

# CS302 - Data Structures

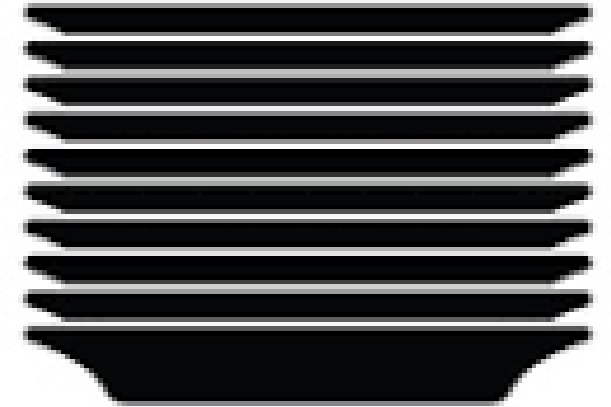
## *using C++*

Topic: The ADT Stack

Kostas Alexis

# The ADT Stack

- Stack Concept
  - **Last-in, first-out (LIFO) property**
  - Last item placed on stack will be first item removed
  - Items placed and removed on top of stack
- Analogies
  - Books on a desk
  - Dishes in a Cafeteria
  - Boxes in an attic

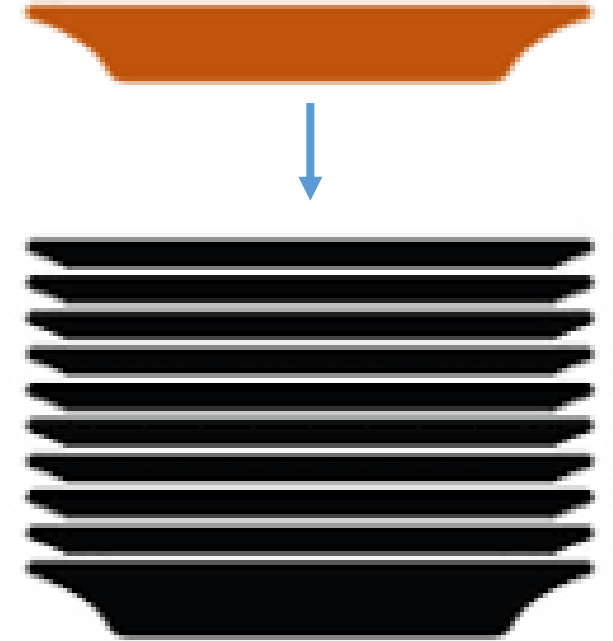


A stack analogy

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Add item



A stack analogy

# The ADT Stack

Add item

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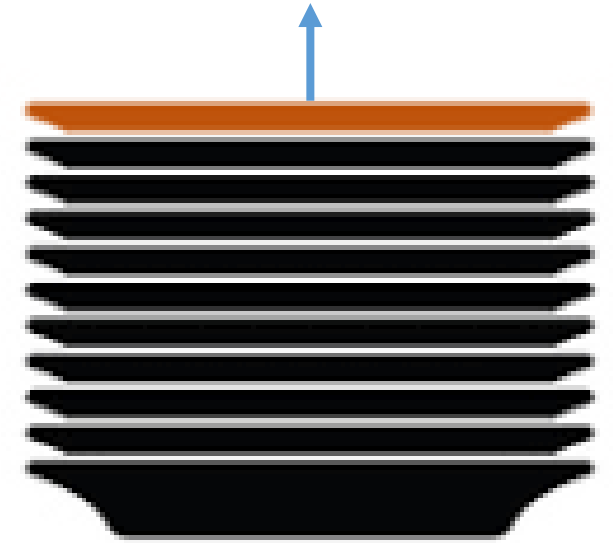


A stack analogy

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Remove item

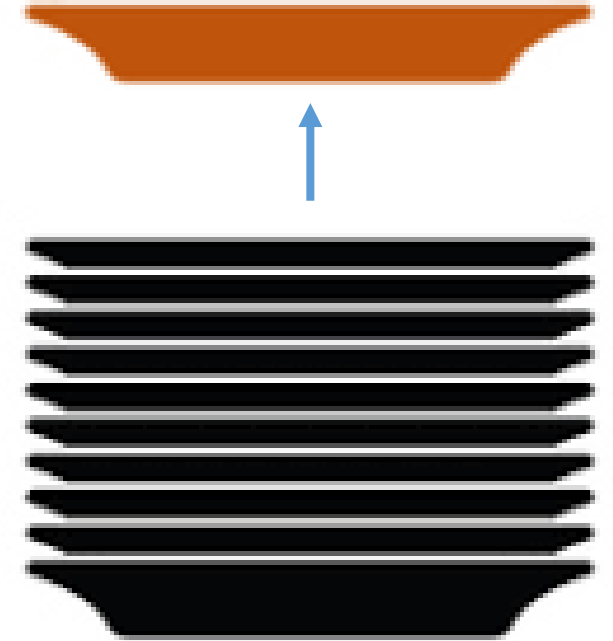


A stack analogy

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Remove item



A stack analogy

# The ADT Stack

- Stacks are heavily used in CS
  - Examples?

