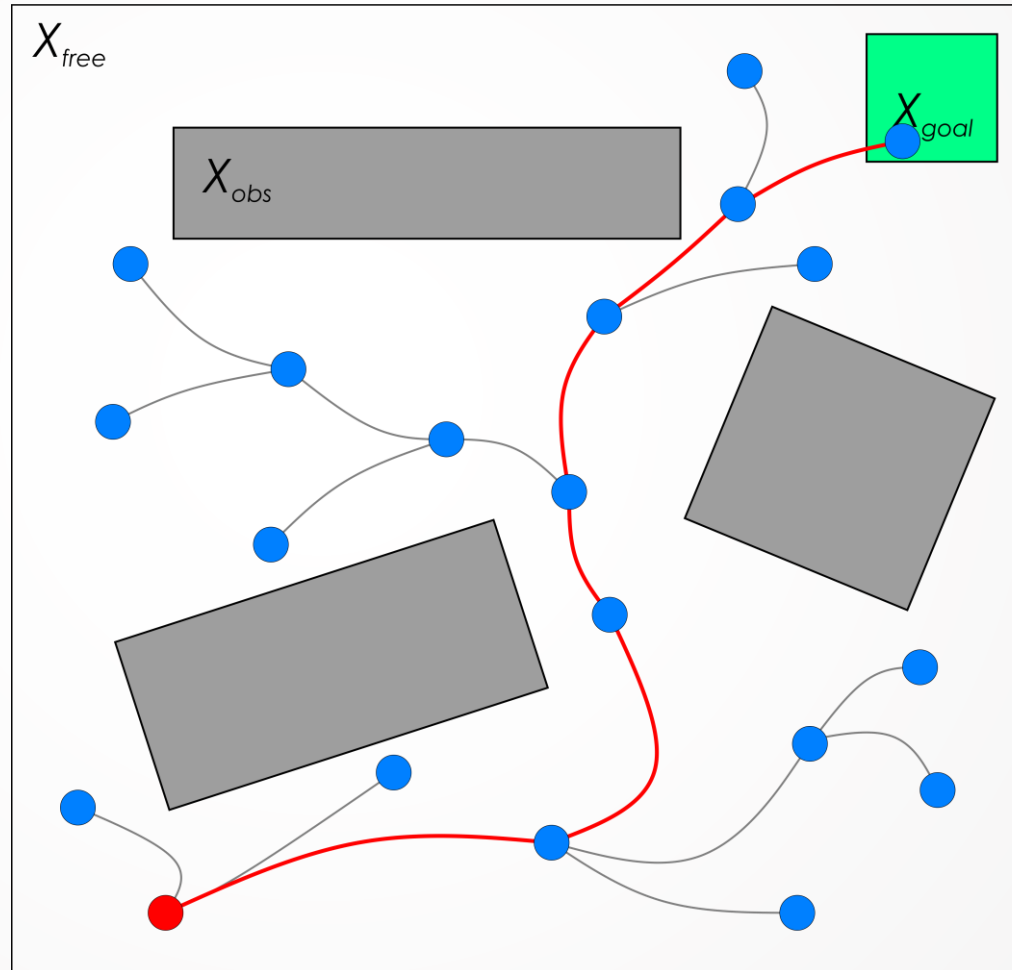
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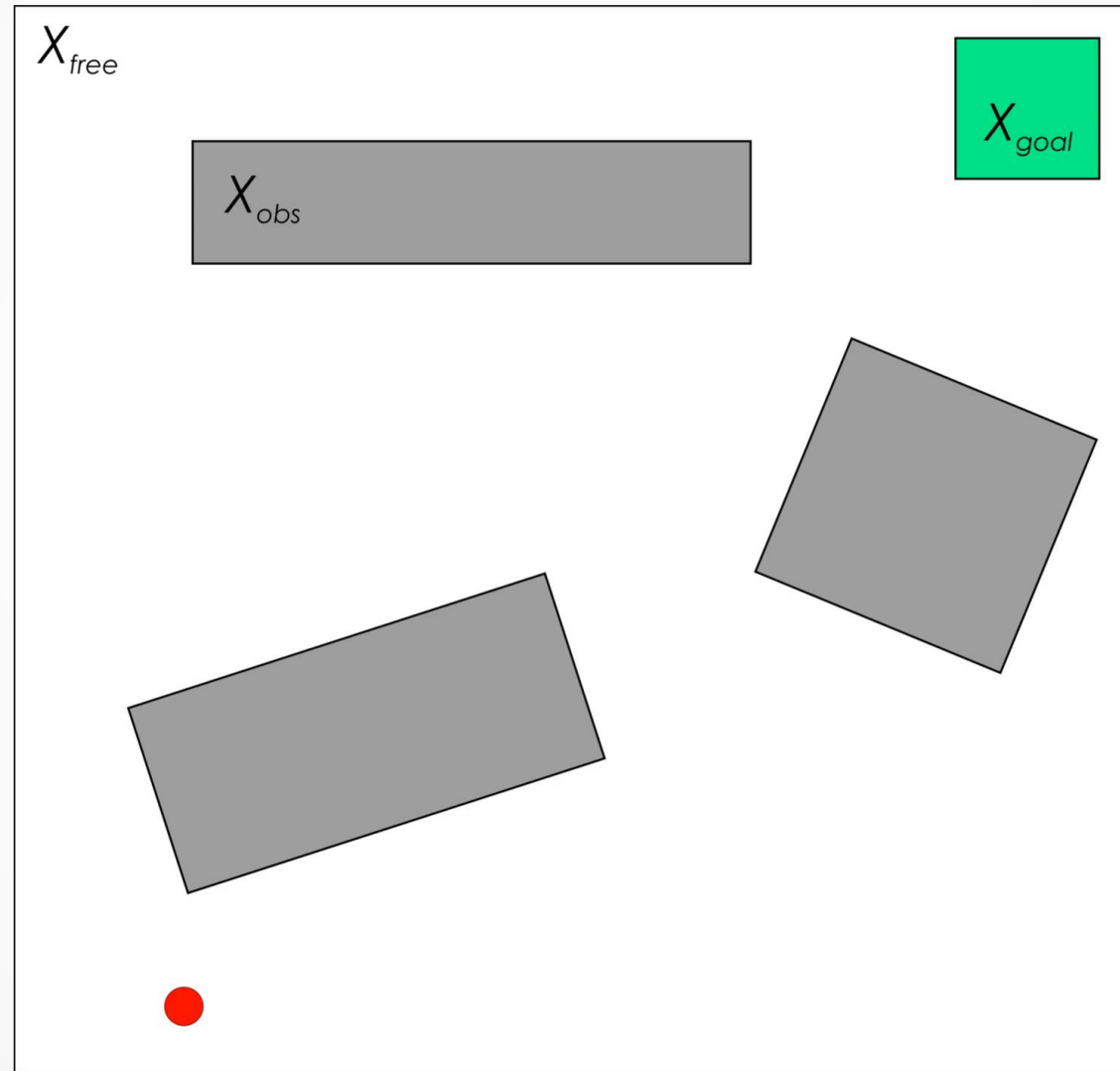
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Voronoi bias