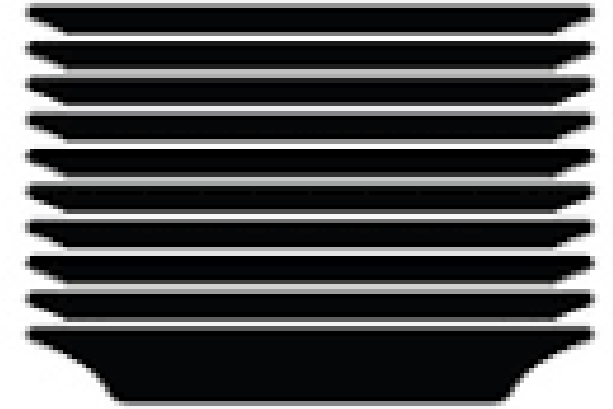
# The ADT Stack

- Stacks are heavily used in CS
  - Reverse a word
  - Undo mechanism in text editors
  - Backtracking – when you need to access the most recent data element in a series of elements
  - Function Call
    - A stack is used to keep information about the active functions or subroutines
  - Language processing:
    - Space for parameters and local variables is created internally using a stack
    - Compiler's syntax check for matching braces is implemented by using a stack
    - Support for recursion



# The ADT Stack

Restricts access “from top”

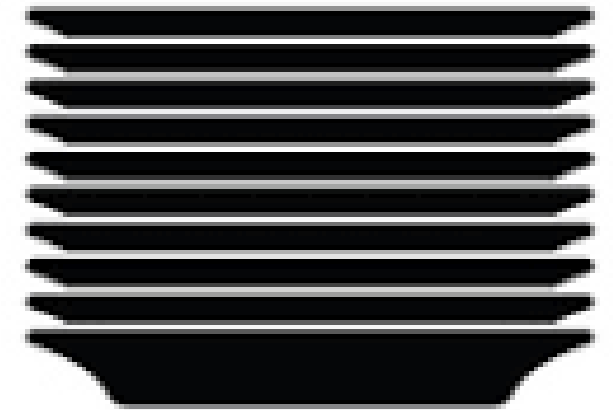


A stack analogy

# The ADT Stack

Restricts access “from top”

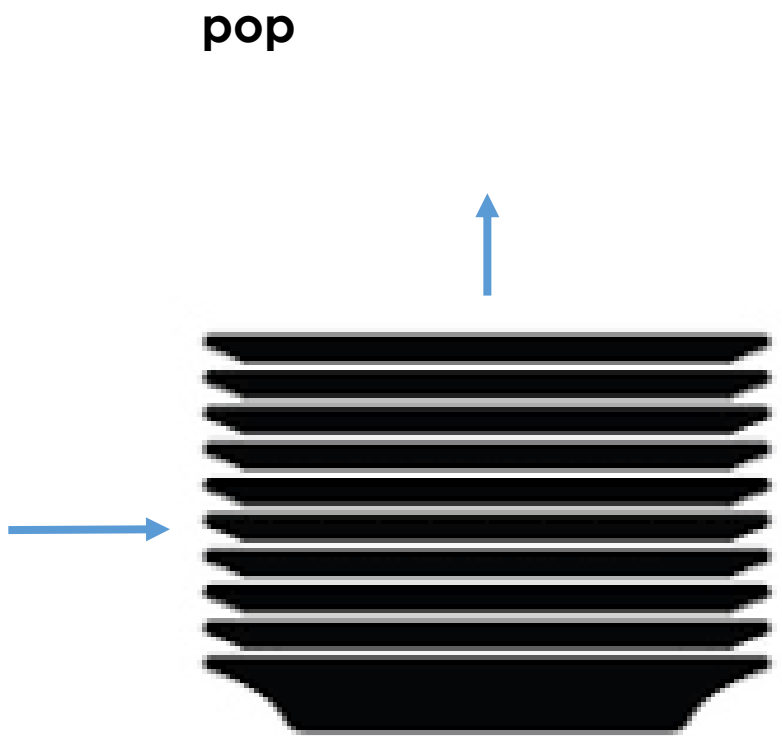
If one wants to access  
the 6<sup>th</sup>- from top entry?