Definition - Voronoi diagram:

Given n sites in d dimensions, the Voronoi diagram of the sites is a partition of \mathbb{R}^d into regions, one region per site, such that all points in the interior of each region lie closer to that regions site than to any other site.

- Vertices of the RRT that are more “isolated” (e.g. in unexplored areas, or at the boundary of the explored area) have the larger Voronoi regions – and are more likely to be selected for extension.

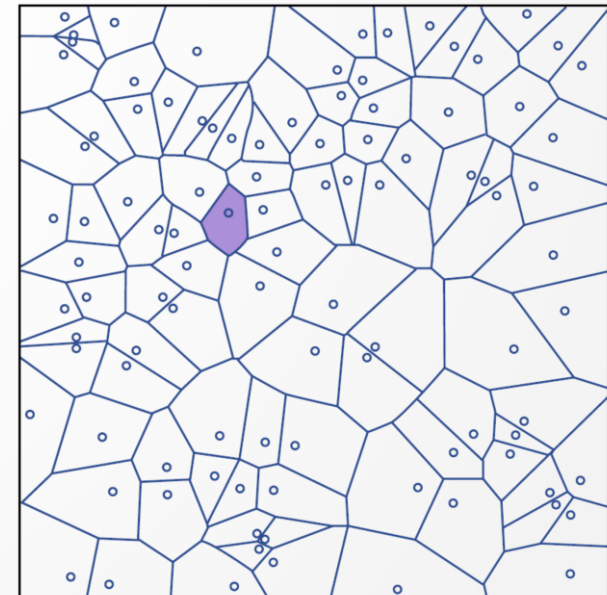
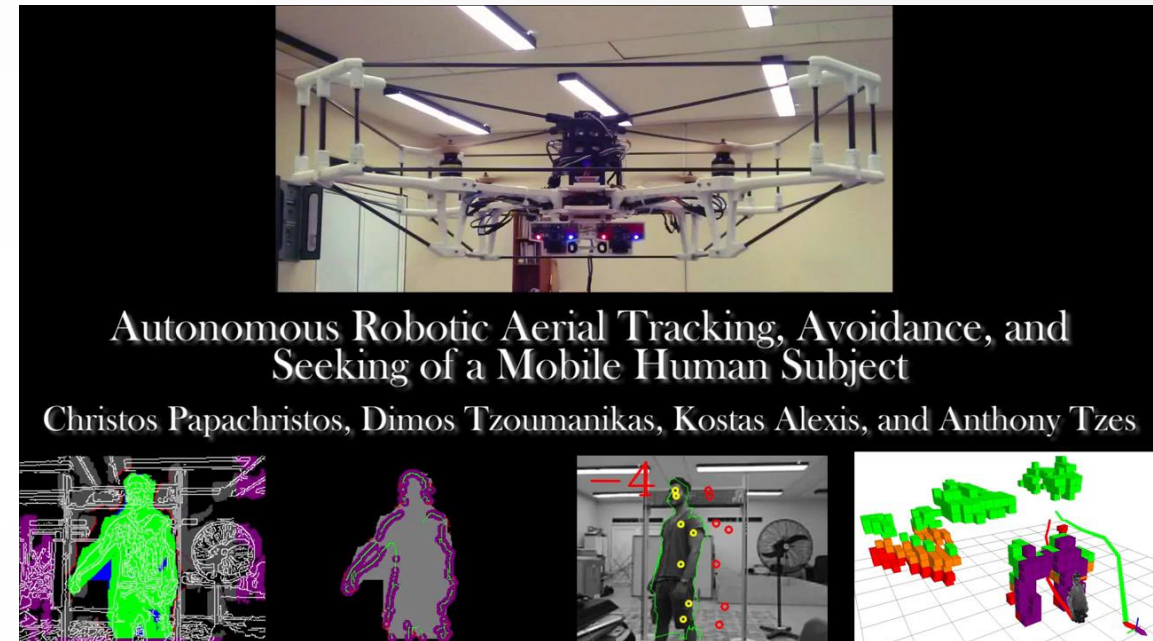