A stack analogy

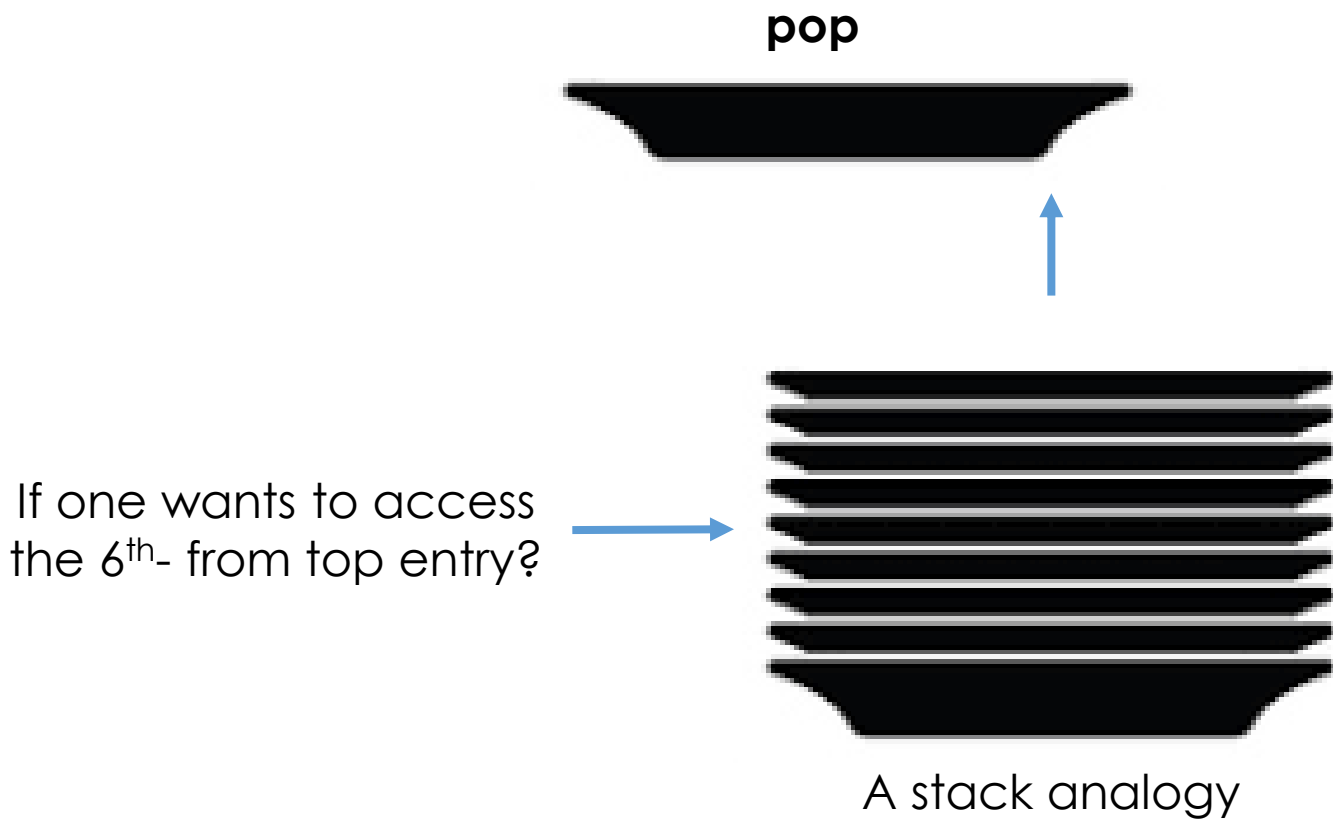
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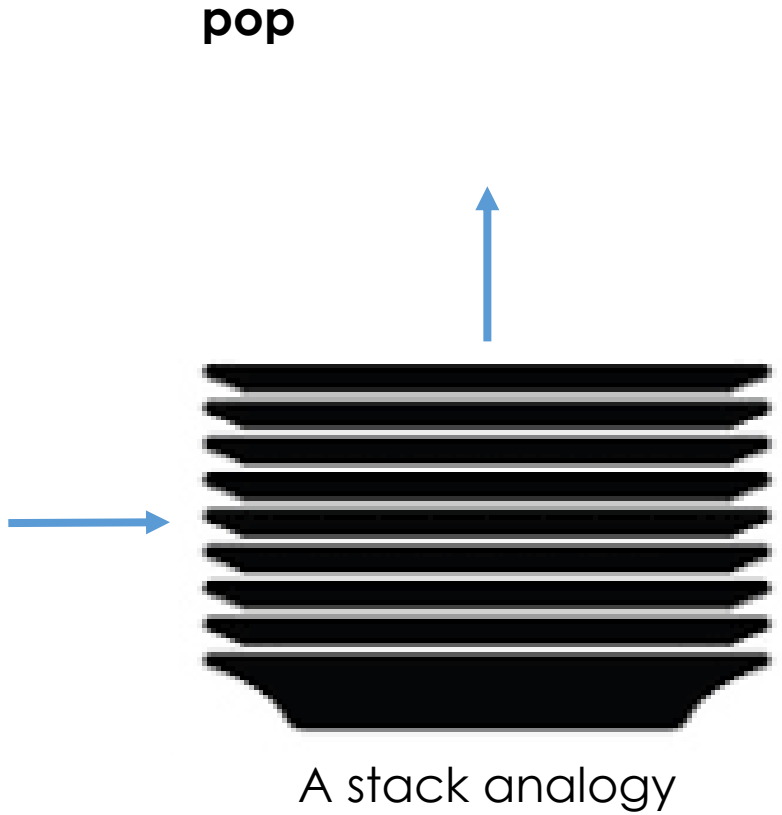
A stack analogy