Image by MIT OpenCourseWare.

RRTs in action



- Great results for collision-avoidance of UAVs
- Integral component of several, higher-level algorithms (e.g. exploration and inspection)

Limitations of such incremental sampling methods

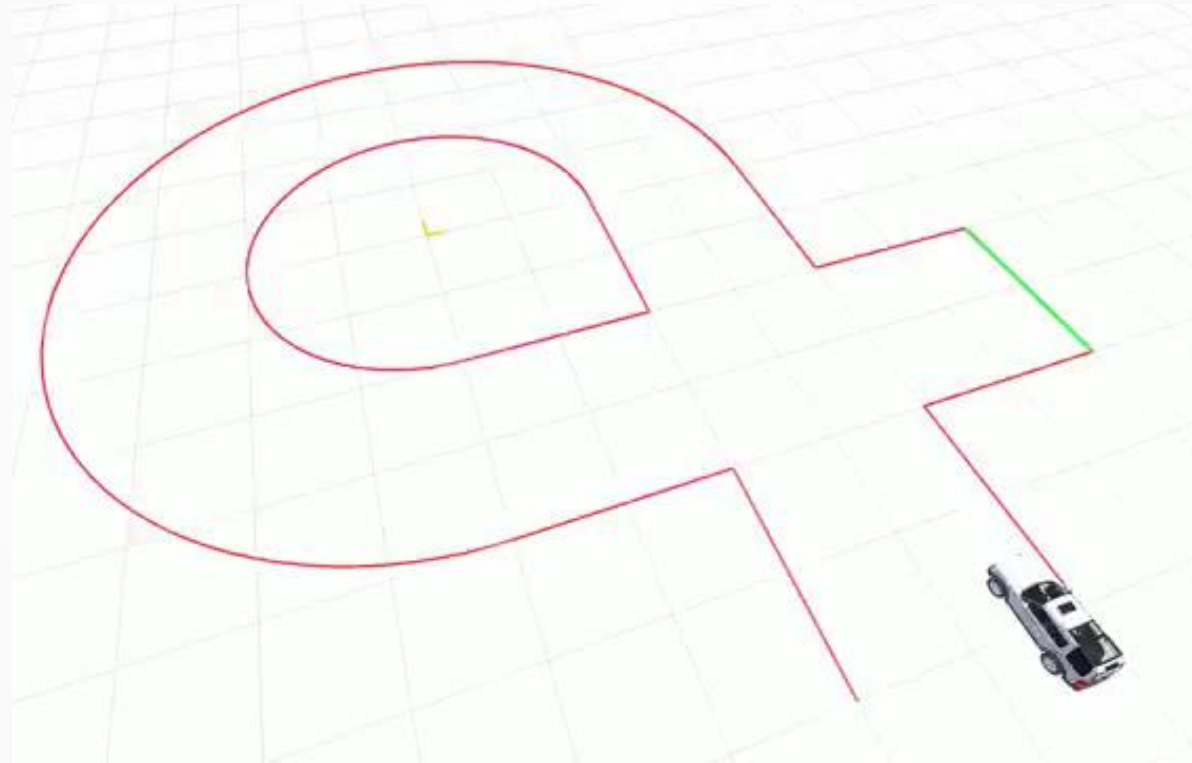
- ▶ No characterization of the quality (e.g. “cost”) of the trajectories returned by the algorithm.

Keep running the RRT even after the first solution has been obtained, for as long as possible (given the real-time constraints), hoping to find a better path than the one already available.

- ▶ No systematic method for imposing temporal/logical constraints, such as, e.g. the rules of the road, complicated mission objectives, ethical/ deontic code.

Next RRT*

- ▶ Asymptotically optimal collision-free navigation.



Video Sertac Karaman, MIT

RRTs don't have the best behavior

- ▶ Let Y_n^{RRT} be the cost of the best path in the RRT at the end of iteration n
- ▶ It is easy to show that Y_n^{RRT} converges (to a random variable), i.e.:
$$\lim_{n \rightarrow \infty} Y_n^{RRT} = Y_\infty^{RRT}$$
- ▶ The random variable Y_∞^{RRT} is sampled from a distribution with zero mass at the optimum:

Theorem – Almost sure suboptimality of RRTs

If a set of sampled optimal paths has measure zero, the sampling distribution is absolutely continuous with positive density in X_{free} and $d \geq 2$, then the best path in the RRT converges to a sub-optimal solution almost surely, i.e.:

$$\Pr[Y_\infty^{RRT} > c^*] = 1$$

Some remarks on that negative result

- ▶ **Intuition:** RRT does not satisfy a necessary condition for asymptotic optimality, i.e., that the root node has infinitely many subtrees that extend at least a distance ϵ away from x_{init} .
- ▶ The RRT algorithm “traps” itself by disallowing new better paths to emerge.
- ▶ **Heuristics such as**
 - ▶ Running the RRT multiple times
 - ▶ Running multiple times concurrently
 - ▶ Deleting and rebuilding parts of the tree etc.