# The ADT Stack

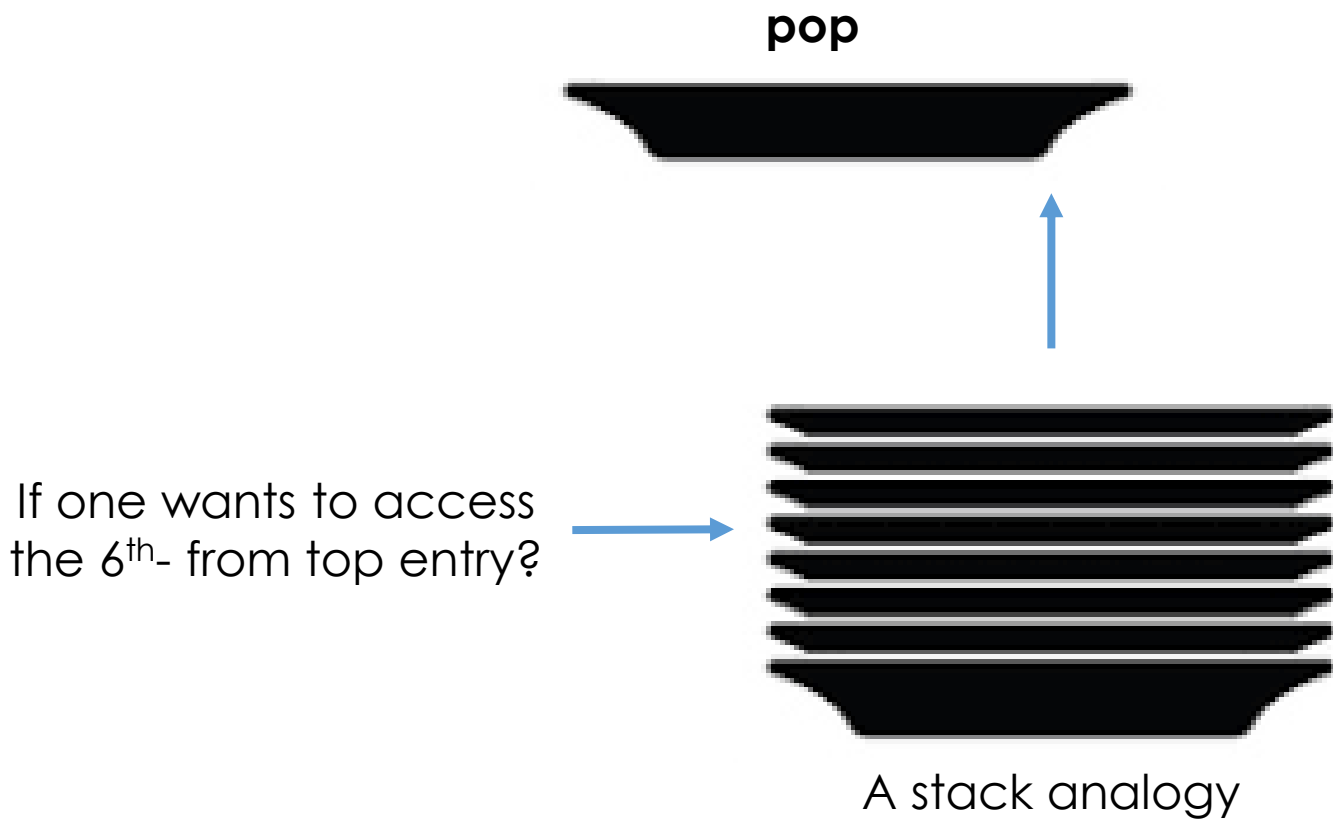


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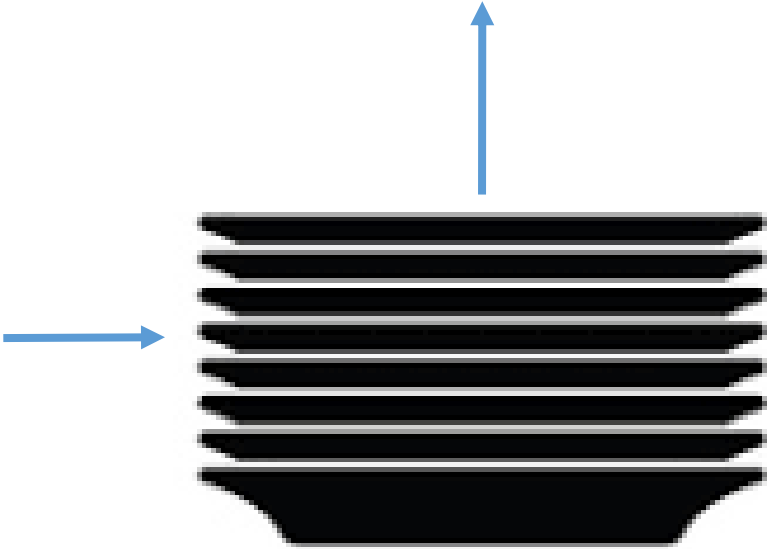


# The ADT Stack



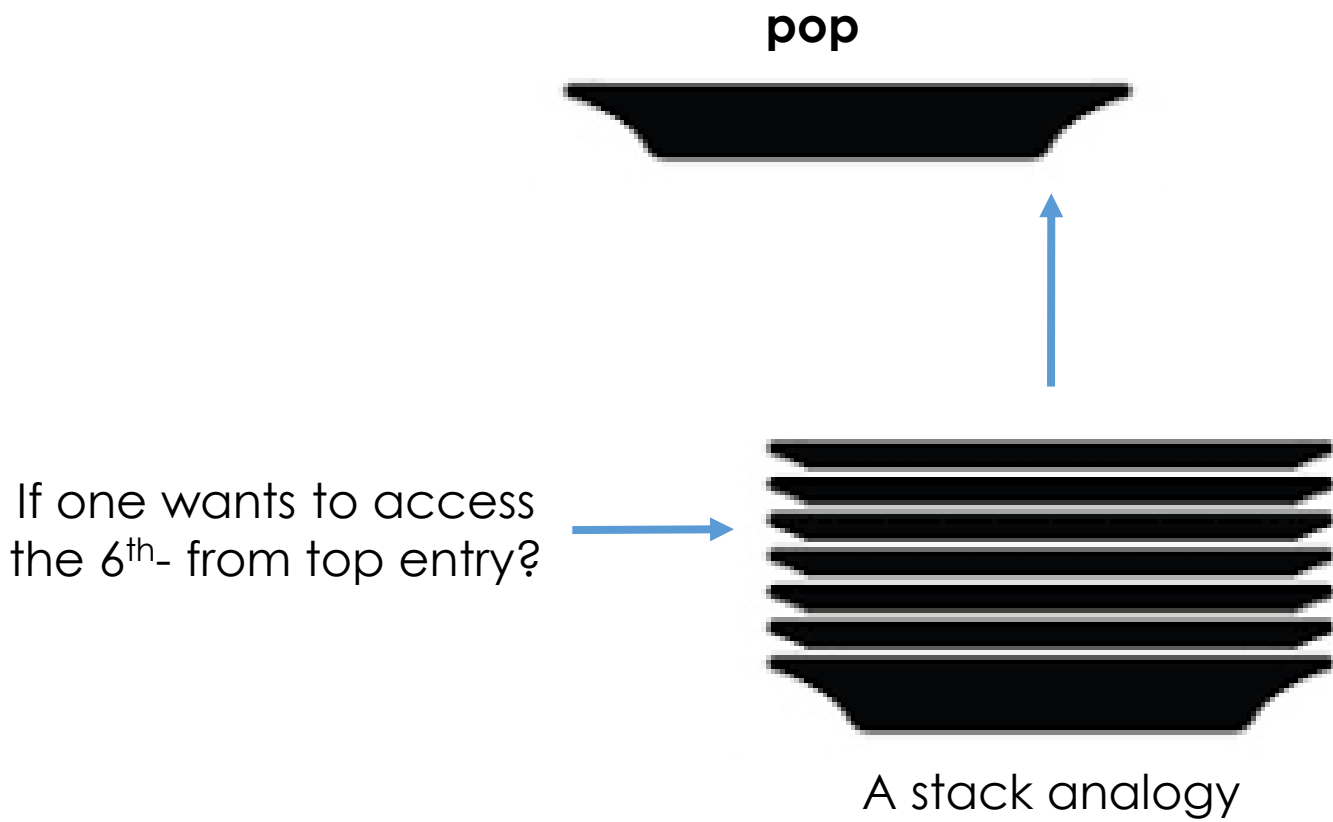
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A stack analogy