Work better than the standard RRT, but cannot remove the sub-optimal behavior.

- ▶ **How can we do better?**

Rapidly-exploring Random Graphs (RRGs)

RRG Algorithm

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     $x_{new} \leftarrow \text{Steer}(x_{nearest}, x_{rand});$   
    if  $\text{ObstacleFree}(x_{nearest}, x_{new})$  then:  
         $X_{near} \leftarrow \text{Near}\left(G = (V, E), x_{new}, \min\{\gamma_{RRG} \left(\frac{\log(\text{card } V)}{\text{card } V}\right)^{1/d}, \eta\}\right);$   
         $V \leftarrow V \cup \{x_{new}\}; E \leftarrow E \cup \{(x_{nearest}, x_{new}), (x_{nearest}, x_{new})\};$   
        foreach  $x_{near} \in X_{near}$  do:  
            if  $\text{CollisionFree}(x_{near}, x_{new})$  then  $E \leftarrow E \cup \{(x_{near}, x_{new}), (x_{near}, x_{new})\};$   
return  $G = (V, E);$ 
```

- At each iteration, the RRG tries to connect to the new sample all vertices in a ball radius r_n centered at it. (Or simply default to the nearest one if such a ball is empty).
- In general, the RRG builds graphs with cycles.

Properties of RRGs