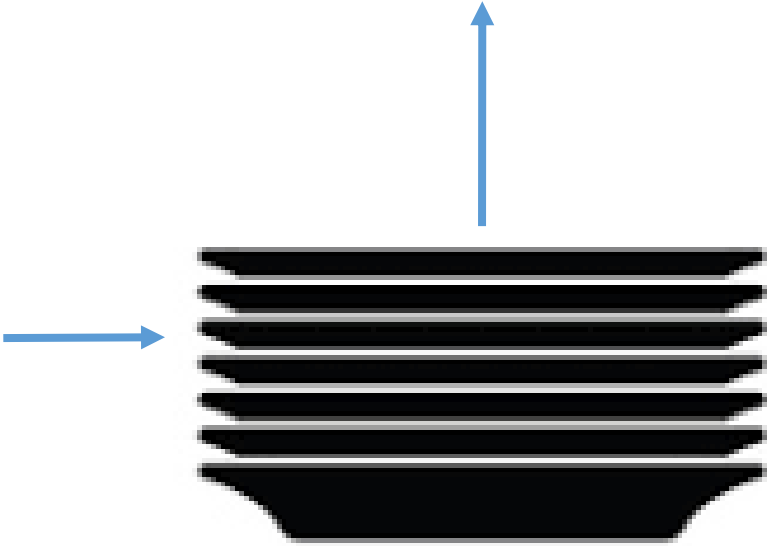
# The ADT Stack





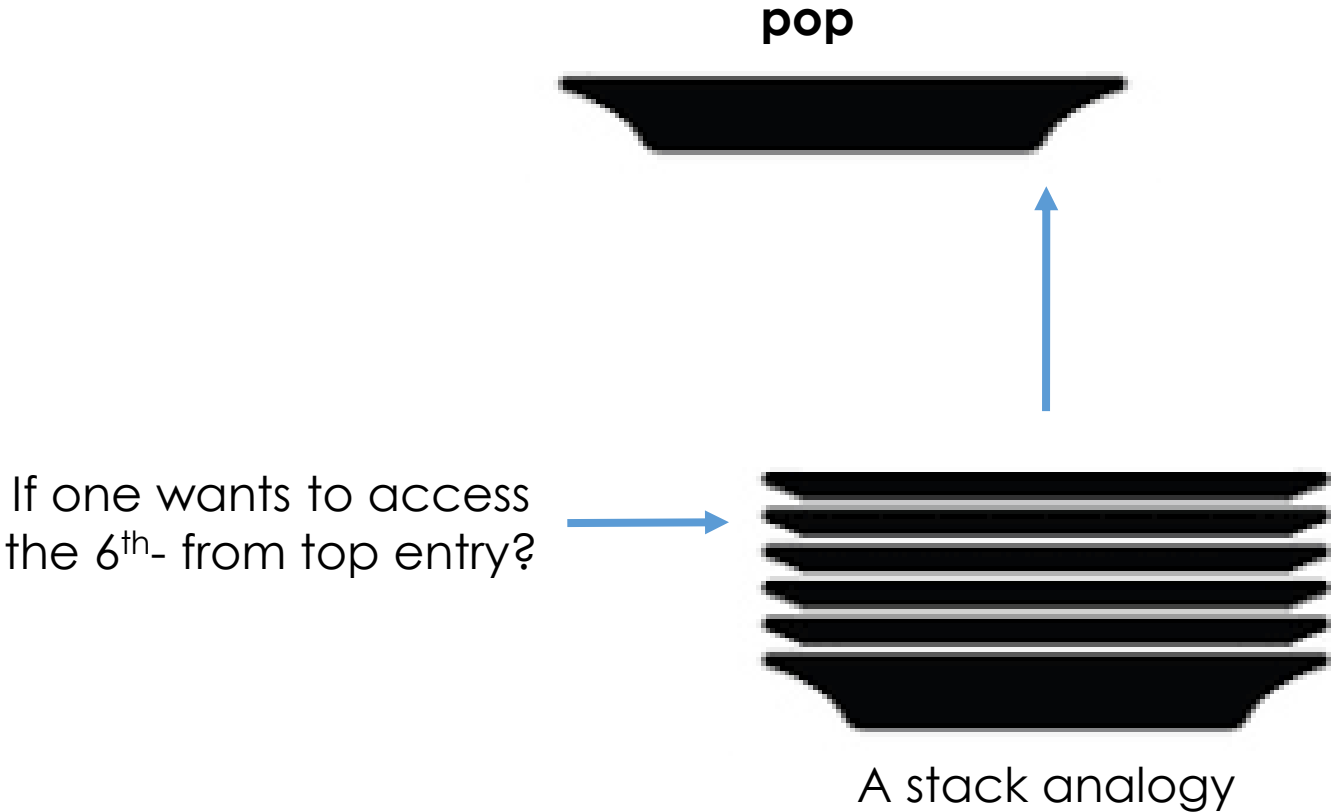
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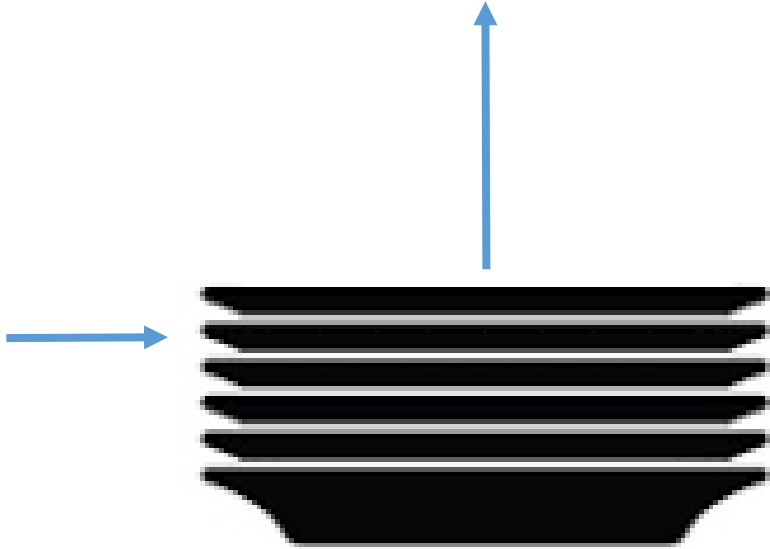
A stack analogy

# The ADT Stack



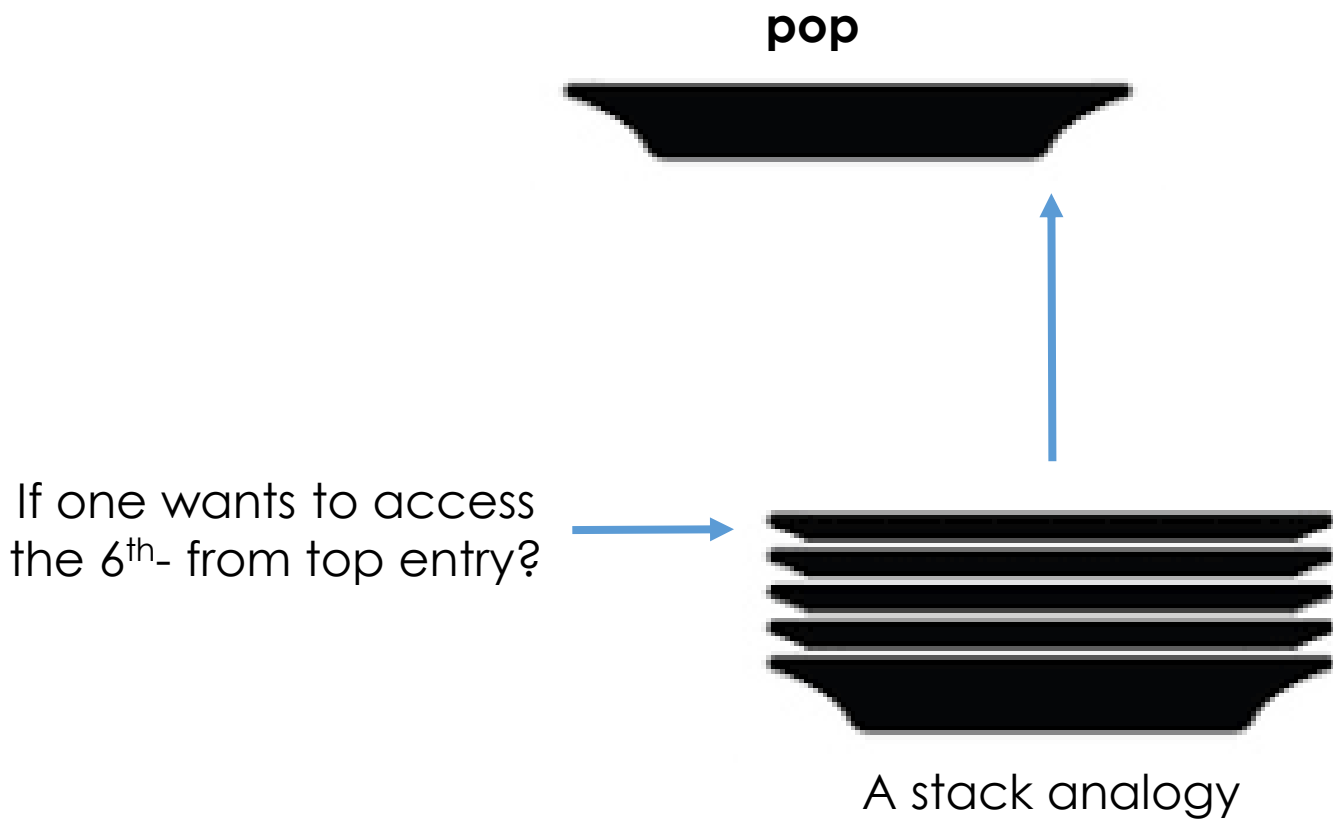
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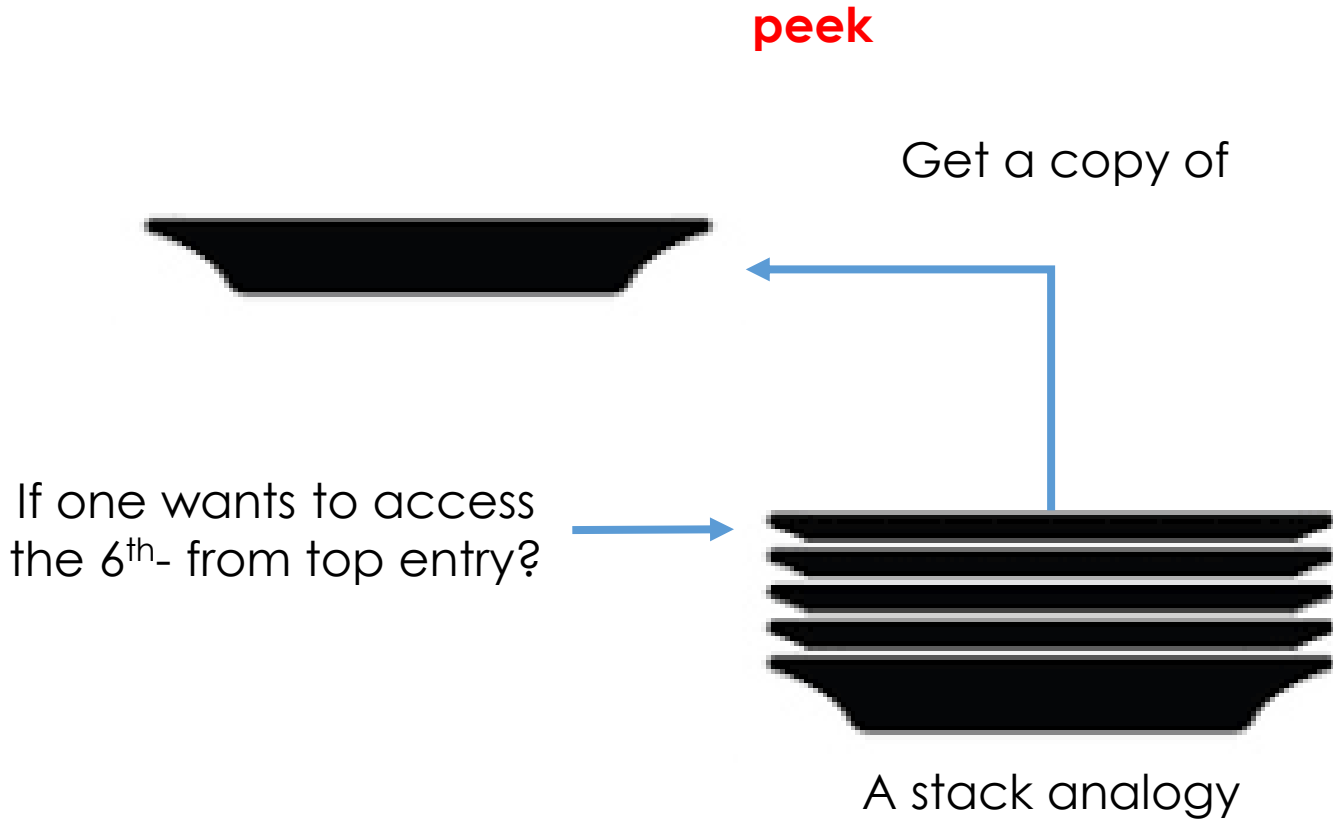