Theorem – Probabilistic completeness

Since $V_n^{RRG} = V_n^{RRT}$, for all n , it follows that RRG has the same completeness properties of RRT, i.e.

$$\Pr[V_n^{RRG} \cap X_{goal} = \emptyset] = O(e^{-bn})$$

Theorem – Asymptotic optimality

If the *Near* procedure returns all nodes in V within a ball of volume

$$Vol = \gamma \frac{\log n}{n}, \gamma > 2^d(1 + 1/d),$$

Under some additional technical assumptions (e.g., on the sampling distribution, on the ϵ clearance of the optimal path, and on the continuity of the cost function), the best path in the RRG converges to an optimal solution almost surely, i.e.:

$$\Pr[Y_\infty^{RRG} = c^*] = 1$$

Computational complexity

- ▶ At each iteration, the RRG algorithm executes $O(\log n)$ extra calls to *ObstacleFree* when compared to the RRT.
- ▶ However, the complexity of the *Nearest* procedure is $\Omega(\log n)$. Achieved if using, e.g., a Balanced-Box Decomposition (BBD) Tree.

Theorem – Asymptotic (Relative) Complexity

There exists a constant $\beta \in \mathbb{R}_+$ such that

$$\limsup_{i \rightarrow \infty} E \left[\frac{OPS_i^{RRG}}{OPS_i^{RRT}} \right] \leq \beta$$

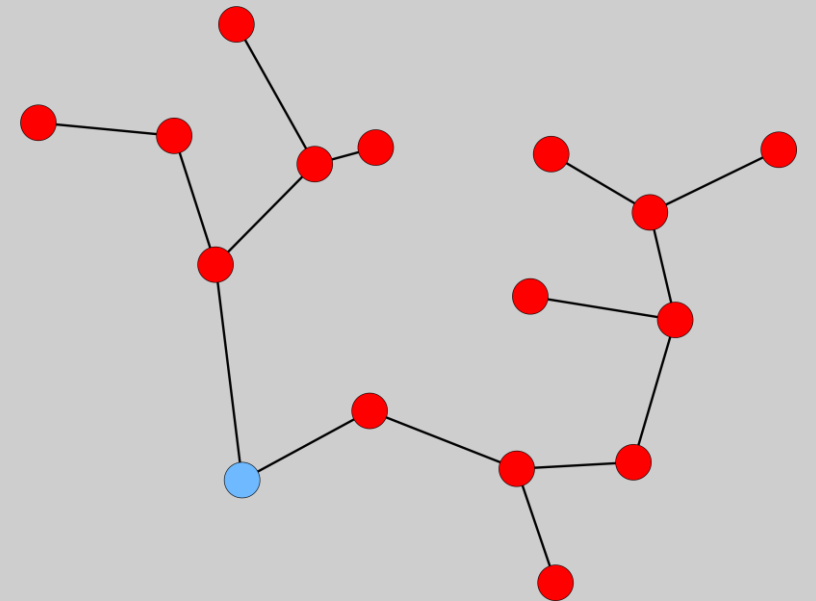
- ▶ In other words, the RRG algorithm has **no substantial computational overhead** over RRT, and ensures asymptotic optimality.

RRT*: A tree version of the RRG

- ▶ RRT algorithm can account for nonholonomic dynamics and modeling errors.
- ▶ RRG requires connecting the nodes exactly, i.e., the *Steer* procedure has to be exact. Exact steering methods are not available for general dynamic systems.

RRT* Algorithm

- RRT* is a variant of RRG that essentially “rewires” the tree as better paths are discovered.
- After rewiring the cost has to be propagated along the leaves.
- If steering errors occur, subtrees can be re-computed.
- The RRT* algorithm inherits the asymptotic optimality and rapid exploration properties of the RRG and RRT.

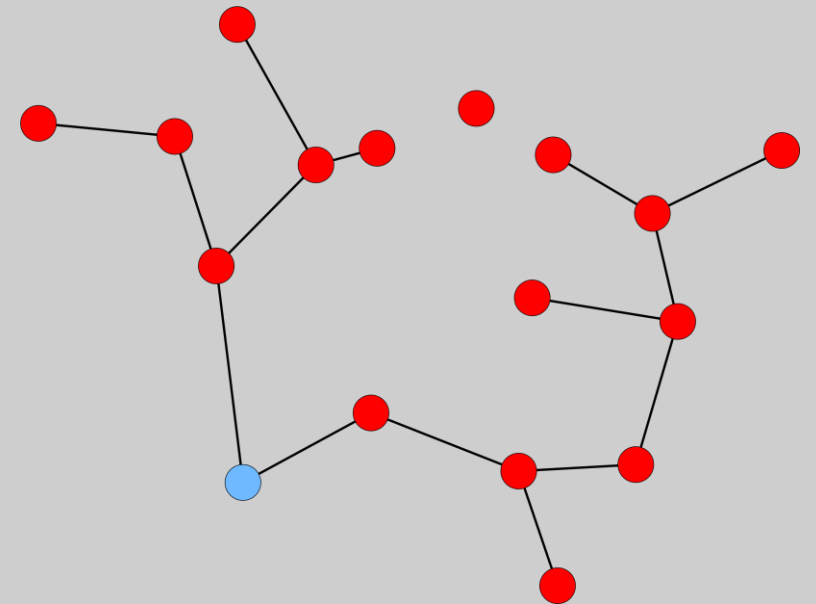


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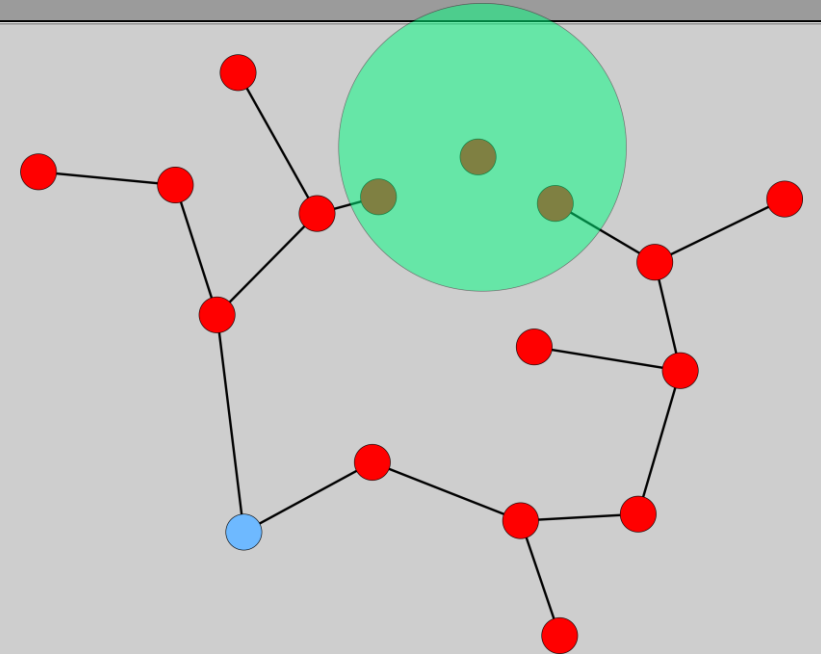


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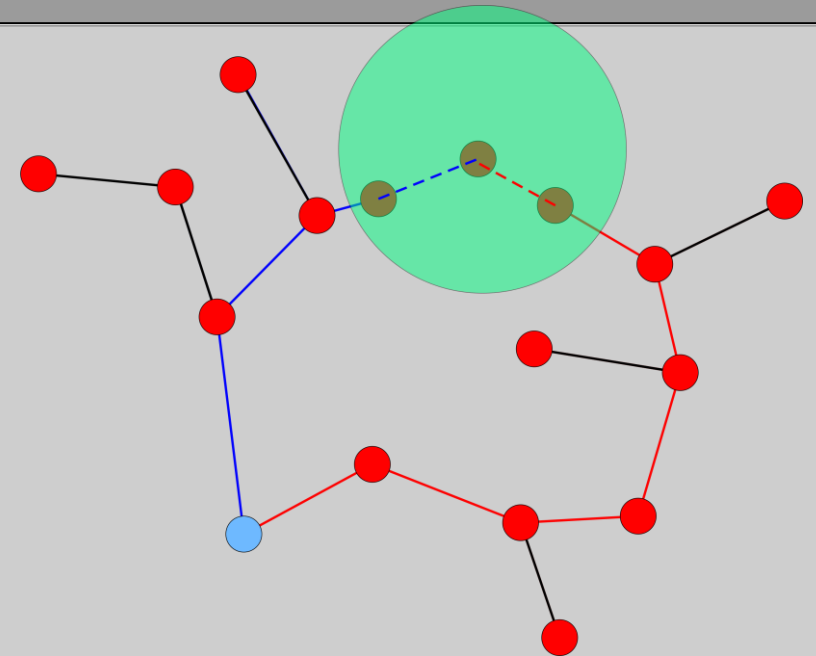


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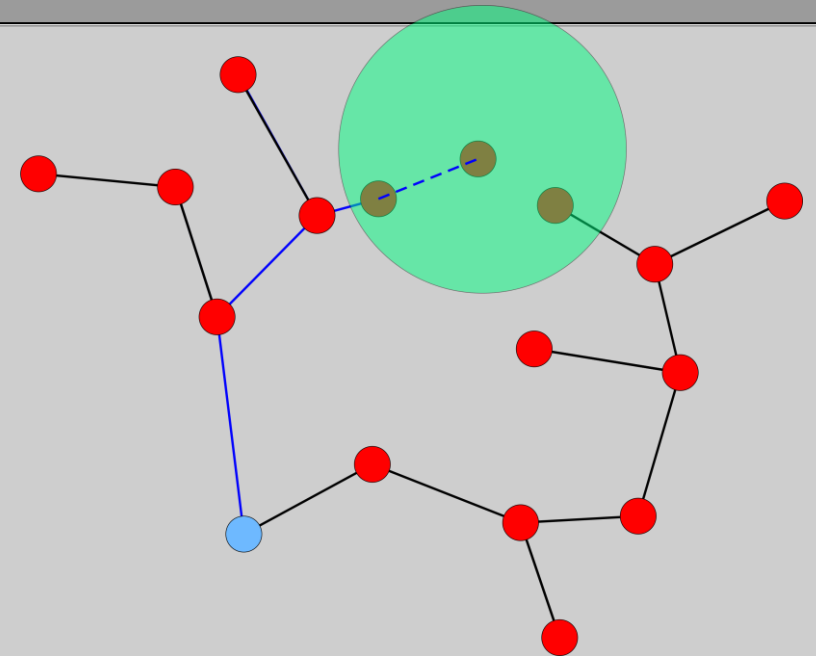