A stack analogy

# The ADT Stack



# The ADT Stack



# The ADT Stack

- Collection of items in reverse chronological order with the same data type
- ADT Stack operations
  - Add a new item to the stack: **push(ItemType newEntry)**
  - Remove item that was added most recently: **pop()**
  - Retrieve item that was added most recently: **ItemType peek()**
  - Determine whether a stack is empty: **boolean isEmpty()**

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  - Add a new item to the stack: `push(ItemType newEntry)`
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Only returns a copy – the item is not removed from the stack

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- ADT Stack operations
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```
Stack
+isEmpty(): boolean
+push(newEntry: ItemType): boolean
+pop(): boolean
+peek(): ItemType
```



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**push(ItemType newEntry)**
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  - Determine whether a stack is empty:  
**boolean isEmpty()**

```
/** @file StackInterface.h */

#ifndef STACK_INTERFACE_
#define STACK_INTERFACE_

template<class ItemType>
class StackInterface
{
public:
    virtual bool isEmpty() const = 0;
    virtual bool push(const ItemType& newEntry) = 0;
    virtual bool pop() = 0;
    virtual ItemType peek() const = 0;
    virtual ~StackInterface() { }
}; // end StackInterface

#endif
```

# Using the ADT Stack

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```
stack<std::string>* stringStack = new Stack<std::string>();
stringStack->push("Jim");
stringStack->push("Jess");
stringStack->push("Jill");
stringStack->push("Jane");
stringStack->push("Joe");

std::string top = stringStack->peek();
std::cout << top << " is at the top of the stack \n";

if(stringStack->pop())
    std::cout << top << " is removed from the stack \n";

top = stringStack->peek();
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Jim

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Jess  
Jim

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Jill  
Jess  
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Joe  
Jane  
Jill  
Jess  
Jim

Joe is at the top of the stack

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Jill  
Jess  
Jim

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Joe is removed from the stack  
Jane is at the top of the stack

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Jill  
Jess  
Jim

Joe is at the top of the stack  
Joe is removed from the stack  
Jane is at the top of the stack  
Jane is removed from the stack

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# Using the ADT Stack

- Checking for balanced expressions

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- Checking for balanced expressions

OK                      NOT OK

{ [ ( ) ( ) ] ( ) }      [ ( ] )

# Using the ADT Stack

- Checking for balanced expressions
  - Scan expression:
    - Discard characters that are not delimiters

{ [ ( ) ( ) ] ( ) }

[ ( ] )

a { b [ c ( d + e ) / 2 - f ] + 1 }

# Using the ADT Stack

- Checking for balanced expressions
  - Scan expression:
    - Discard characters that are not delimiters
  - When open delimiter is encountered
    - **push** it on the stack

{ [ ( ) ( ) ] ( ) }

[ ( ]

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  - Scan expression:
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  - When open delimiter is encountered
    - **push** it on the stack
  - When close delimiter is encountered
    - Check to see if it matches top of stack
    - If yes, **pop** off top of stack
    - If not, expression is not balanced

{ [ ( ) ( ) ] ( ) }

[ ( ] )

a { b [ c ( d + e ) / 2 - f ] + 1 }



# Using the ADT Stack

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  - If braces are balanced
    - Stack is empty when expression is done

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[ ( ]

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  - If braces are balanced
    - Stack is empty when expression is done

{ [ ( ) ( ) ] ( ) }

[ ( ]

a { b [ c ( d + e ] / 2 - f ) + 1 }

# Using the ADT Stack (of characters)

- Checking for balanced expressions

```
// Returns true if the given characters, open and close, form a
// pair of parentheses, brackets, or braces

bool isPaired(char open, char close)
{
    return (open == '(' && close == ')') ||
           (open == '[' && close == ']') ||
           (open == '{' && close == '}');
}; // end isPaired
```

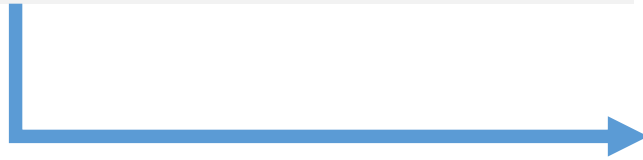
Helper method

# Using the ADT Stack (of characters)

```
bool checkBalance(string expression)
{
    Stack<char> openDelimiterStack = new Stack<char>();
    int characterCount = expression.length();
    bool isBalanced = true;
    int index = 0;
    char nextCharacter = ' ';
```

```
// Returns true if the given characters, open and close, form a
// pair of parentheses, brackets, or braces
```

```
bool isPaired(char open, char close)
{
    return (open == '(' && close == ')') ||
           (open == '[' && close == ']') ||
           (open == '{' && close == '}');
}; // end isPaired
```



```
while (isBalanced && (index < characterCount)) {
    nextCharacter = expression.charAt(index);
    switch (nextCharacter)
    {
        case '(': case '[': case '{':
            openDelimiterStack->push(nextCharacter);
            break;
        case ')': case ']': case '}':
            if (openDilimiterStack->isEmpty())
                isBalanced = false;
            else
            {
                char openDilimeter = openDilimeterStack->peek();
                openDelimiterStack->pop();
                isBalanced =
                    isPaired(openDilimeter, nextCharacter);
            } // end if
            break;
        default:
            break;
    } // end switch
    index++;
} // end while
if (!openDilimeterStack->isEmpty())
    isBalanced = false;
return isBalanced;
} // end checkBalance
```

**Thank you**