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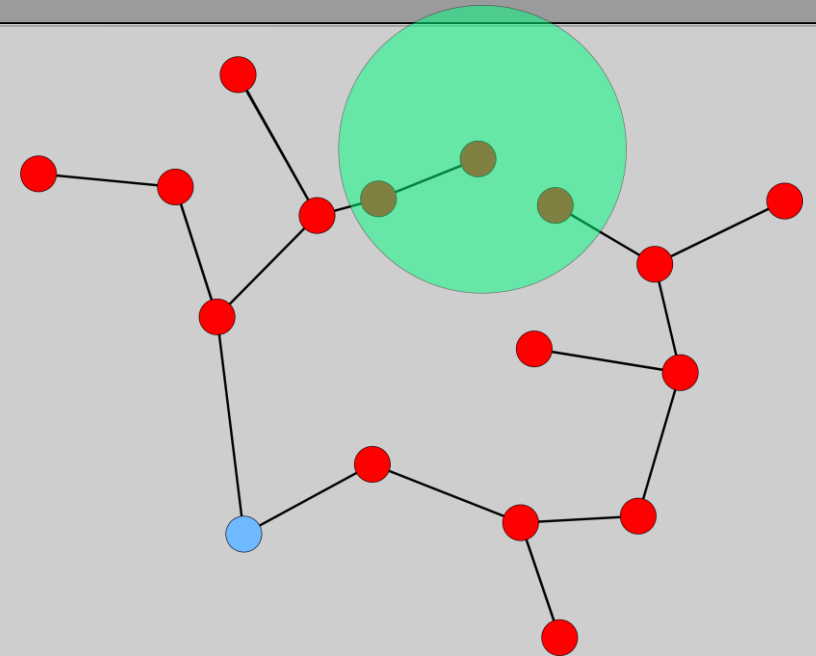


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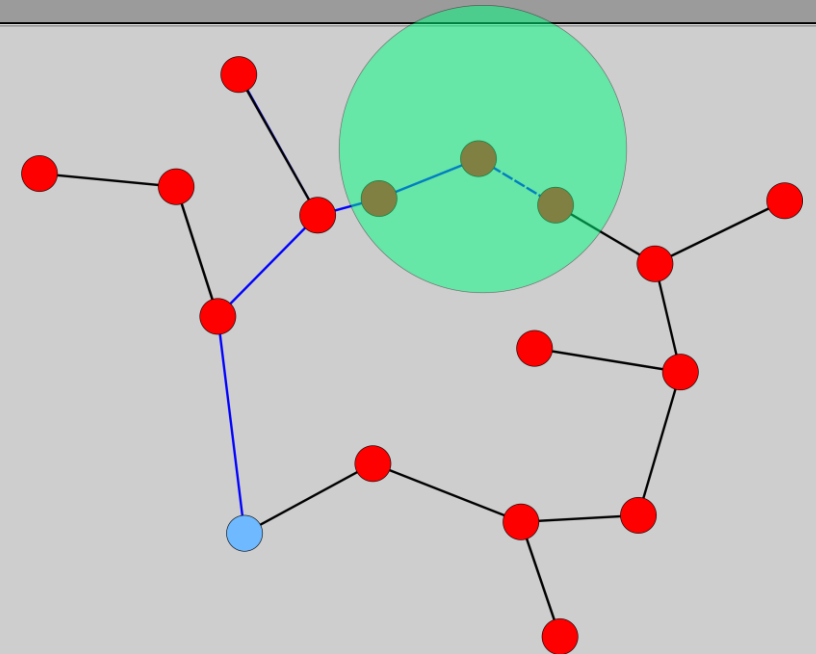


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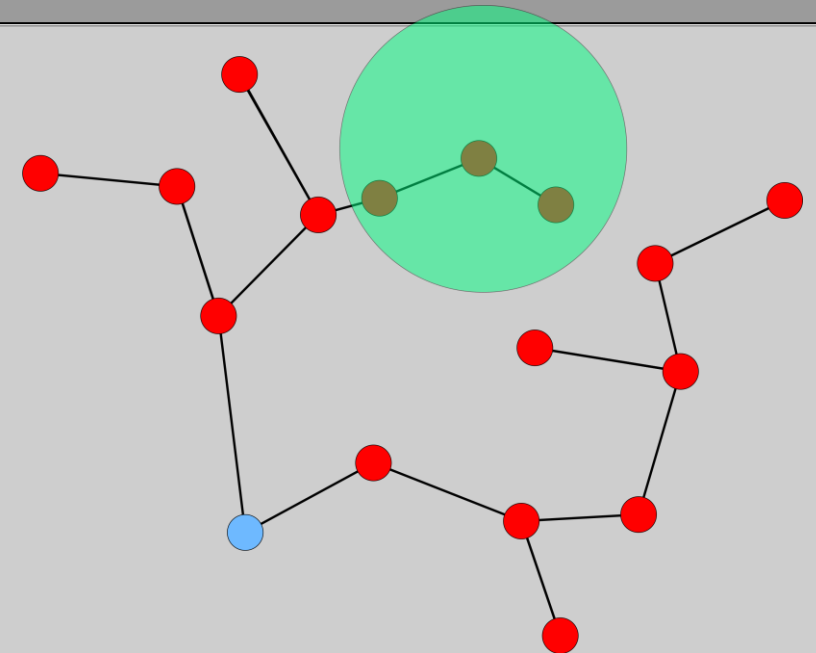


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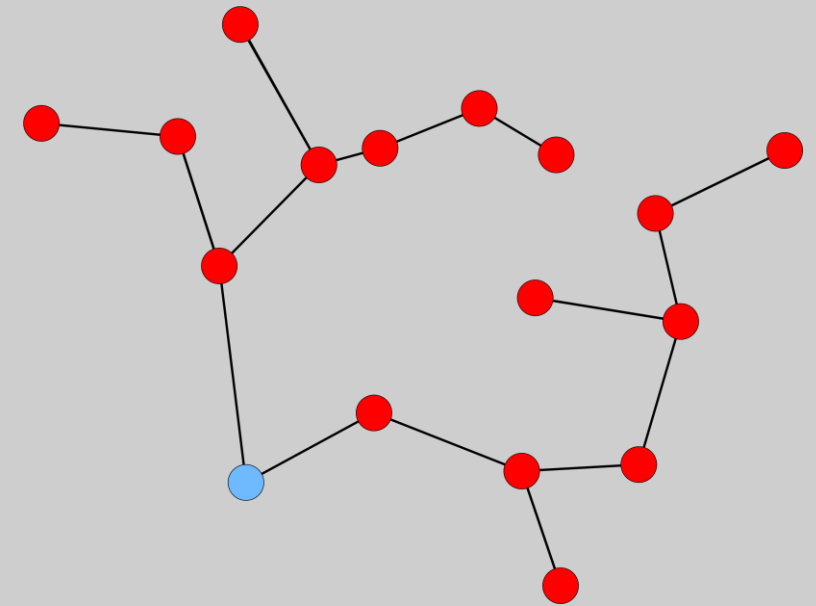


RRT*: A tree version of the RRG

- ▶ RRT algorithm can account for nonholonomic dynamics and modeling errors.
- ▶ RRG requires connecting the nodes exactly, i.e., the *Steer* procedure has to be exact. Exact steering methods are not available for general dynamic systems.

RRT* Algorithm

- RRT* is a variant of RRG that essentially “rewires” the tree as better paths are discovered.
- After rewiring the cost has to be propagated along the leaves.
- If steering errors occur, subtrees can be re-computed.
- The RRT* algorithm inherits the asymptotic optimality and rapid exploration properties of the RRG and RRT.



Rapidly-exploring Random Tree-star (RRT*)

RRT* Algorithm

```
 $V \leftarrow \{x_{init}\}; E \leftarrow 0;$   
for  $i=1, \dots, N$  do:  
   $x_{rand} \leftarrow \text{SampleFree};$   
   $x_{nearest} \leftarrow \text{Nearest}(G = (V, E), x_{rand});$   
   $x_{new} \leftarrow \text{Steer}(x_{nearest}, x_{rand});$   
  if  $\text{ObstacleFree}(x_{nearest}, x_{new})$  then:  
     $X_{near} \leftarrow \text{Near}\left(G = (V, E), x_{new}, \min\left\{\gamma_{RRG} \left(\frac{\log(\text{card } V)}{\text{card } V}\right)^{1/d}, \eta\right\}\right);$   
     $V \leftarrow V \cup \{x_{new}\};$   
     $x_{min} \leftarrow x_{nearest}; c_{min} \leftarrow \text{Cost}(x_{nearest}) + c(\text{Line}(x_{nearest}, x_{new}))$   
    foreach  $x_{near} \in X_{near}$  do:  
      if  $\text{CollisionFree}(x_{near}, x_{new}) \wedge \text{Cost}(x_{near}) + c(\text{Line}(x_{near}, x_{new})) < \text{Cost}(x_{min})$  then:  
         $x_{parent} \leftarrow \text{Parent}(x_{near});$   
         $E \leftarrow E \setminus \{(x_{parent}, x_{near})\} \cup \{(x_{new}, x_{near})\};$   
return  $G = (V, E);$ 
```

Summary

- ▶ **Key idea in RRG/RRT*:** to combine optimality and computational efficiency, it is necessary to attempt connection to $\Theta(\log N)$ nodes at each iteration.
 - ▶ Reduce volume of the “connection ball” as $\log(N)/N$;
 - ▶ Increase the number of connections as $\log N$
- ▶ These principles can be used to obtain “optimal” versions of PRM etc.

Algorithm	Probabilistic Completeness	Asymptotic Optimality	Computational Complexity
sPRM	YES	YES	$O(N)$
k-nearest PRM	NO	NO	$O(\log N)$
RRT	YES	NO	$O(\log N)$
PRM*	YES	YES	$O(\log N)$
k-nearest PRM*	YES	YES	$O(\log N)$
RRG	YES	YES	$O(\log N)$
k-nearest RRG	YES	YES	$O(\log N)$
RRT*	YES	YES	$O(\log N)$
k-nearest RRG	YES	YES	$O(\log N)$

RRT* in Action

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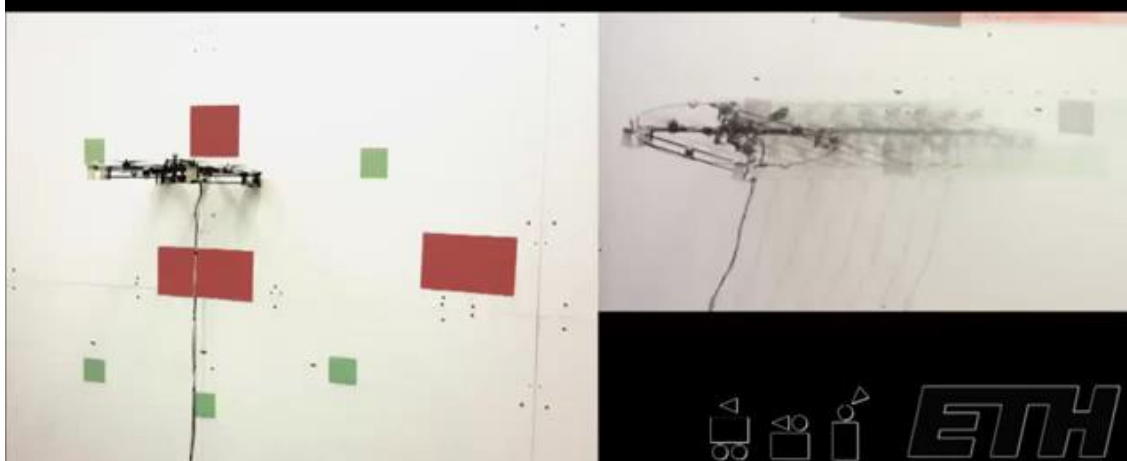


Continuous-Time Trajectory Optimization for Online UAV Replanning

Helen Oleynikova, Michael Burri, Zachary Taylor, Juan Nieto, Roland Siegwart and Enric Galceran

Aerial Robotic Contact-based Inspection Planning and Physical Interaction Control

Kostas Alexis, Georgios Darivianakis, Michael Burri and Roland Siegwart



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- <http://ocw.mit.edu/courses/aeronautics-and-astronautics/16-410-principles-of-autonomy-and-decision-making-fall-2010/lecture-notes/>
- <http://ompl.kavrakilab.org/>
- <http://moveit.ros.org/>
- <http://planning.cs.uiuc.edu/>

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- ▶ A. Bircher, M. Kamel, K. Alexis, H. Oleynikova, R. Siegwart, "Receding Horizon "Next-Best-View" Planner for 3D Exploration", IEEE International Conference on Robotics and Automation 2016 (ICRA 2016), Stockholm, Sweden (Accepted - to be presented)

A black and white photograph of a drone flying in the foreground. The drone is a quadcopter with a white protective cover over its camera. In the background, there is a construction site with several large cranes and a building under construction. The scene is slightly blurred, suggesting motion or a shallow depth of field.

Thank you!

Please ask your question!